



Mathematics achievement at the end of upper secondary school during COVID-19 pandemic: insights from the INVALSI national assessment

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INVALSI





OUTLINE

- 1. "Measuring" mathematics achievement at the end of secondary upper school: the INVALSI computer based assessment
- 2. A cohort analysis on INVALSI data: longitudinal predictors of mathematics achievement in the COVID-19 era.





conceptually defined by the INVALSI Theoretical Framework (INVALSI, 2018), in line with the National Guidelines, as well as with the main results of research findings in mathematics education, and is characterized by

Latent variable (construct)

- "vertical" continuity (across school grades)
- "transversal" continuity (common knowledge and competences across school tracks)

 operationalized through a Rasch-model-based item bank, administered through computer-based test.





The INVALSI item bank for Grade 13

Content Domain:

- Numbers
- Space and Figures
- Data and Forecasts
- Relationships and Functions

Cognitive process:

- Knowing
- Problem Solving
- Arguing

"vertical" continuity

"transversal" continuity

INVALSI The INVALSI item bank for Grade 13

- maintenance (M) items are about fundamental content knowledge and competences, in continuity with the goals of the lower secondary school and the first two years of the upper secondary school. For all school tracks.
- Recontextualization items (R): the mathematical situations are similar to those of grade 8 or 10 (for reference objects, contexts, etc.), but require the acquisition of new tools and new mathematical contents learned during the subsequent school years. For all school tracks;
- Items for Technical Institute (T) and/or Scientific Lyceum (S) (e.g. mathematical analysis).

"vertical" continuity

"transversal" continuity







An Item Bank is a large collection of test items systematically classified and stored with their associated information (metadata).

In a Rasch item bank, items are placed onto a common underlying linear scale, so that different subsets of these items produce interchangeable measures (Wolfe, 2000). Rasch item bank









The mathematics proficiency scale – G13

Students' locations along the latent variable continuum are described by:

- ✓ numerical scores, which quantifies «how much» of the measured latent variable is present.
- ✓ 5 levels describing the skills and proficiencies of students who attained scores that are within that particular segment of the scale. A described proficiency level "puts into words what the numerical score means" (Turner, 2014)







The mathematics proficiency scale - G13

- ✓ allows to directly compare different cycles of administration (e.g. G13 COVID-COHORT vs G13 pre-COVID-COHORT), taking into account the linking error;
- ✓ Is not (yet) on the same metric of the INVALSI-mathematics scales of grades 8 and 10.
- ✓ does not (yet) allow to measure students' progresses across grades by comparing students locations on one common scale.



Item-person map





Subject	Grade	Overall Gap ₂₀₂₁₋₂₀₁₉ (Unit:SD)
Italian language (Reading)	2	0.12*
Mathematics	2	-0.06
Italian language (Reading)	5	0.12*
Mathematics	5	-0.06
English (Listening)	5	0.01
English (Reading)	5	0.03
Italian language (Reading)	8	-0.07 *
Mathematics	8	-0.18*
English (Listening)	8	0.00
English (Reading)	8	0.00
Italian language (Reading)	13	-0.24*
Mathematics	13	-0.23*
English (Listening)	13	0.05
English (Reading)	13	0.06

* p<.05 taking into account the Linking Error

Source: authors' elaboration with the INVALSI data



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Source: INVALSI (2021) https://public.tabl eau.com/app/profi le/invalsi/viz/RAP PORTO2020-2021_1626172845 0410/INIZIO

Lowest proficiency level Highest proficiency level

G13-mathematics proficiency scale*

* a proficiency scale describes the extent to which the learner possesses the skills, knowledge and understanding that comprise the area (Turner, 2014)





AIM

Exploring **individual and contextual predictors** of students' **mathematics achievement during the COVID-19 pandemic** (Grade 13, s.y. 2020-2021), taking into account their prepandemic learning levels (Grade 10, s.y. 2017-2018).

Predictors at individual and higher levels will be considered, such as **students' sociodemographic characteristics, learning environments characteristics, and an estimate of the duration of school closures** in the s.y. 2020-2021.

The predictive role of students' **educational aspirations** and **interest in mathematics** are also considered in the study. We hypothesized that these constructs are consistent predictors of academic resilience across the challenging COVID-19 Pandemic period.





Our contribution:

- explore the joint distribution of students' mathematics levels on the G10 maths proficiency scale and the G13 maths proficiency scale [1];
- investigate predictors of students relative progresses in mathematics during pandemic through a multilevel approach [2].

	s.y. 2017-2018 (T1)	s.y. 2018-2019	s.y. 2019-2020	s.y. 2020-2021 (T2)
Cohort	Grade 10	Grade 11	Grade 12	Grade 13

> Data:

[1] INVALSI population data (G10+G13+questionnaire): Cases N=406,494 (missing=17.8%)

[2] A random sample of schools (n=718) from the INVALSI database (classes = 2,988; students = 41,388)





Conditional distribution (%) of G10-proficiency scale within the G13-proficiency levels – Pandemic Cohort







Level 1 - Grade 13

The student can use **basic content knowledge and procedures mainly acquired in lower secondary school and, partly, at the end of the first two years of upper secondary school**. Can answer simple questions using easily identifiable information. Can solve problems concerning familiar contexts that require simple procedures.

Level 2 - Grade 13

The student knows the basic mathematical concepts as outlined in the national guidelines in the first two years of upper secondary school. Can answer questions that require simple processing of available data (e.g., comparing various kinds of graphs). Can solve problems for which it is necessary to extrapolate data from the text and use mathematical knowledge acquired in previous grades (i.e., lower secondary school and the first two years of upper secondary school).



Group	Level Grade 10	Level Grade 13
L-L	Low (1-2)	Low (1-2)
L-IH	Low (1-2)	Intermediate to High (3-5)
IH-L	Intermediate to High (3-5)	Low (1-2)
IH-IH	Intermediate to High (3-5)	Intermediate to High (3-5)





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Outcome:

G13-mathematics ability estimate

Level 1:

- G10-mathematics ability estimate;
- sociodemographic characteristics;
- interest in mathematics;
- educational aspirations (0= at maximum high-school diploma; 1= higher).







Level 2:

- G10-class average mathematics ability estimate;
- class-composition based on sociodemographic characteristics;
- class average interest in mathematics;
- prop. of stud.s aspiring to achieve a higher attainment level than uppersecondary school diploma.







Level 3:

- school tracks;
- G10-school average mathematics ability estimate;
- school-composition based on sociodemographic characteristics;
- school average interest in mathematics;
- prop. of stud.s aspiring to achieve a higher attainment level than uppersecondary school diploma.







Level 4: Italian Regions

- ✓ G10-region average mathematics ability estimate;
- ✓ Days of school closure in the school year 2020-21 (%);
- ✓ Gross Domestic Product (GDP) per capita-2018 (source: Italian National Istitute of Statistics, ISTAT);
- ✓ % of NEET (young people neither in employment nor in education and training, source: ISTAT).







School closures caused by COVID-19 in Italy





Source: UNESCO map on school closures (https://en.unesco.org/covid.19/educatio nnresponse) and UIS. March 2022 (https://data.uis.unesco.org) **Source**: authors' elaboration with the data of the Bank of Italy Note (Bovini & De Philippis, 2021) based on the Decree DPCMs and regional ordinances.





How G13 mathematics ability estimate during pandemic varies between students (within class), between classes (within school), between schools (within Region) and between Regions?

Results: Random intercept model

Variance Partition Index45%
45%
10%
10%35%
35%
endRegionSchoolClassStudent

The 11% of the variation in mathematics scores lies between Regions; 35% lies within Region between schools; 10% lies between classes within school and 45% between students.

LR test (4-level model vs 3-level model (χ^2_1 = 163.897. p < 0.01)).





How G13 mathematics ability estimate varies between classes (within school), between schools (within Regions), and between Regions during pandemic?



The range of values of the Region residuals (departure from the grand mean: 189.66) is from a reduction in mathematics ability estimate of 23 points to an increase of 19 points.







How mathematics ability estimate varies during Pandemic once the pre-pandemic baseline level (Mathematics-G10) is accounted for?

Results: Random intercept+fixed effect of MATH10 (GMC)







Adjusting for MATH10 explains 55% of variability in MATH13 score.

Large decline in the Region- (66%) and School- (61%) level. Large differences between students' mathematics level at the baseline (class-level reduction is 27%; student-level reduction is 21%)

		Fixed Part	Estimate	SF	Contextual effect
		Intercent	198.026	3.256	contextual encer
	Student baselin	e Maths 10	0.532	0.004 **	
INVALSI		Female	-2.674	0.256 **	
		First Generation Immigrant	-4,44	0,645 **	
	Student level	Second Generation Immigrant	-2,561	0,481 **	
		ESCS	0,174	0,126	
Direct within and		Interest in mathematics	3,11	0,129 **	
batwa en effe ete		Educational aspiration	2,401	0,295 **	
between effects		Average Math-10	0,667	0,019 **	0.136 **
		Prop. Female	-4,725	1,156 **	-2.051
Centering: CWC(M)		Prop. FGIMM	3,305	3,874	7.745 *
(Brincks et al. 2017;	Class level	Prop. SGIMM	-2,204	3,079	0.358
Yaremych, Preacher &		Average ESCS	0,644	0,796	0.47
Hedeker, 2021)		Average interest in mathematics	4,152	0,693 **	1.042
		Prop. educational aspiration	1,729	1,693	-0.671
		Average Math-10	0,713	0,028 **	0.046
		Scientific lyceum (vs Other Lycei)	4,891	1,721 **	
		Technical Institute	0,298	1,799	
	School level	Vocational Institute	-7,278	2,298 **	
		Prop. Female	-8,482	2,277 **	-3.757
		Prop. FGIMM	-9,131	9,198	-12.436
		Prop. SGIMM	-7,777	6,808	-5.573
Adjusting for 11		Average ESCS	-2,131	1,357	-2.775
L4 covariates		Average interest in mathematics	2,644	1,602	-1.508
		Prop. educational aspiration	4,083	3,635	2.354
explains 62% of	Region level	Math10_GMC	0,537	0,091 **	-0,176
		days of school_closure (%): LOW	-2,509	1,6	
variability in		days of school_closure (%): HIGH	-5,361	1,709 **	
MATH13 score.		NEET_C_ITALY	-0,658	0,18 **	
		GDP_C_ITALY	0,061	0,183	





Conclusions

- The overall differences between pre-pandemic and pandemic cohorts in Italy suggest a pandemic achievement gap in mathematics at the end of upper secondary school (INVALSI,2022; Bazoli, Marzadro, Schizzerotto & Vergolini., 2022);
- Considering low-performers starting points (G10) in a longitudinal perspective, it emerges that although most of G13 low performers were already struggling with mathematics, about one out three moved from intermediate-high (G10 scale) to lowest levels (G13 scale).
- More encouraging results are those from another subgroup of pandemic-cohort students who maintained intermediate to high performance in mathematics (with respect to G10 and G13 scales), suggesting positive patterns of adaptation in the context of adversity due to the COVID-19 crisis.
- Future perspective: vertical scaling for monitoring progresses across upper secondary school by using a common vertical scale.





Conclusions

- Multilevel approach allows to depict an overview of the relevance of different variables in supporting students' relative progresses in mathematics during pandemic:
 - socioeconomic and cultural background seems to play a minor role in predicting students' progresses from G10 to G13. However, students ESCS might play an indirect effect through other covariates and over the previous grades;
 - ✓ within classes, being a student with an immigrant background and being a female is associated with relative smaller progresses in mathematics from G10 to G13 during pandemic; contextual effects also emerged for class-average baseline level;
 - interest in mathematics and educational goals students set for themselves act a key role in predicting students' relative progresses in mathematics (protective factors) in the context of adversity due to the COVID-19 crisis and might be eligible target variables for intervention programs.
 - Regions showing a higher disengagement of young people from the process of entering adult life, the labour market, and the possibility of accessing it through education or training (Bynner and Parsons, 2002) are more likely to report lower progresses in mathematics during pandemic, even when the Regions' school closure duration is accounted for.





Thank you for your attention

"The ability to adapt well in the face of hard times is a valuable skill for young adults. The good news is that resilience is something that can be learned" (APA, 2020).