

Quantum Simulation of Solid-State Systems with Ultracold Atoms

Jacopo Catani

National Institute of Optics (INO-CNR)
Sesto Fiorentino (Florence)

LENS – University of Florence

PhD in Quantum technologies

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UNIVERSAL

Feynman's approach

~~'Employing a Universal Quantum Computer~~
allows to simulate **any** Quantum System'



Quantum Simulators: pillar of QT

“AD HOC”

FeynNormalMan’s approach

**Retrieve properties of a «tricky» Quantum System
by implementing a physically equivalent one**



«Engineer» effective Hamiltonians

Ultracold Atoms – a powerful tool

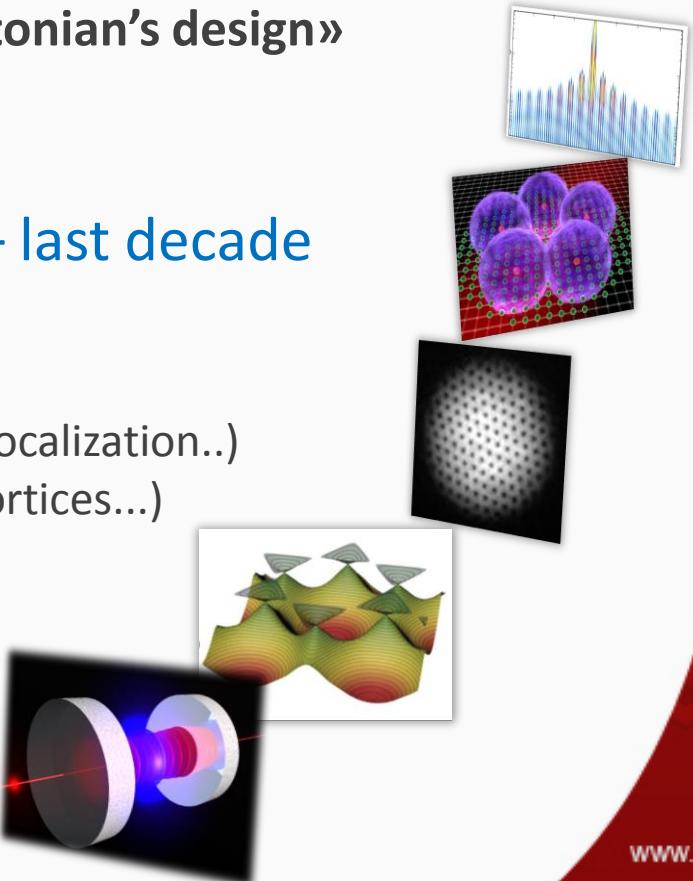
Ultracold Atoms platform



unprecedented **control** and **versatility** in «Hamiltonian's design»

Quantum Simulation with UCA – last decade

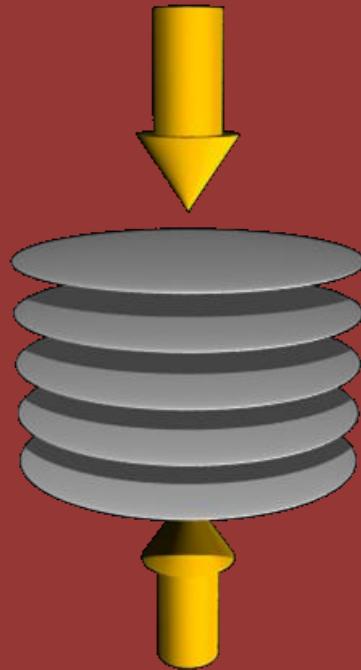
- Superfluidity, BEC/BCS crossover
- Lattice Phase transitions (Mott, Anderson Localization..)
- Low dimensional physics (Tonks gas, BKT, vortices...)
- Synthetic FIELDS -> Hall-like systems



«Solid-state-like» systems

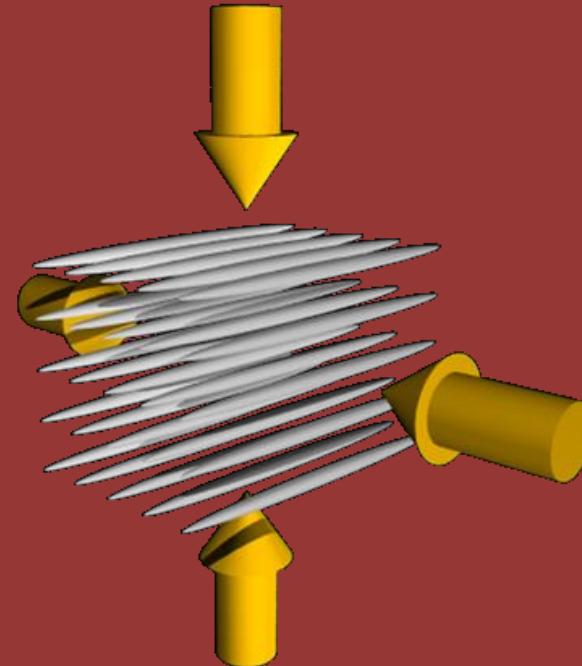
Quantum Manipulation through Light

Ultracold gases offer a unique platform in association to **OPTICAL LATTICES**



2D systems

BKT,
quantum Hall systems,
graphene, ...



1D systems

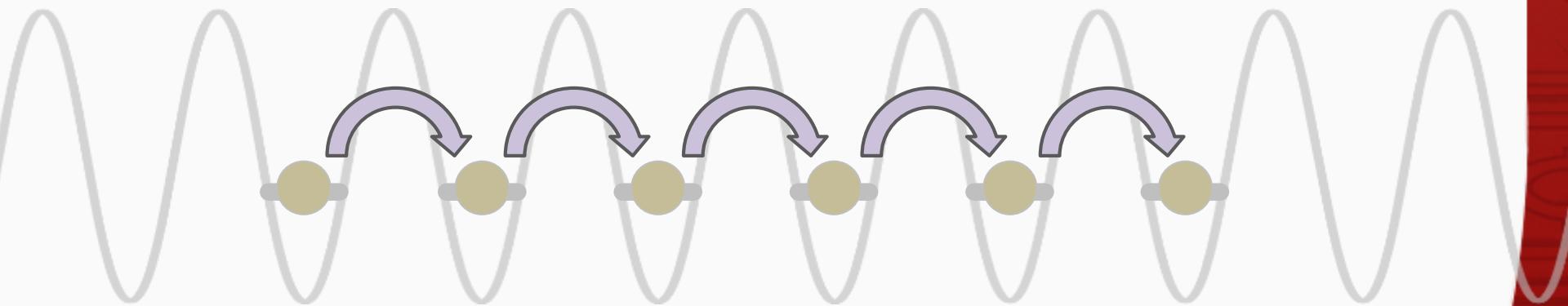
carbon nanotubes,
nanowires, ...

Optical manipulation / lattices

Adjusting the light intensity allows for tuning of the tunneling

$$H = -t \sum_{\langle i,j \rangle, \sigma} (\hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + \text{h.c.}) + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow} + \sum_i \varepsilon_i \hat{n}_i$$

Fermi-Hubbard (spin $\frac{1}{2}$)



«Real» spatial lattice
Spacing as tight as $\lambda/2$
Depth U up to 100ths of recoils

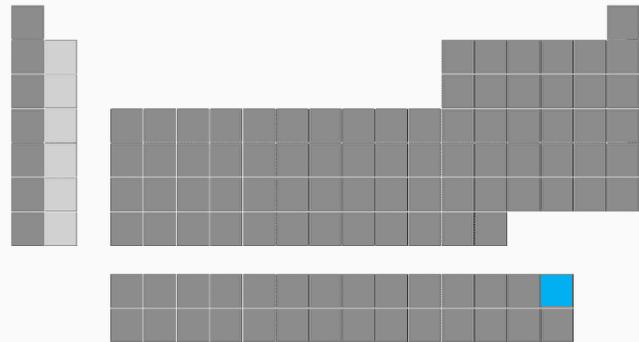


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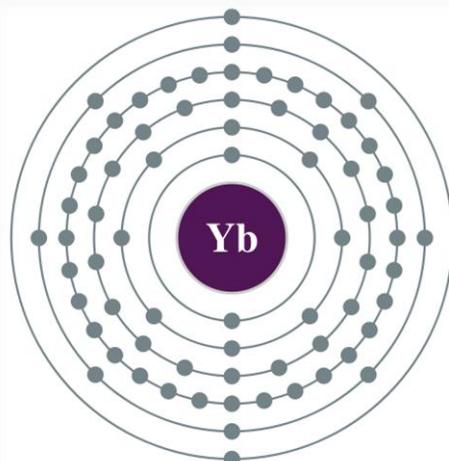


Quantum gases of Ytterbium

The large Ytterbium family...

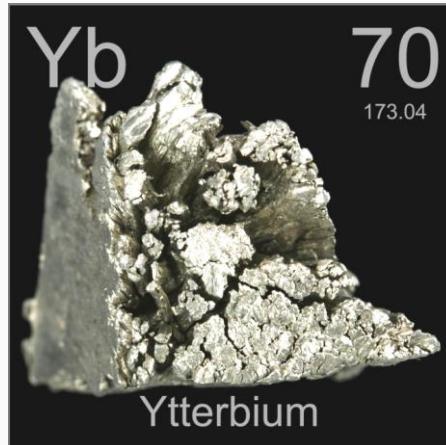


<http://periodictable.com>

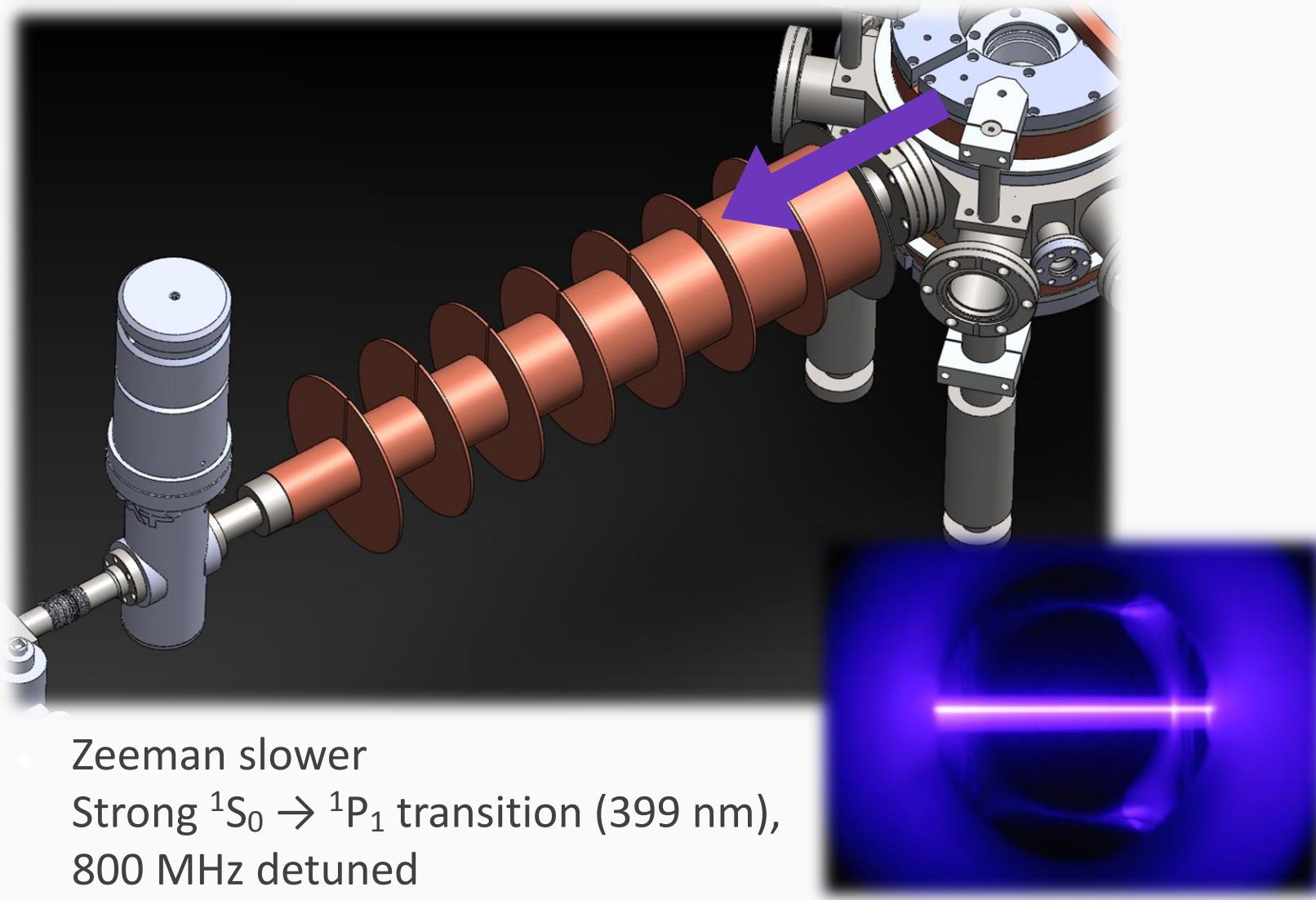


Natural Ytterbium comes in **seven** stable isotopes:

| | | | |
|-------------------|--------|---------|---------|
| ^{168}Yb | 0.13% | $I=0$ | boson |
| ^{170}Yb | 3.04% | $I=0$ | boson |
| ^{171}Yb | 14.28% | $I=1/2$ | fermion |
| ^{172}Yb | 21.83% | $I=0$ | boson |
| ^{173}Yb | 16.13% | $I=5/2$ | fermion |
| ^{174}Yb | 31.83% | $I=0$ | boson |
| ^{176}Yb | 12.76% | $I=0$ | boson |

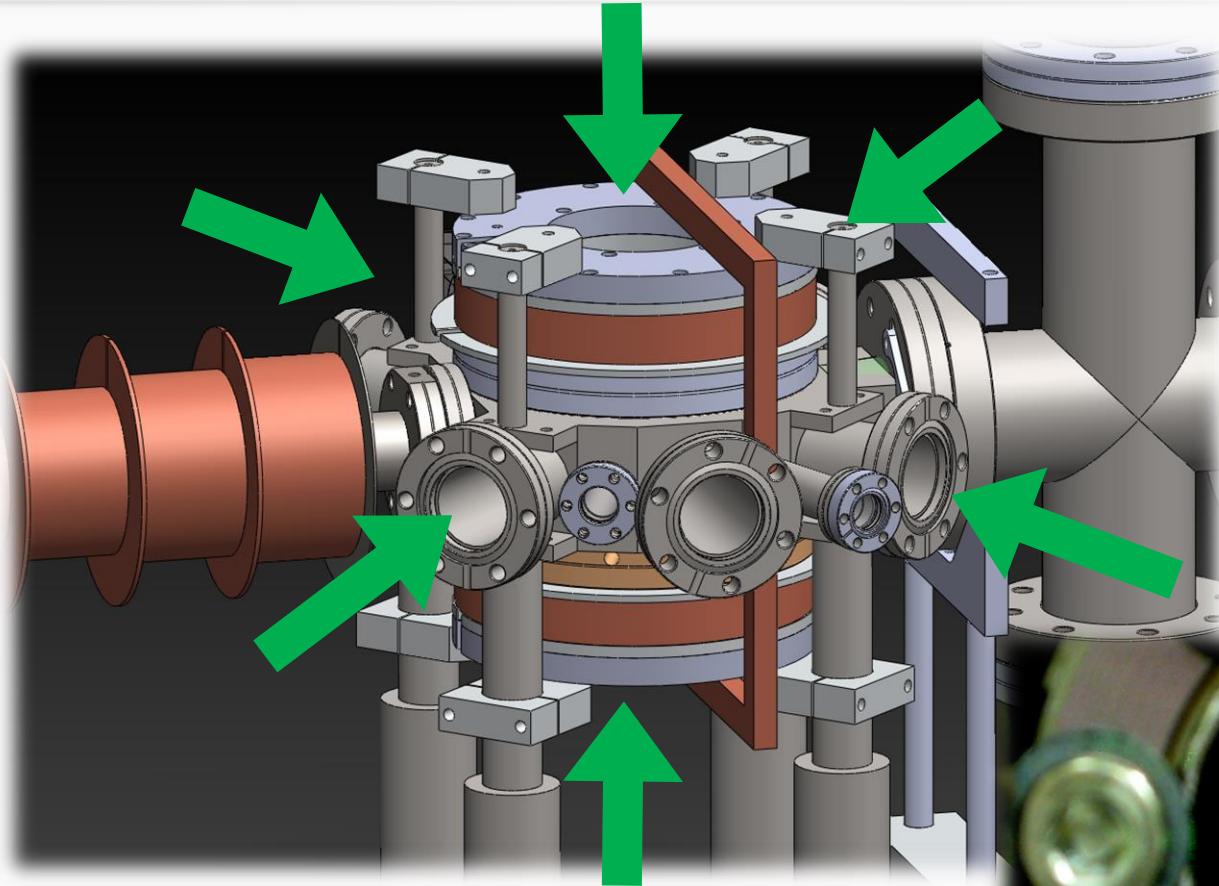


Atomic beam slowing

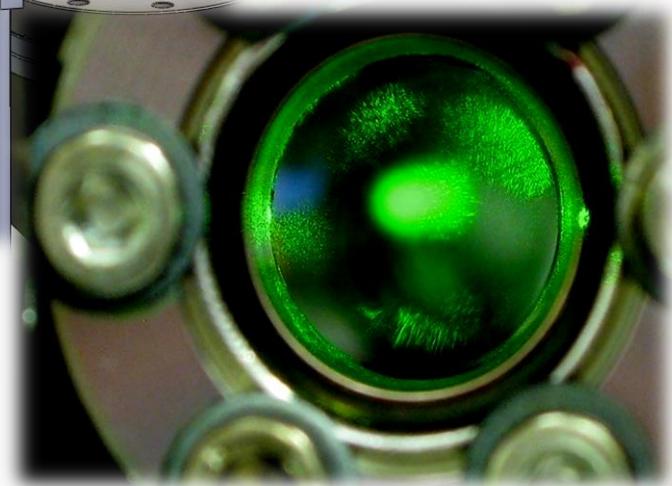


- Zeeman slower
Strong $^1S_0 \rightarrow ^1P_1$ transition (399 nm),
800 MHz detuned
- Final atom velocity: ≈ 20 m/s

Laser cooling of Ytterbium



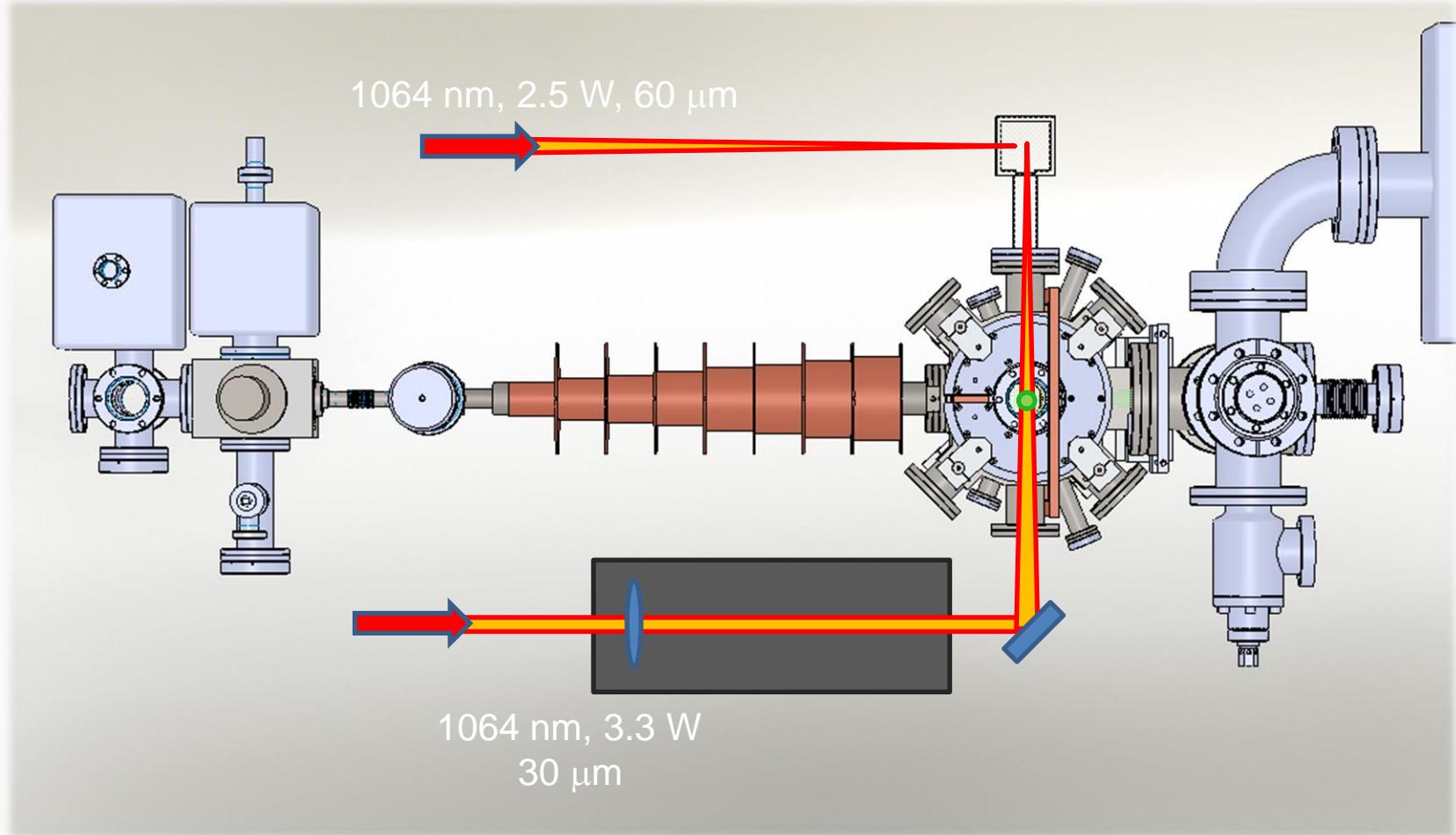
MAGNETO
OPTICAL
TRAP
(MOT)



Temperature: $\approx 30 \mu\text{K}$

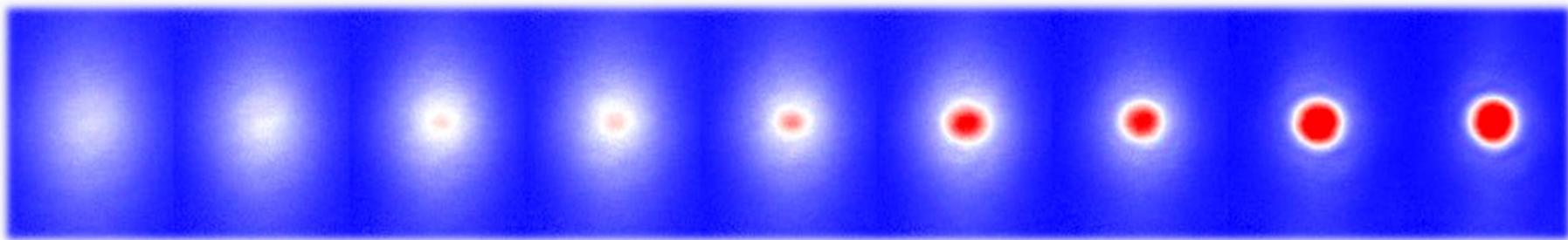
Number of atoms $\approx 10^9$

Optical transport of atomic sample



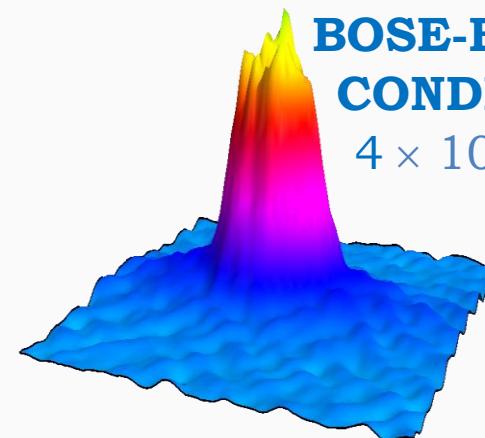
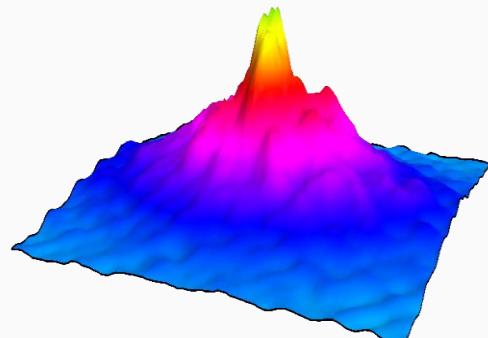
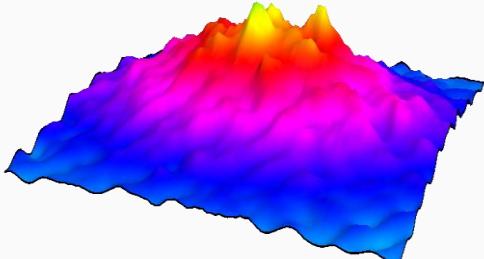
Quantum degeneracy - Bosons

Time-of-flight images: momentum distribution



$T \approx 400 \text{ nK}$
Thermal

$N_{\text{tot}} \approx 1 \text{ million}$



$T \approx 70 \text{ nK}$

Pure
BOSE-EINSTEIN
CONDENSATE
 $4 \times 10^5 \text{ atoms}$

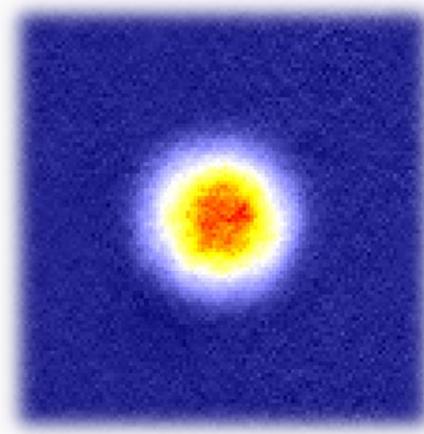
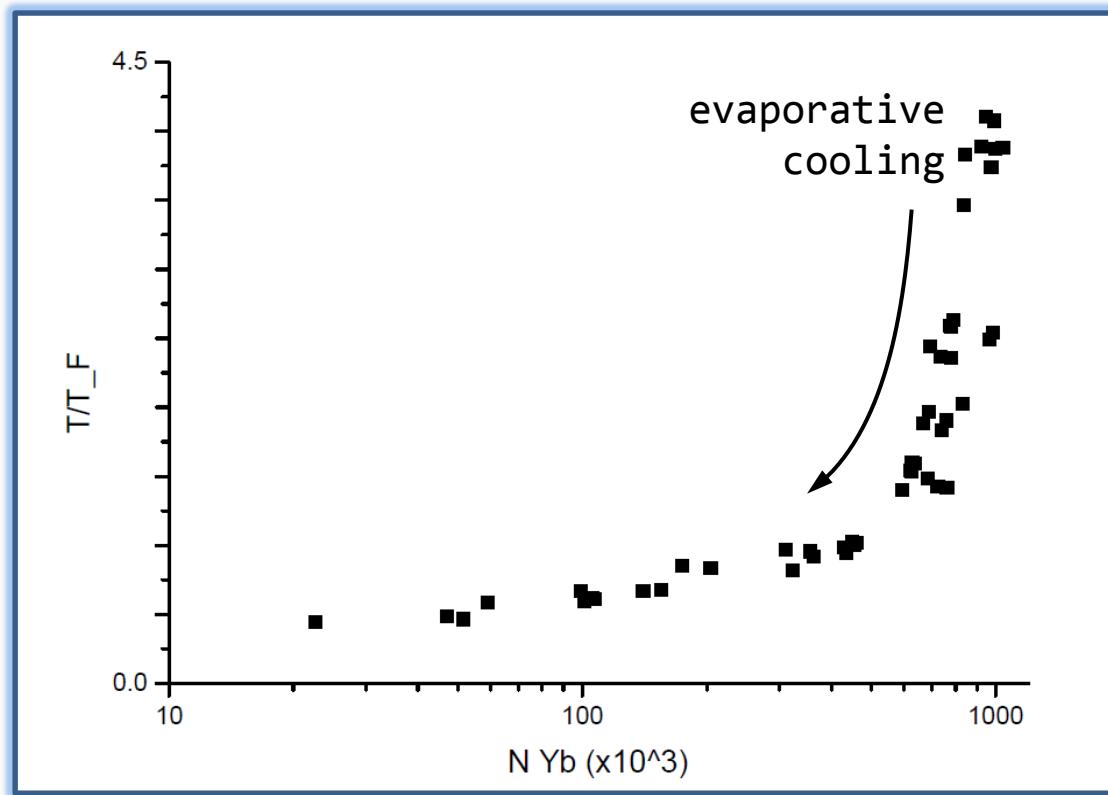
Quantum degeneracy - Fermions

^{173}Yb : evaporative cooling of a **spin mixture**

(6 components)

Nuclear spin $I=5/2$

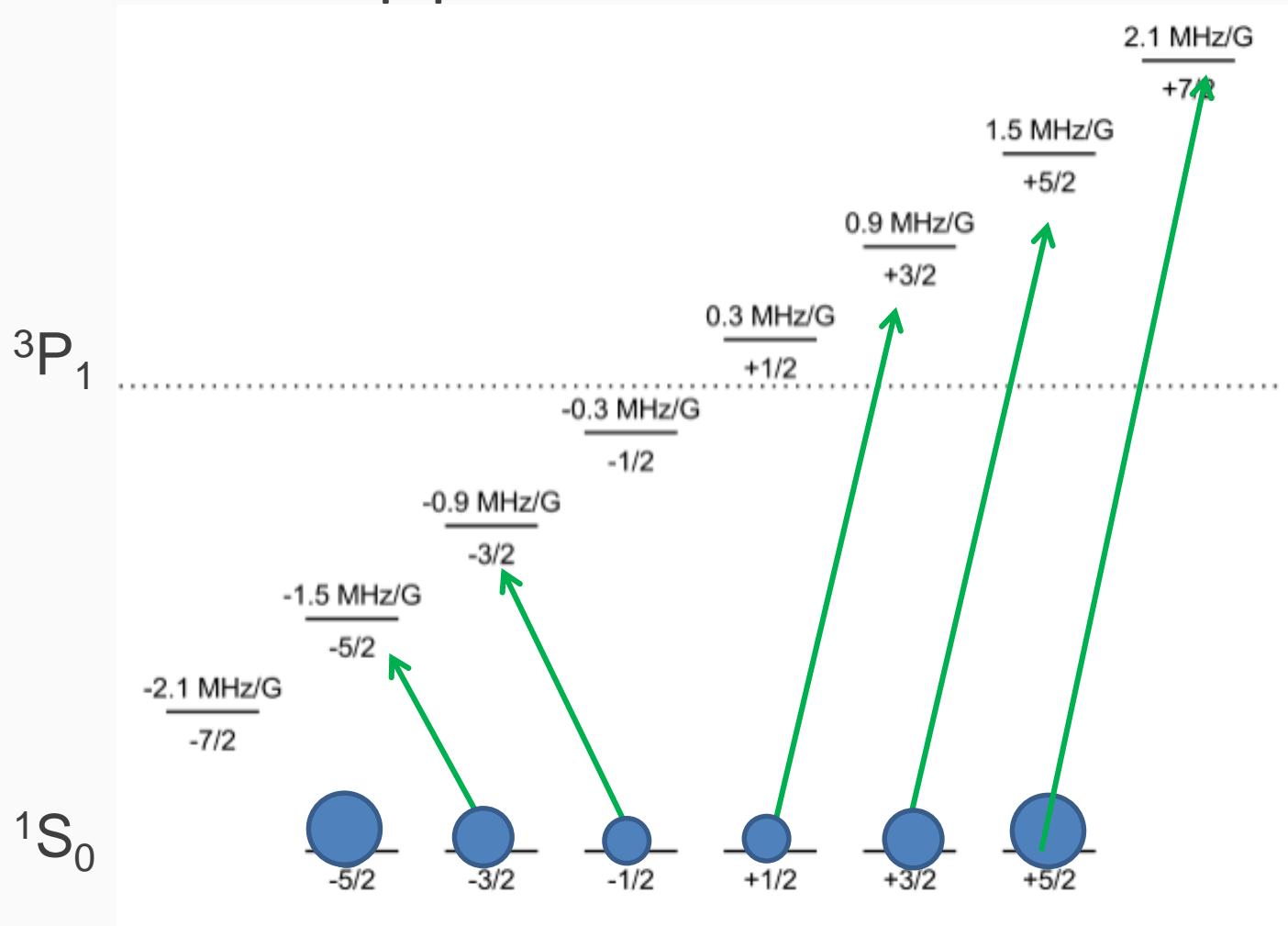
-5/2 ————— +5/2



^{173}Yb Fermi gas
 $T/T_F < 0.1$ (20 nK!)
 $N = 1 \times 10^4$ atoms/spin

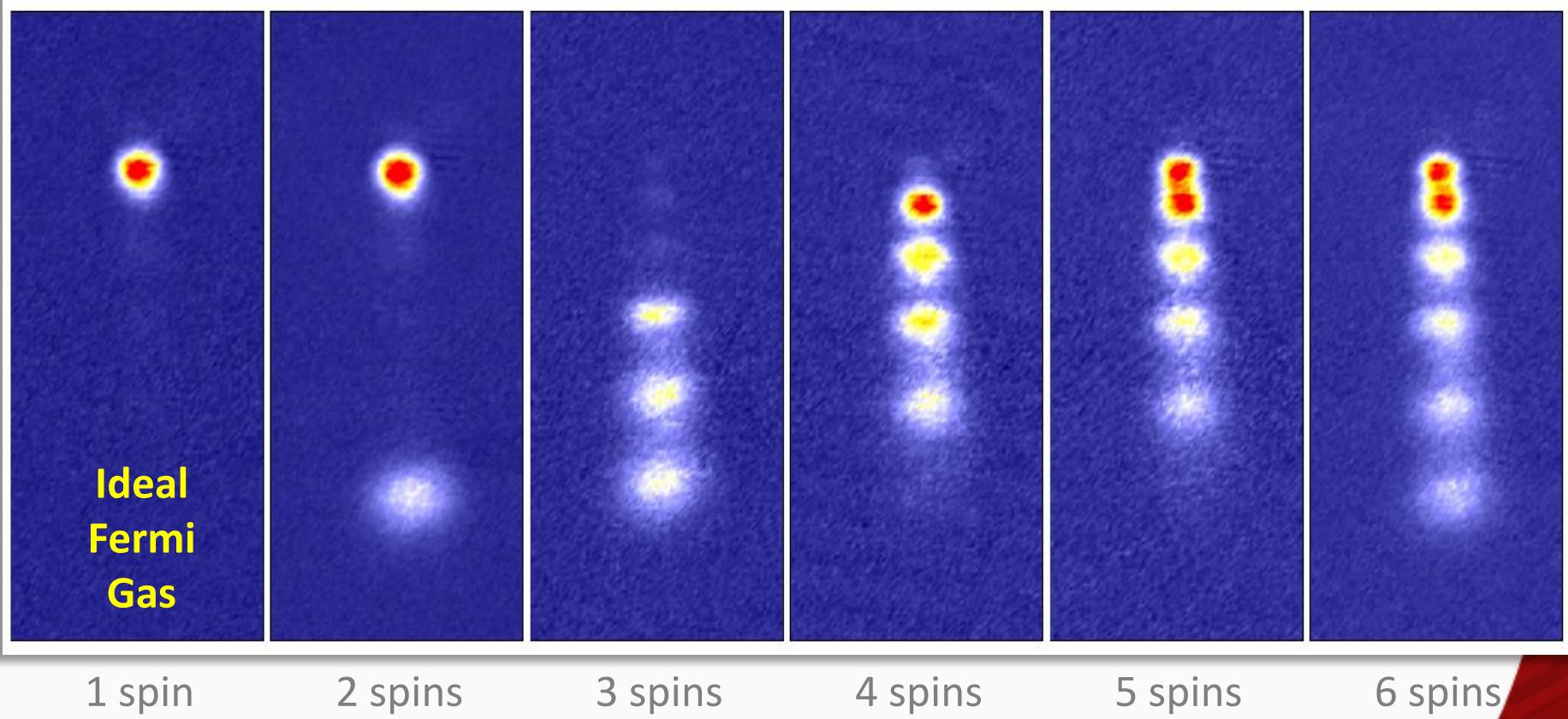
Spin Manipulation

Optical pumping through sequence of resonant light pulses and B field control of the population in each Zeeman sublevel



Spinful Quantum Gases

^{173}Yb Fermi gases in an arbitrary number of equally-populated components:



1 spin

2 spins

3 spins

4 spins

5 spins

6 spins



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Engineering Hall Systems with Atoms

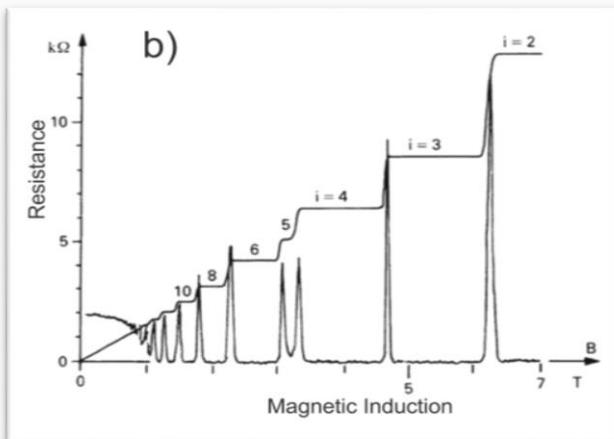
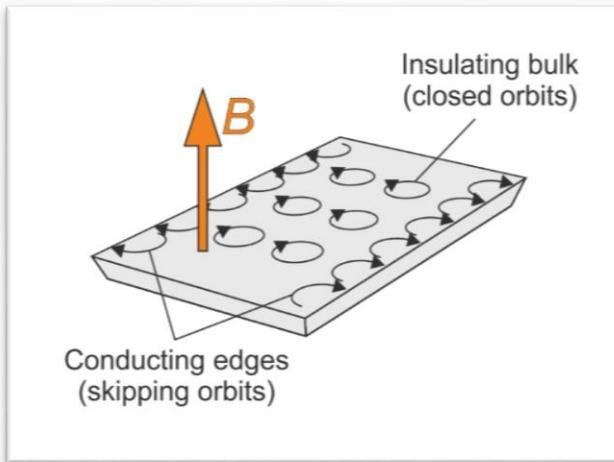
Quantum Hall Effect in a Nutshell

Quantum Hall effect

(th. Ando, Matsumoto, Uemura 1975, Laughlin 1981)

(exp: Von Klitzing 1990)

Charged 2D Particles (e^-) in strong B field



- Quantized Cyclotron Orbits (Landau levels)
Insulating Bulk States
- Skipping Orbit at boundaries
Superconducting Edge States
- Quantized plateaux in transv. conductance
for critical values of B

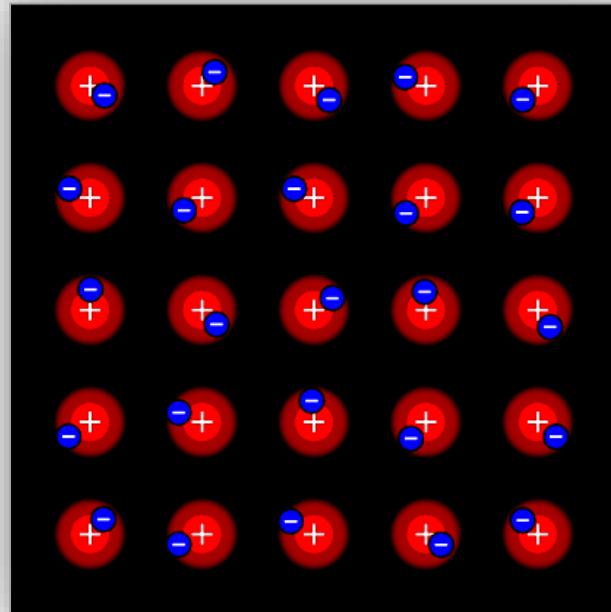


$$\sigma = \nu \frac{e^2}{h}$$

$$B = \frac{n_0 h}{e \nu}$$

Simulating crystals under ***B*** fields with atoms

Underlying lattice structure: exploit advantages in manipulation of atomic systems



...electrons are CHARGED PARTICLES, whilst ATOMS are
NEUTRAL...



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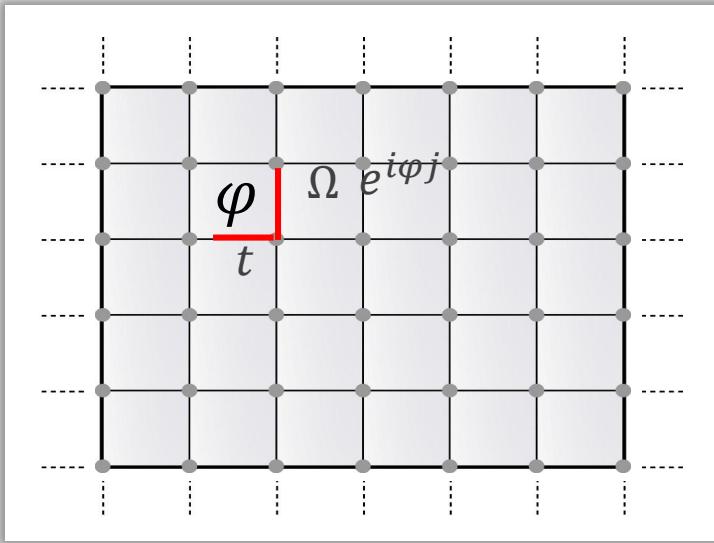
...what's the trick...?

Harper – Hofstadter Hamiltonian

charged particle in a 2d lattice + magnetic field

Harper, Proc. Phys. Soc. A **68**, 874 (1955)

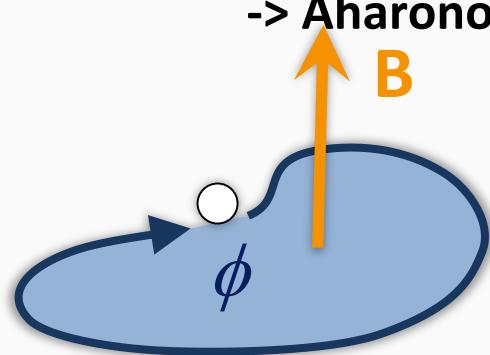
$$H = -t \sum_{j,m} (c_{j,m}^\dagger c_{j+1,m} + h.c.) - \Omega \sum_{j,m} (e^{i\varphi j} c_{j,m}^\dagger c_{j,m+1} + h.c.)$$



Can be imprinted by laser beams!
ARTIFICIAL GAUGE FIELDS

D. Jaksch and P. Zoller, NJP **5**, 56 (2003)

Geometric (Peierls) phase
Embeds **B** field and charge
-> Aharonov-Bohm!

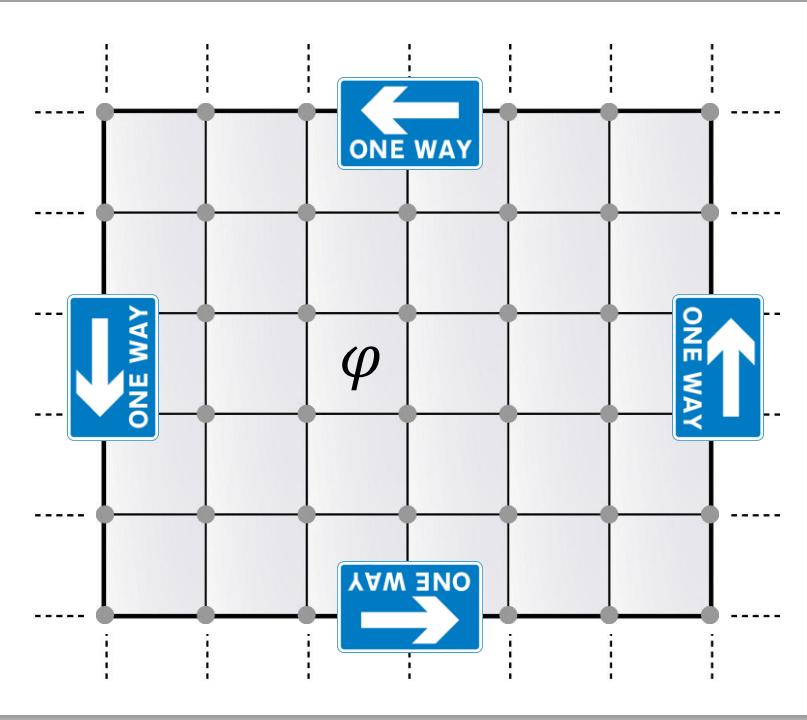


$$\psi \rightarrow e^{i\phi} \psi \quad \phi = \frac{2\pi e}{h} \Phi_B$$

Harper-Hofstadter model features

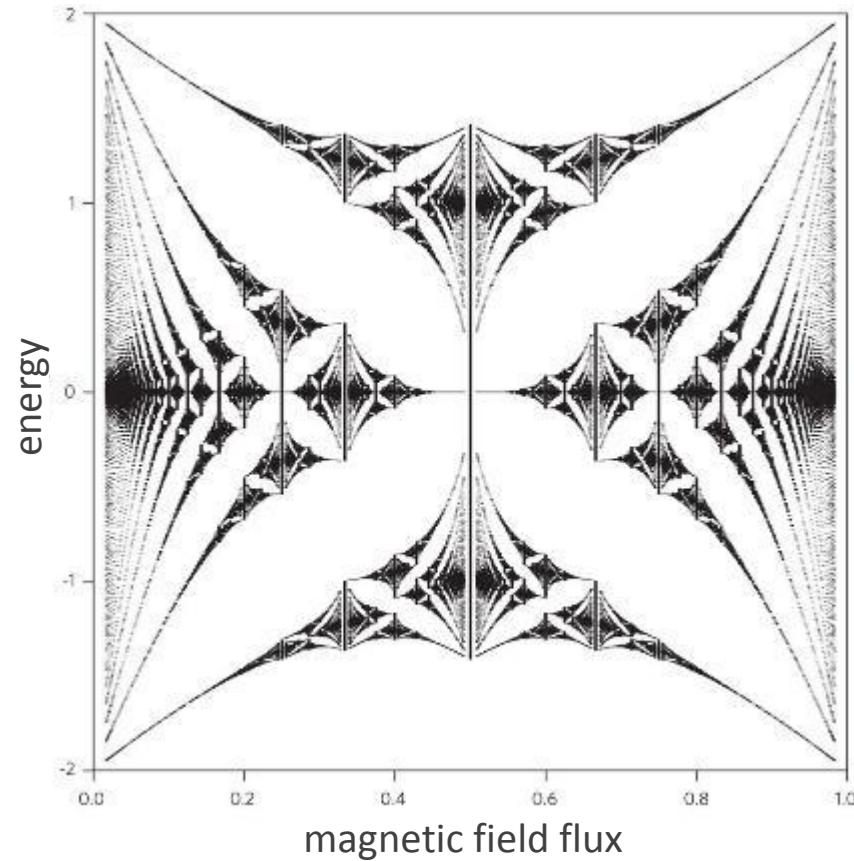
Features of the model

chiral edge currents



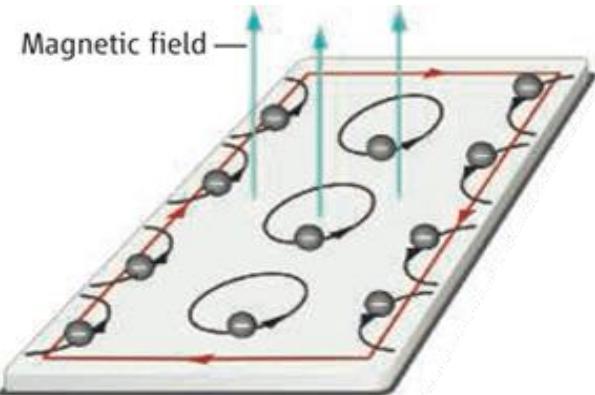
Hofstadter, PRB **14**, 2239 (1976)
Promptly left Physics for Cognitive Science

Hofstadter «Butterfly» spectrum

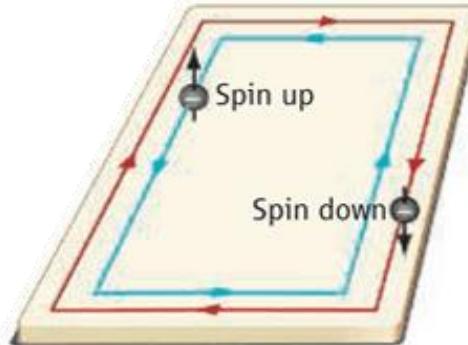


Edge States

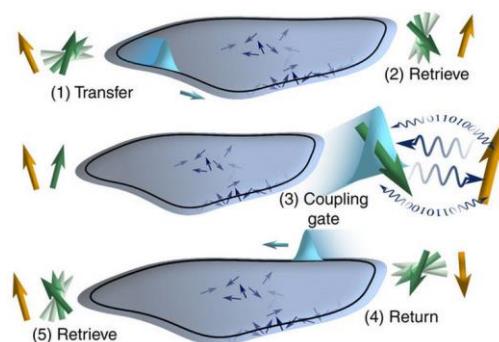
Quantum Hall effect



Topological insulators



ROBUSTNESS > Quantum technology



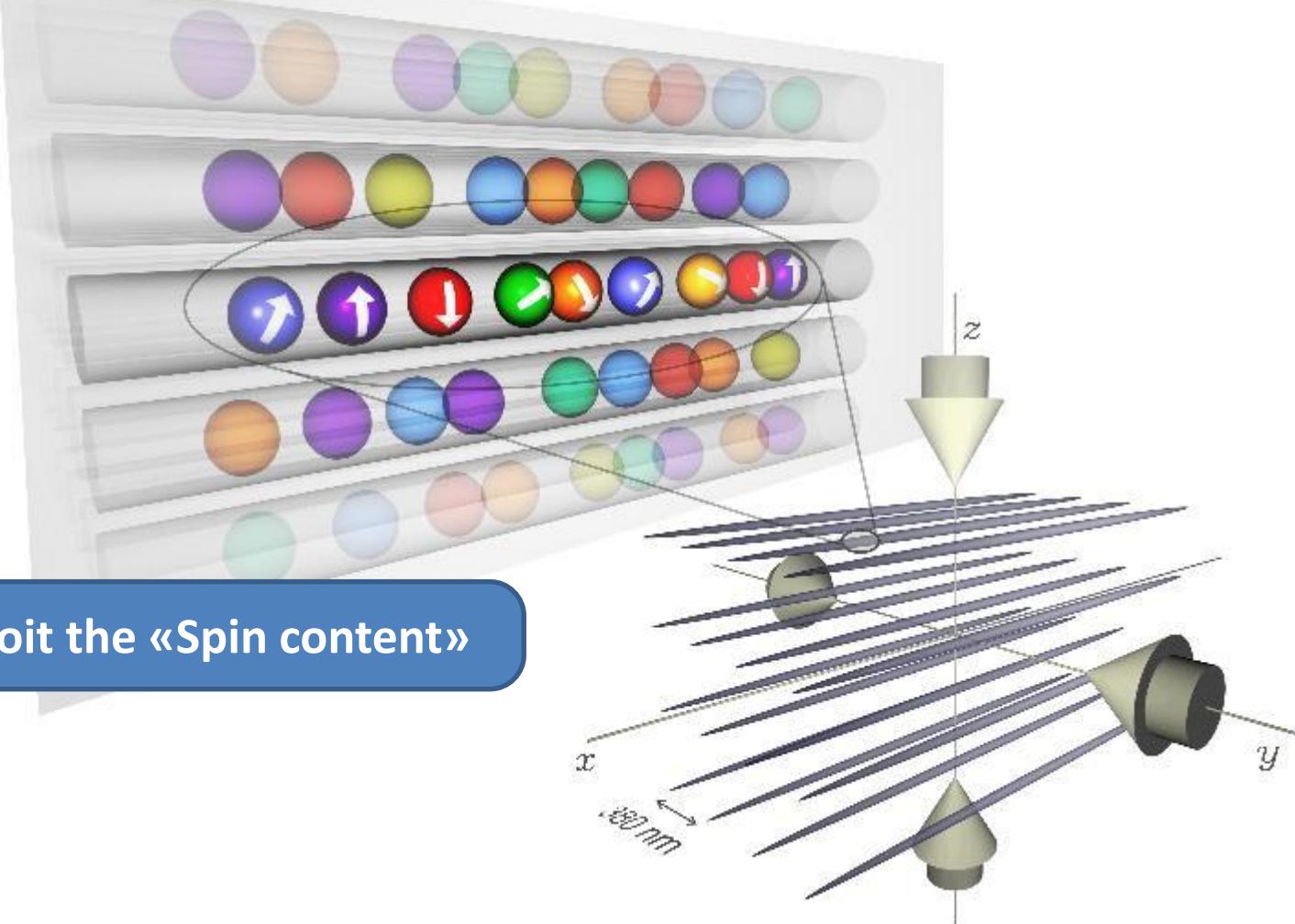


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...preparation of Atomic Hall ribbons..

Implementing Hall Ribbons with Atoms

1 . 1D Atomic «Wires» using a 2D optical lattice

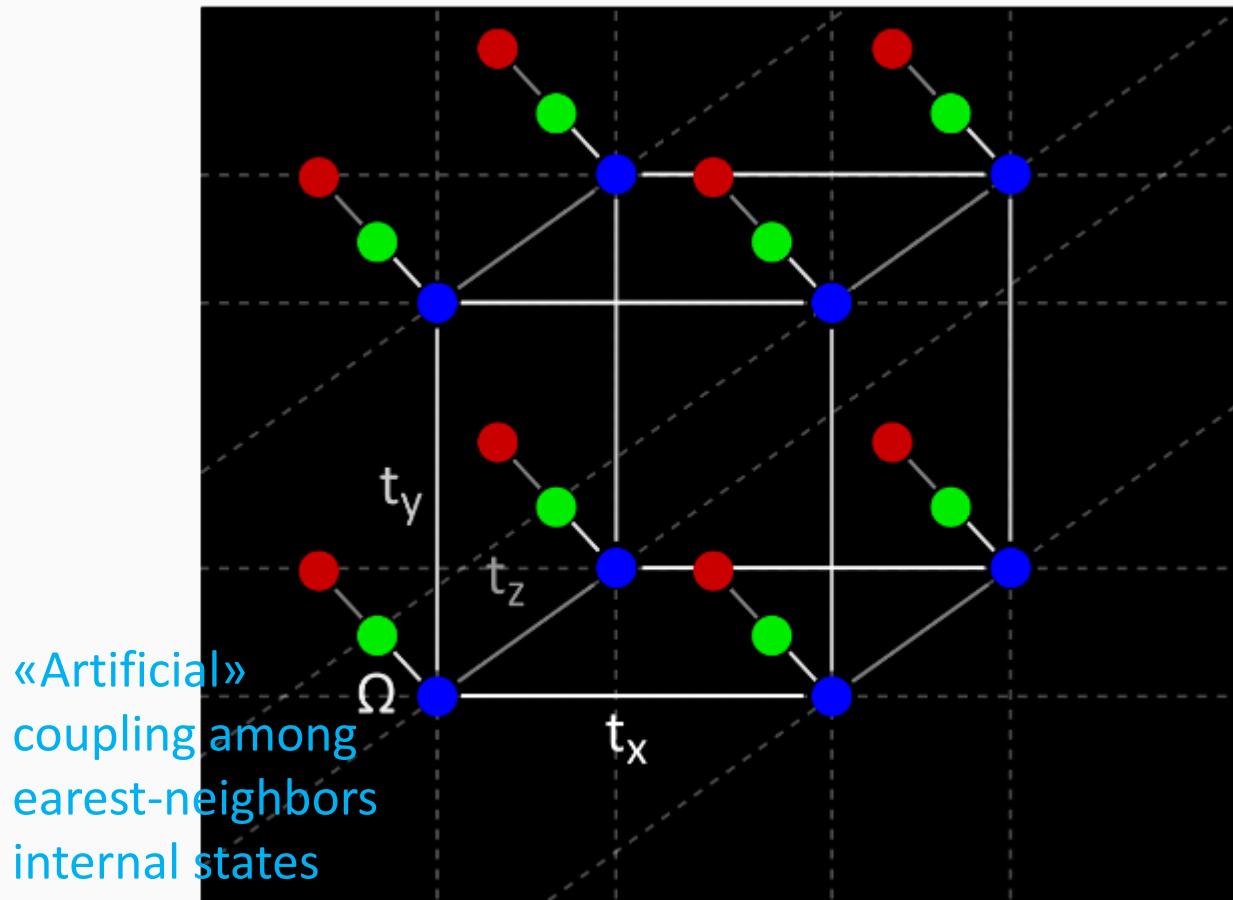


2 . Exploit the «Spin content»

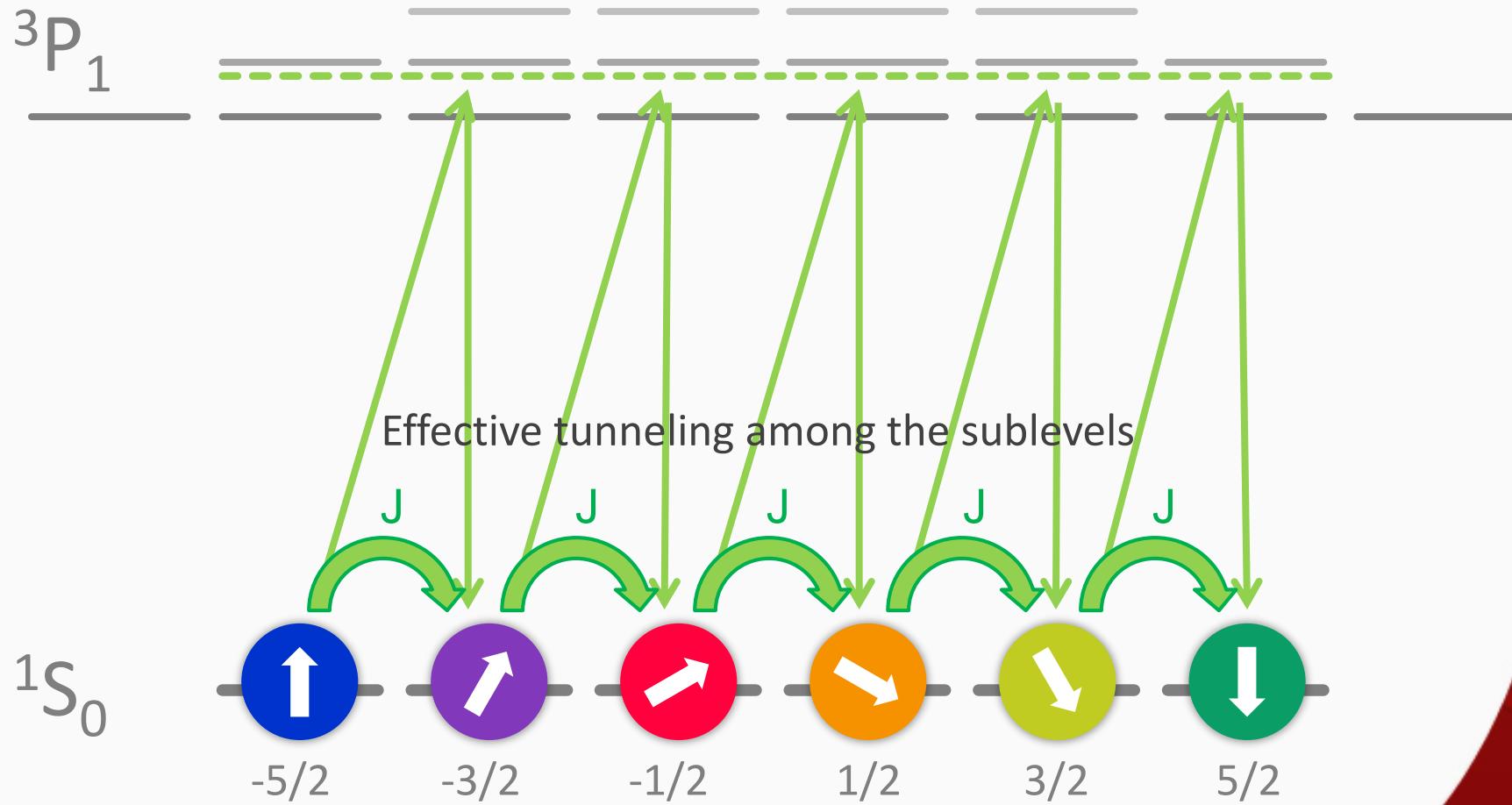
A “synthetic” extra-dimension

Use internal DOF in order to «simulate»
EXTRA DIMENSIONAL lattice sites

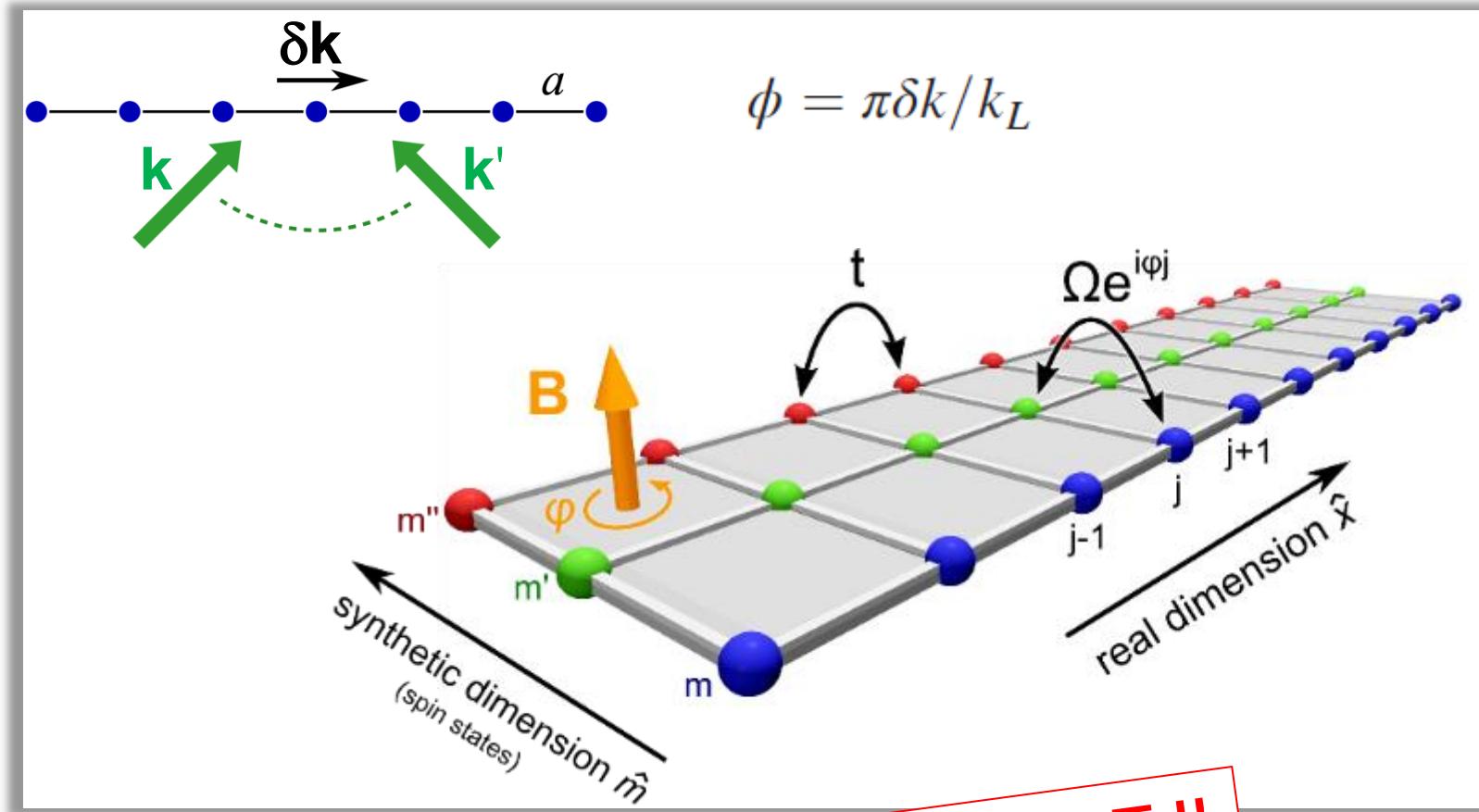
Boada et al., PRL 108, 133001 (2012)



3. Raman Coupling between Spins



Implementing Hall Ribbons with Atoms



**«Hybrid»
Synthetic Fields up to 10000 T !!**

realized: M. Mancini et al., Science **349**, 6255 (2015)

proposed: A. Celi et al., PRL **112**, 043001 (2014)

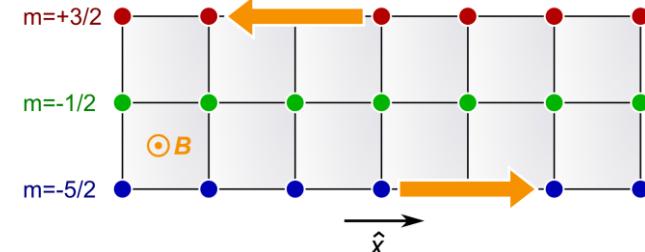
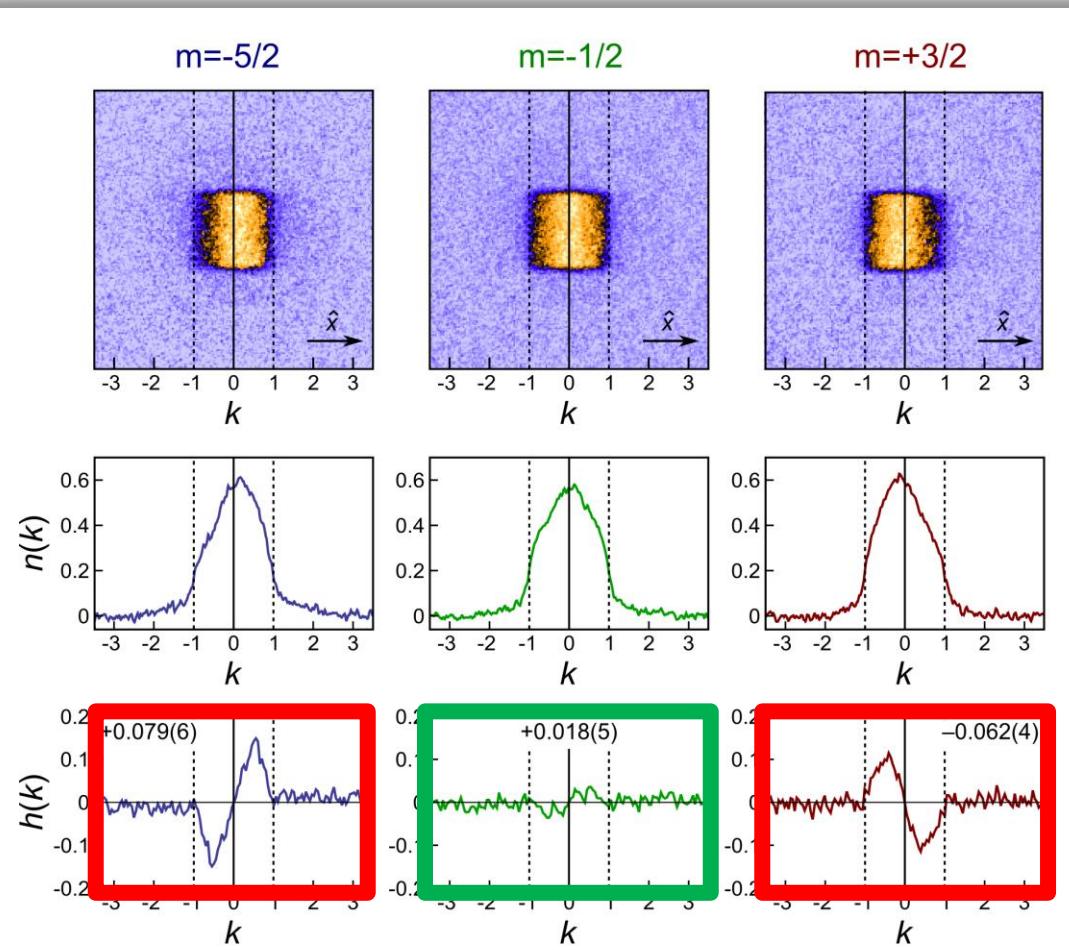
Observation of Edge Currents



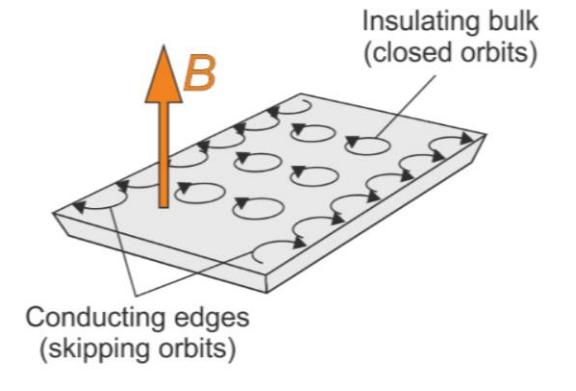
Observation of Edge Currents

Adiabatic loading of a 3-leg ladder (*edges + bulk*)

Lattice momentum distribution:



Conducting edges
no bulk current



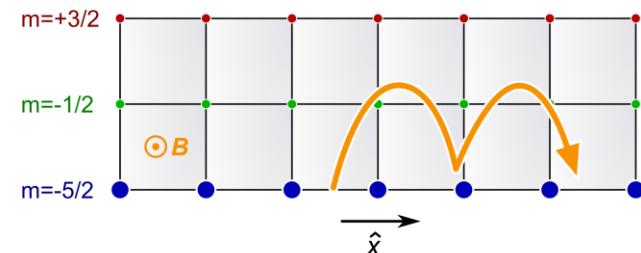
Observation of Skipping Orbits



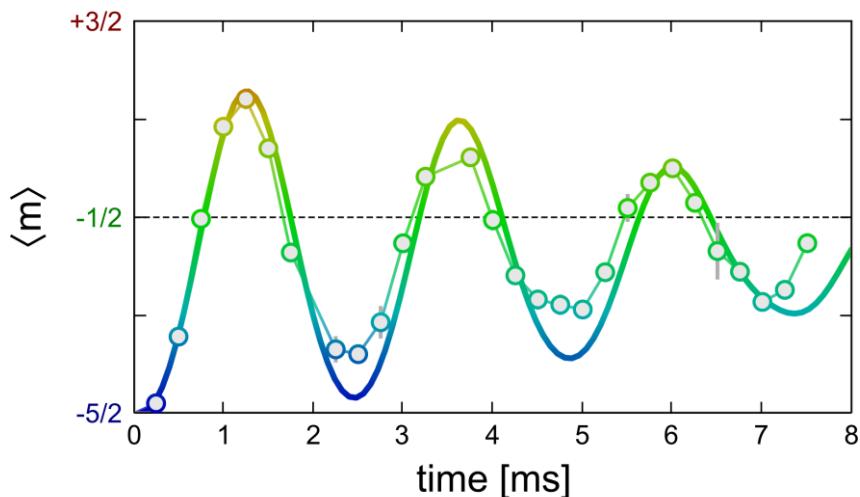
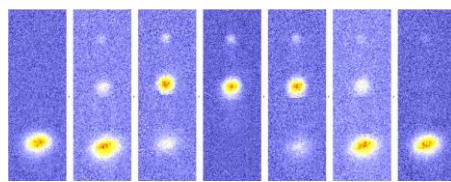
Observation of Skipping Orbits

Initial state prepared on a **single edge**

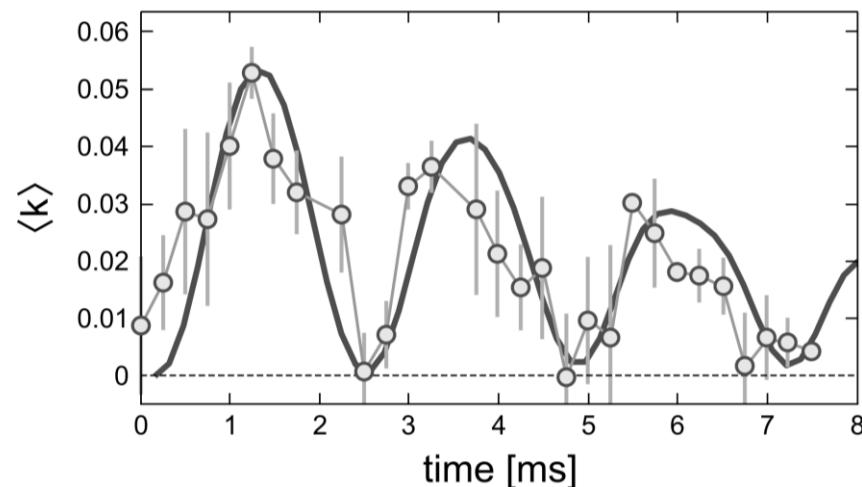
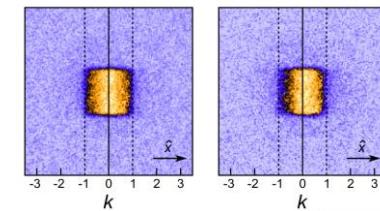
Observe dynamics after **sudden activation**
of synthetic tunneling



Magnetization:

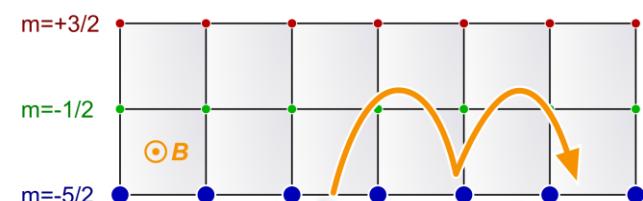
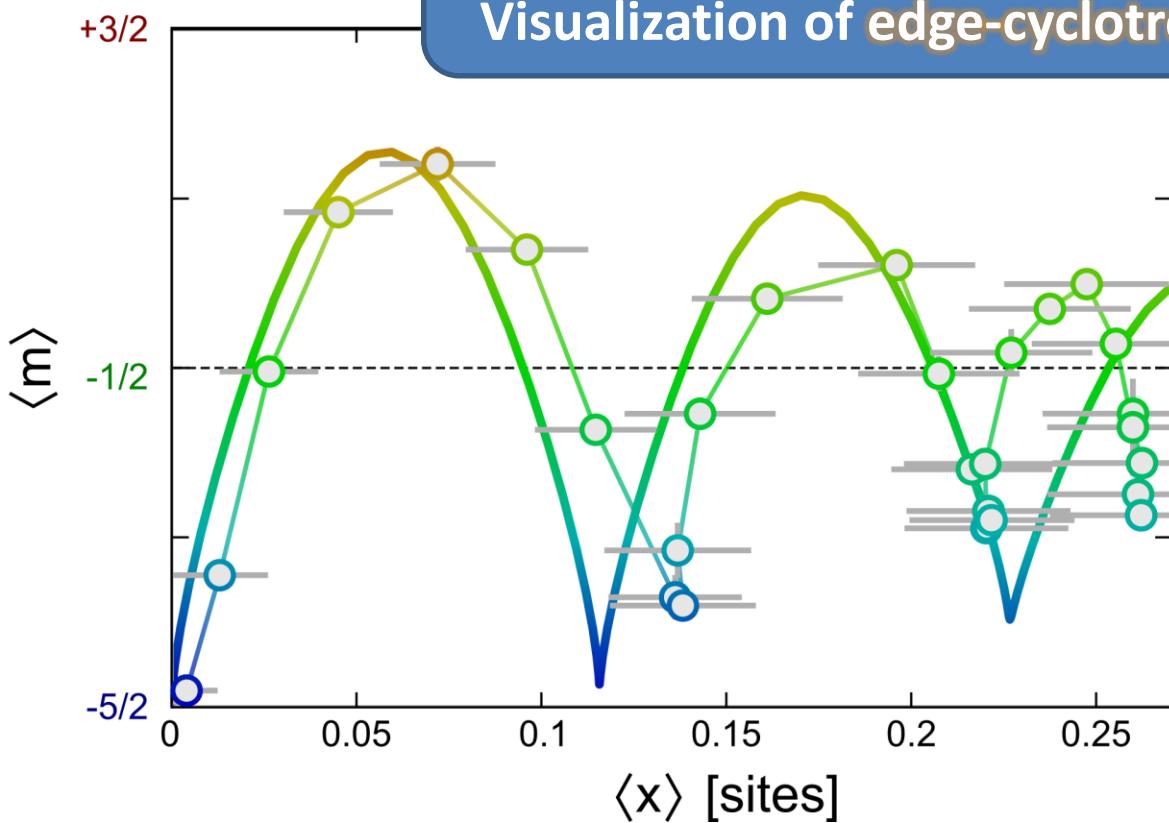


Momentum:



Observation of Skipping Orbits

By knowing the (single-)band dispersion the **real space orbits** $m(\langle x(t) \rangle)$ are reconstructed



Quantum-Hall-like dynamics!

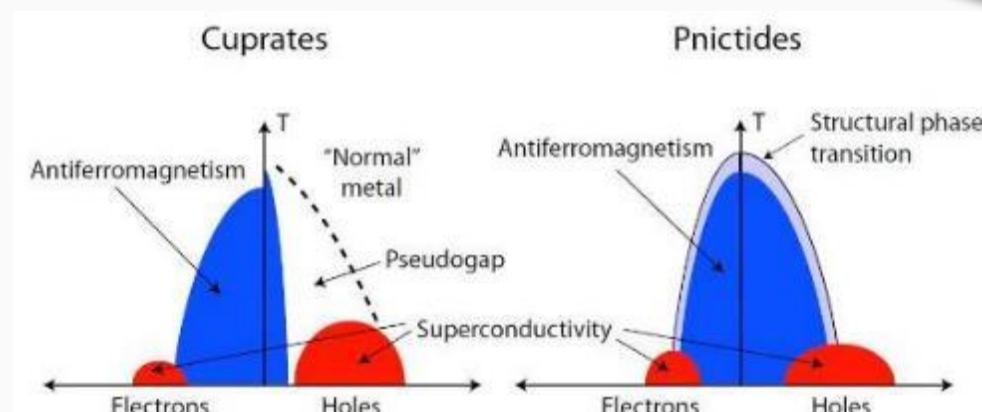
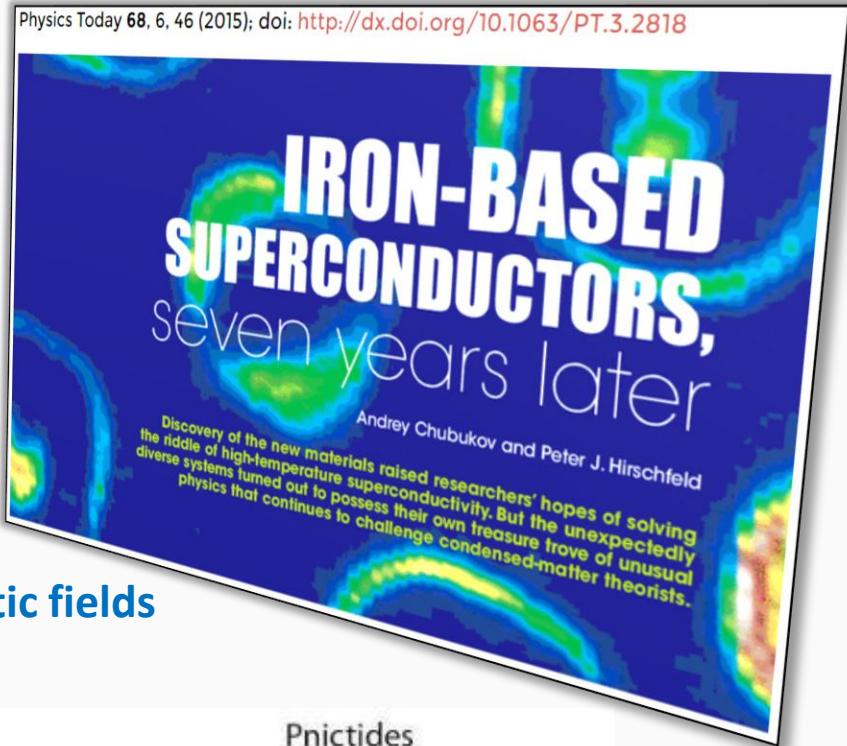
see related work at (NIST):
 B. K. Stuhl et al.,
 Science 349, 6255 (2015)

Perspectives (one out of many..)

Multi-orbital (iron-based)
High-T_c superconductors with interactions



Simulation via
Multi-component (nuclear and/or orbital)
Atomic Mott-Insulators in artificial magnetic fields



from <http://research.physics.berkeley.edu/lanzara/research/pnictide.html>



FISH

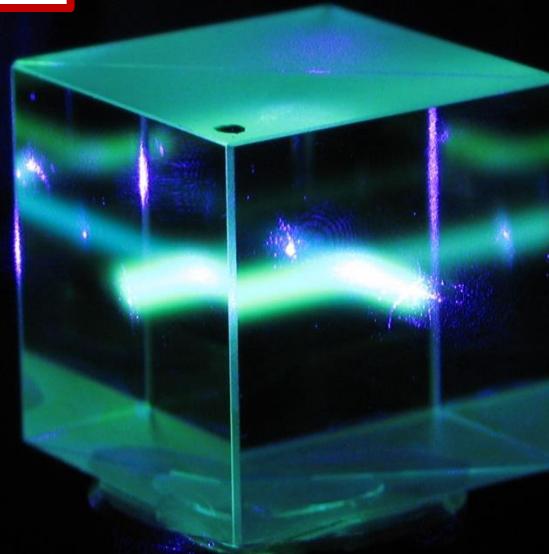


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PostDoc positions 😊

Thanks for your Attention !



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 European Laboratory for
Non-Linear Spectroscopy

