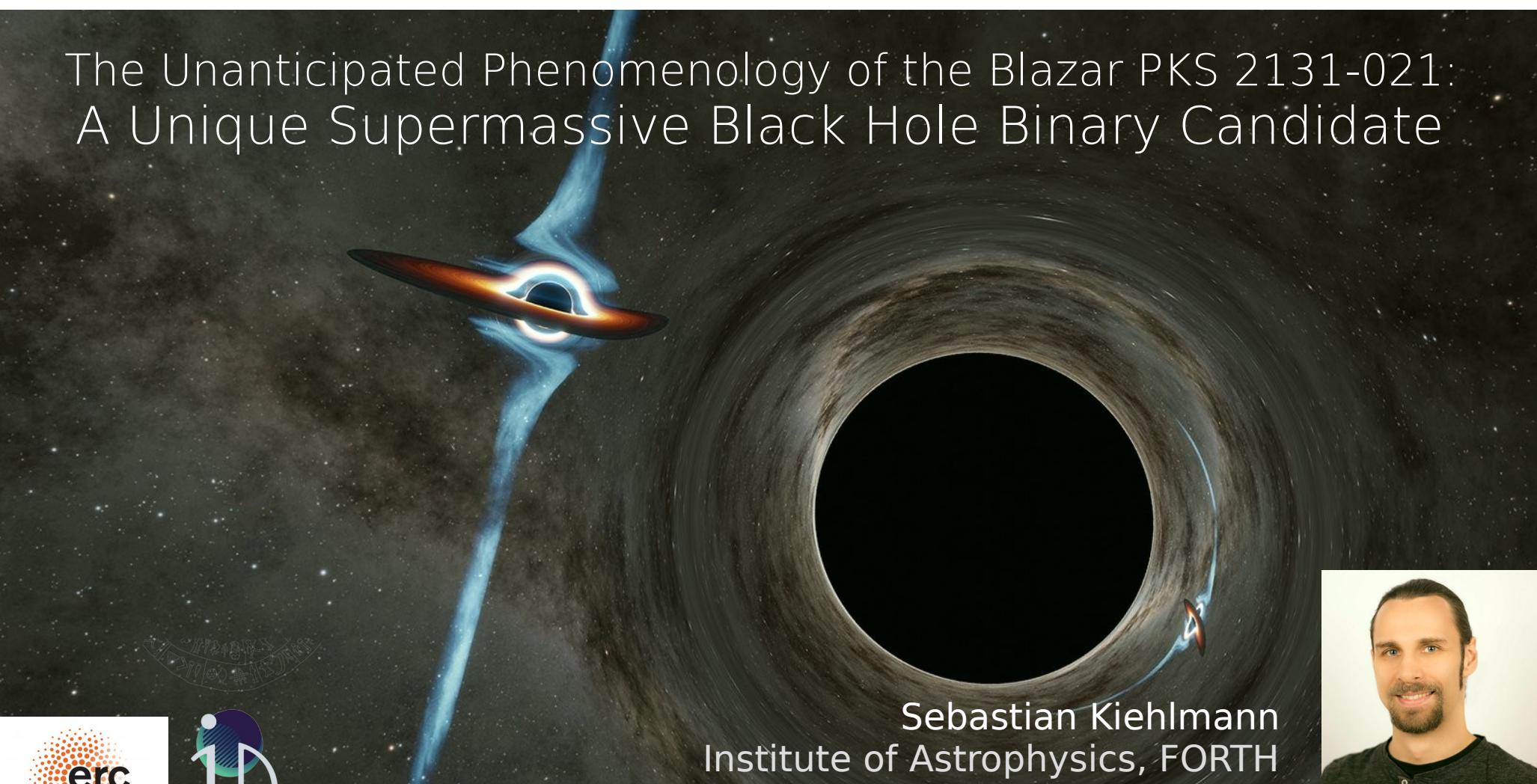


# The Unanticipated Phenomenology of the Blazar PKS 2131-021: A Unique Supermassive Black Hole Binary Candidate



Sebastian Kiehlmann  
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European Research Council  
Established by the European Commission



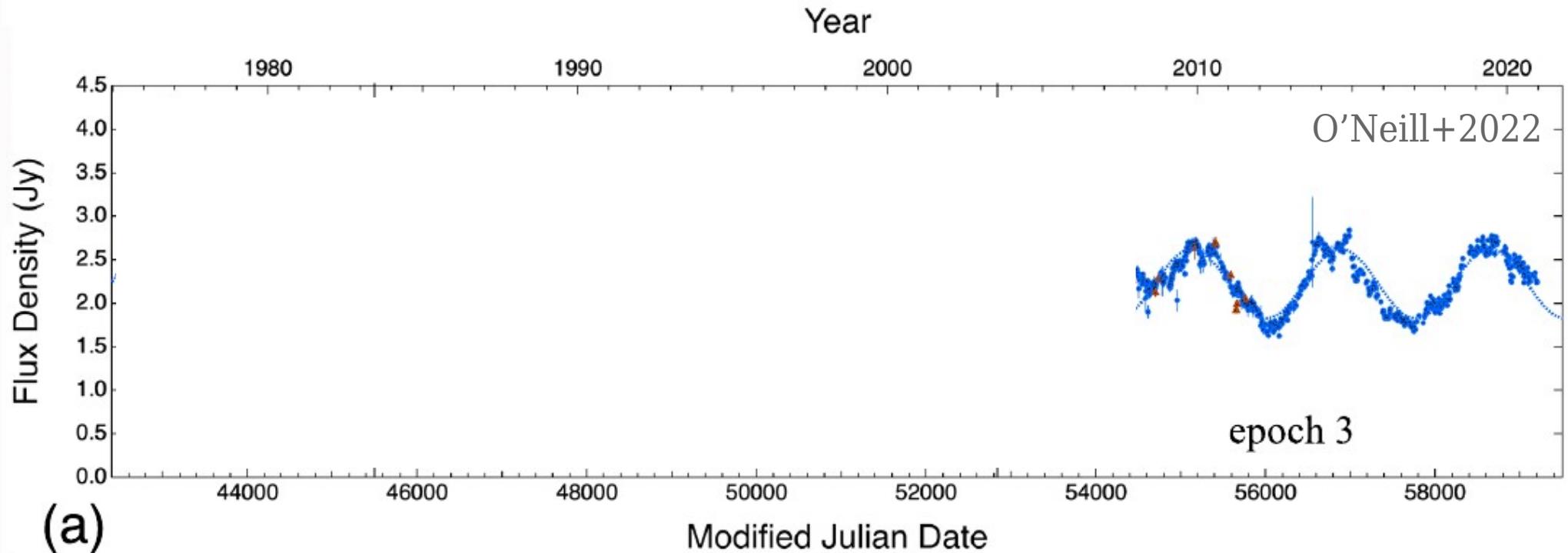
# Synopsis

- 45 years radio light curve of PKS 2131-021
  - two epochs of strong sinusoidal variation with the same period and phase
    - unlikely due to random fluctuations at  $4.6\sigma$  significance level
    - suggests a Super Massive Black Hole Binary (SMBHB)

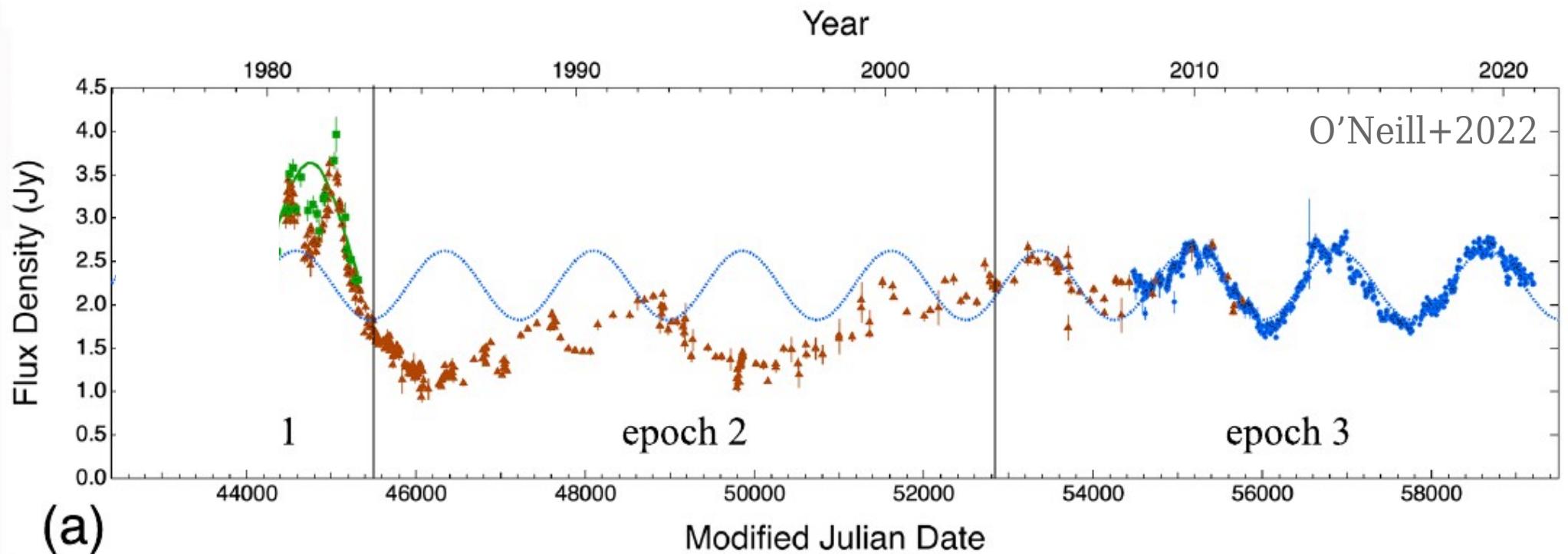


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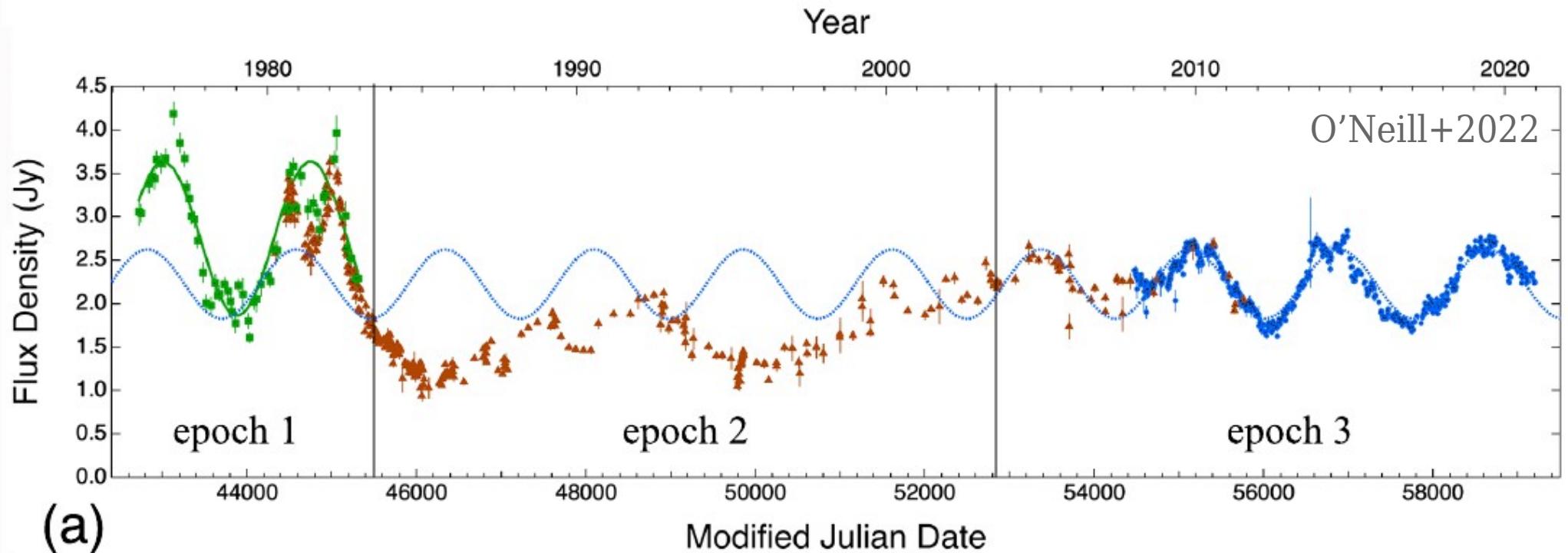
45 years radio light curve: two epochs of periodic signal



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# Sinusoid fits: two epochs with matching period and phase

**Table 1**  
Sine-fitting Results for Epoch 1, Epoch 2, Epoch 3, and the Joint Epoch 1 + Epoch 3 Data Sets

	epoch 1	epoch 2	epoch 3	epoch 1 + epoch 3
$P$ (days)	$1729.1 \pm 32.4$	$3779.1 \pm 46.0$	$1760.4 \pm 5.3$	$1737.9 \pm 2.6$
$\phi_0$	$0.89 \pm 0.46$	$0.35 \pm 0.08$	$0.60 \pm 0.07$	$0.88 \pm 0.03$
$A$ (epoch 1)	$0.709 \pm 0.047$	...	...	$0.679 \pm 0.045$
$S_0$ (epoch 1)	$2.553 \pm 0.036$	...	...	$2.584 \pm 0.034$
$\sigma_0$ (epoch 1)	$0.333 \pm 0.022$	...	...	$0.337 \pm 0.023$
$A$ (epoch 2)	...	$0.392 \pm 0.020$	...	...
$S_0$ (epoch 2)	...	$1.724 \pm 0.021$	...	...
$\sigma_0$ (epoch 2)	...	$0.140 \pm 0.009$	...	...
$A$ (epoch 3)	...	...	$0.400 \pm 0.007$	$0.400 \pm 0.007$
$S_0$ (epoch 3)	...	...	$2.225 \pm 0.005$	$2.229 \pm 0.005$
$\sigma_0$ (epoch 3)	...	...	$0.118 \pm 0.004$	$0.120 \pm 0.004$

**Note.** We also determined the least-squares sine fit to epoch 3 for shifted boundaries between epoch 2 and epoch 3 at MJD 51,200 and MJD 53,800, with the results  $P = 1762.9 \pm 6.1$  days and  $P = 1756.0 \pm 5.5$  days, respectively. These may be compared with the result above of  $P = 1760.4 \pm 5.3$  days for the boundary set at MJD 52,850. The peak periods identified in our WWZ analyses of epochs 1, 2, and 3 were 1740, 3919, and 1779 days, respectively. Those in our GLS analyses were 1730, 3937, and 1788 days, respectively.

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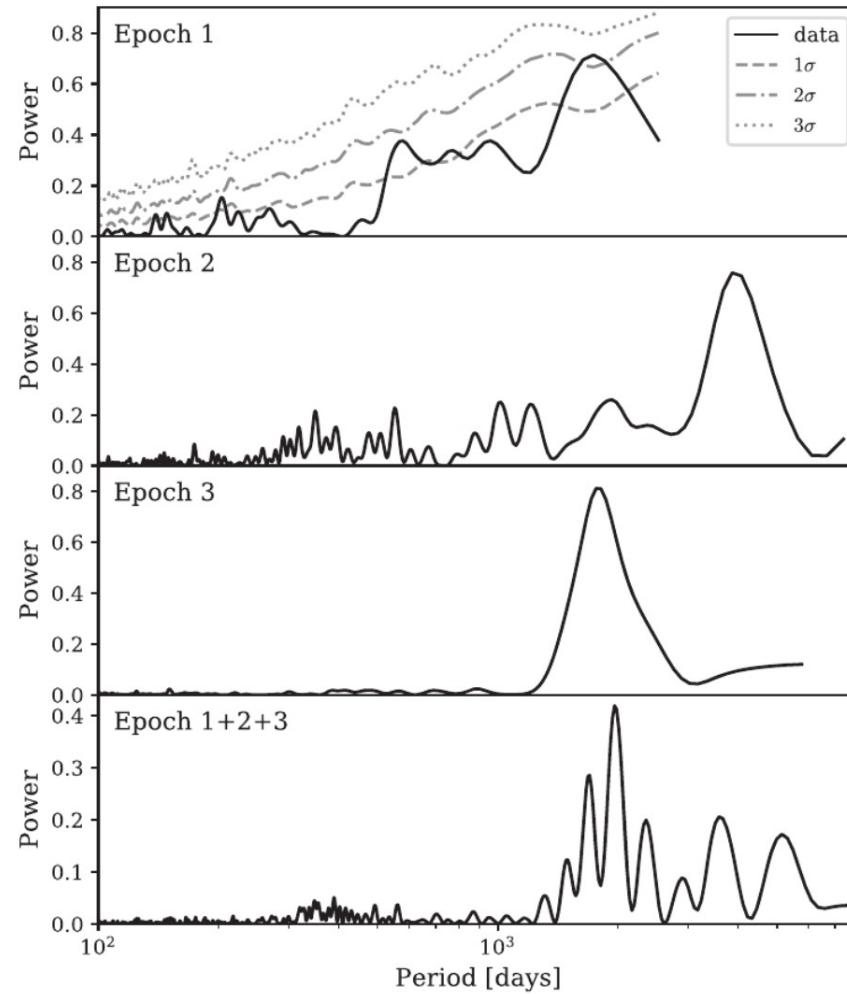
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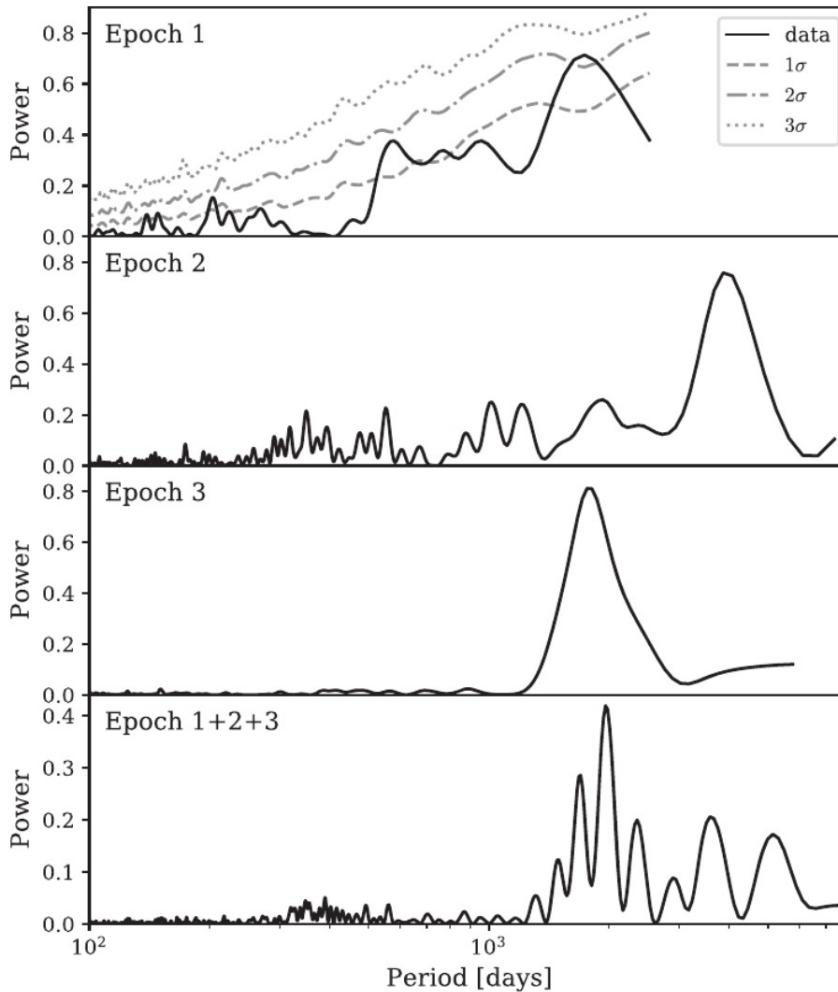
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# Generalized Lomb-Scargle Periodogram



# Generalized Lomb-Scargle Periodogram: significance



**H0:** variability follows  
a red noise process  
(i.e. is purely stochastic)

---

**H1:** variability has  
a periodic component

**Table 3**  
Single-period (Spurious) and All-period (True) Probabilities

Epoch and Test	$N_{\text{tot}}$	$n_{\text{pass}}$	$p\text{-value}$	$\sigma$
epoch 1 single period	10000	108	$1.08 \times 10^{-2}$	2.3
epoch 1 all periods	10000	1446	$1.45 \times 10^{-1}$	1.06 <sup>a</sup>
epoch 2 single period	10000	122	$2.20 \times 10^{-3}$	2.85
epoch 2 all periods	10000	632	$6.32 \times 10^{-2}$	1.53 <sup>a</sup>
epoch 3 single period	100000	0	$<10^{-5}$	>4.26
epoch 3 all periods	100000	40	$4.00 \times 10^{-4}$	3.35 <sup>a</sup>

**Note.** The tests using all periods are the “Look Elsewhere” tests.

<sup>a</sup> These are the true significances; the others are totally spurious unless the periods have been selected “a priori.”

# A highly significant detection

**Table 2**

Probabilities and Significance Levels of GLS Tests Computed from Simulations with Matched Red-noise Tail

Test Number	Test	GLS $\mathcal{P}_{\text{peak}}$ (max = 1)	Period Range ( $\Delta P$ ) (days)	Total Simulations	Number of Simulations That Pass Test	p-value	Significance ( $\sigma$ )
1.1	epoch 1 $\mathcal{P}_{\text{peak}}, p_{\text{sim}} \leq p_{\text{peak}}$	0.71	All	10,000	1446	$1.45 \times 10^{-1}$	1.06
1.2	epoch 2 $\mathcal{P}_{\text{peak}}, p_{\text{sim}} \leq p_{\text{peak}}$	0.76	All	10,000	632	$6.32 \times 10^{-2}$	1.53
1.3	epoch 3 $\mathcal{P}_{\text{peak}}, p_{\text{sim}} \leq p_{\text{peak}}$	0.81	All	100,000	40	$4.0 \times 10^{-4}$	3.35
2	epoch 1 $\mathcal{P}_{\text{lim}}, \Delta P_{\text{epoch 3}}$	$\geq 0.50$	1661.9–1858.9	10,000	197	$1.97 \times 10^{-2}$	2.06
3	1.3+2	...	...	...	...	$7.88 \times 10^{-6}$	4.32
4	3+phase	...	...	...	...	$1.58 \times 10^{-6}$	4.66

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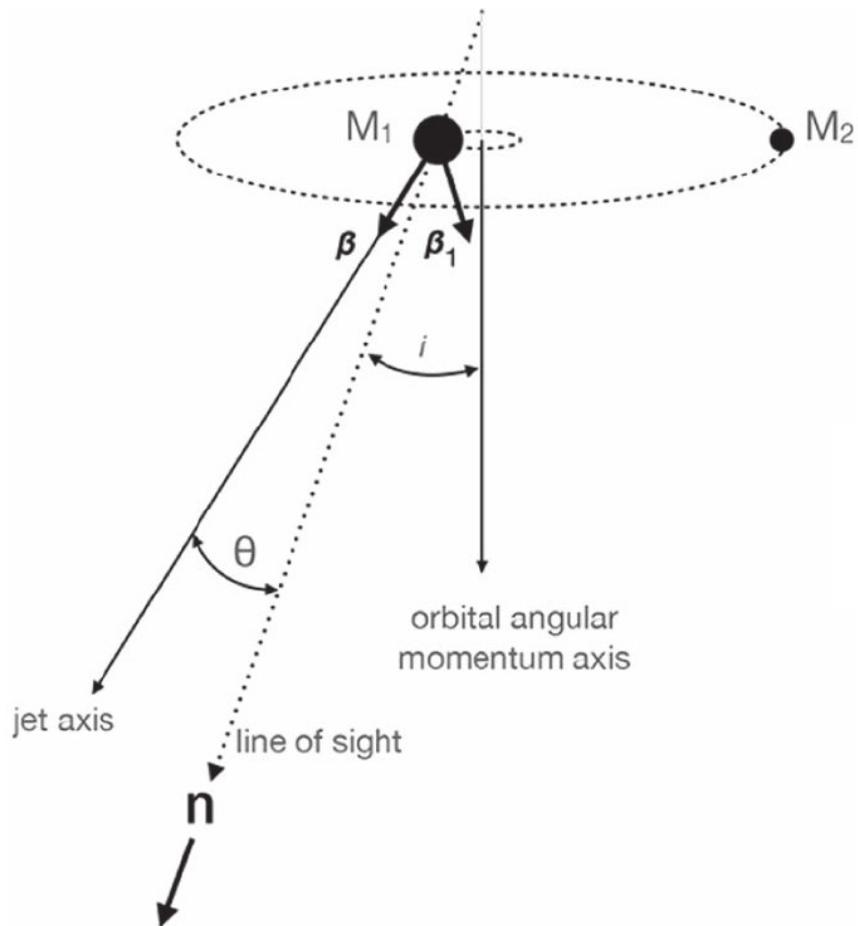
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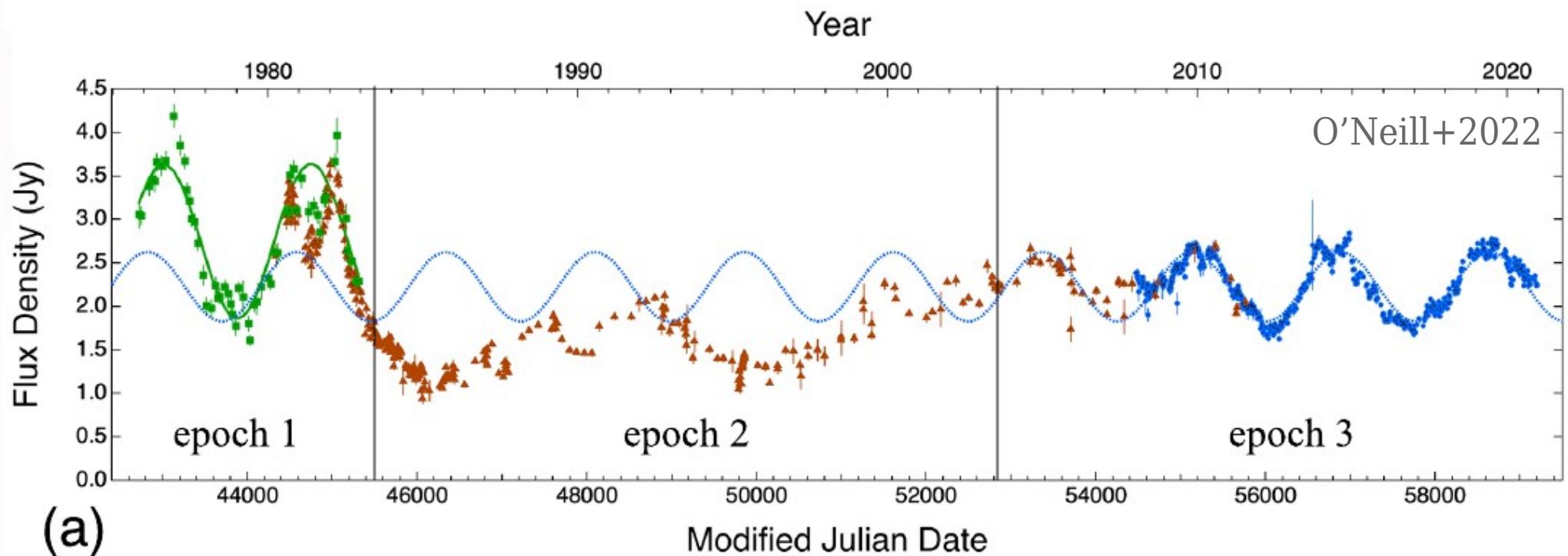
# Model: Doppler boosting in black hole binary system



$$S = D^{2-\alpha} S'$$

$$\delta \ln S = \frac{2(2 - \alpha)\gamma^2\theta\beta_1 \cos i}{(1 + \gamma^2\theta^2)} \cos(2\pi t/P).$$

Why is the periodicity turning on and off?



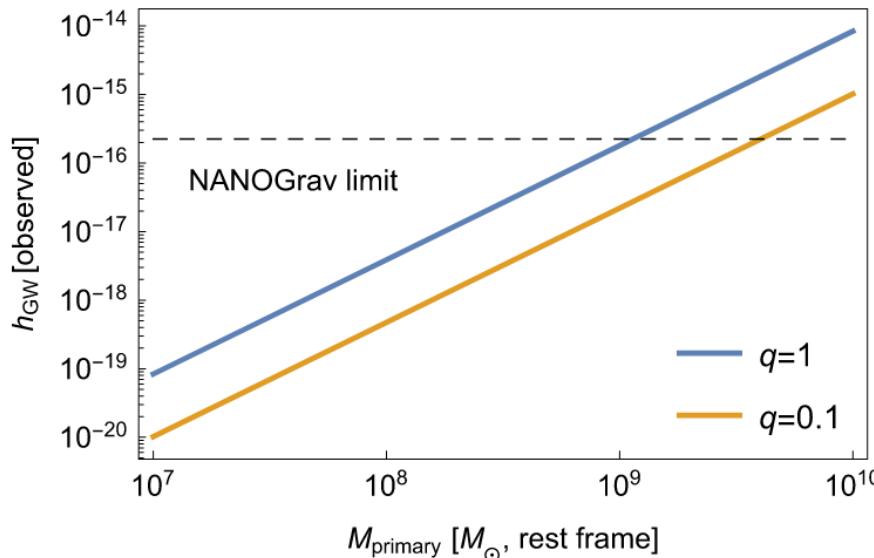
# A unique super-massive black hole binary candidate

## Binary separation and orbital period

$$r \sim 0.001 - 0.1 \text{ pc} \quad \text{for} \quad m \sim 3 \times 10^6 M_{\odot} - 3 \times 10^9 M_{\odot}$$

$$P_{rf} = 2 \text{ yr}$$

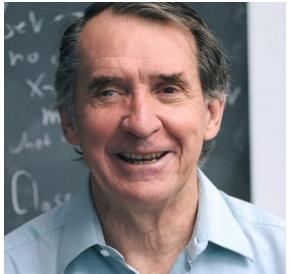
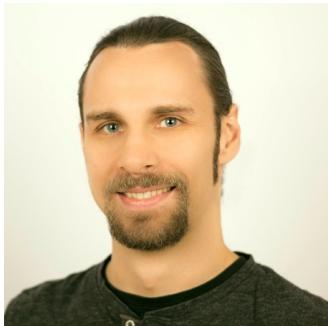
## Implications for gravitational wave emission



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# The Unanticipated Phenomenology of the Blazar PKS 2131–021: A Unique Supermassive Black Hole Binary Candidate

S. O'Neill<sup>1</sup> , S. Kiehlmann<sup>2,3</sup> , A. C. S. Readhead<sup>1,3</sup> , M. F. Aller<sup>4</sup> , R. D. Blandford<sup>5</sup> , I. Liodakis<sup>6</sup> , M. L. Lister<sup>7</sup> , P. Mróz<sup>8</sup> , C. P. O'Dea<sup>9</sup> , T. J. Pearson<sup>1</sup> , V. Ravi<sup>1</sup> , M. Vallisneri<sup>10</sup> , K. A. Cleary<sup>1</sup> , M. J. Graham<sup>11</sup> , K. J. B. Grainge<sup>12</sup> , M. W. Hodges<sup>1</sup> , T. Hovatta<sup>6,13</sup> , A. Lähteenmäki<sup>13,14</sup> , J. W. Lamb<sup>1</sup> , T. J. W. Lazio<sup>10</sup> , W. Max-Moerbeck<sup>15</sup> , V. Pavlidou<sup>2,3</sup> , T. A. Prince<sup>11</sup> , R. A. Reeves<sup>16</sup> , M. Tornikoski<sup>13</sup> , P. Vergara de la Parra<sup>16</sup> , and J. A. Zensus<sup>17</sup> 

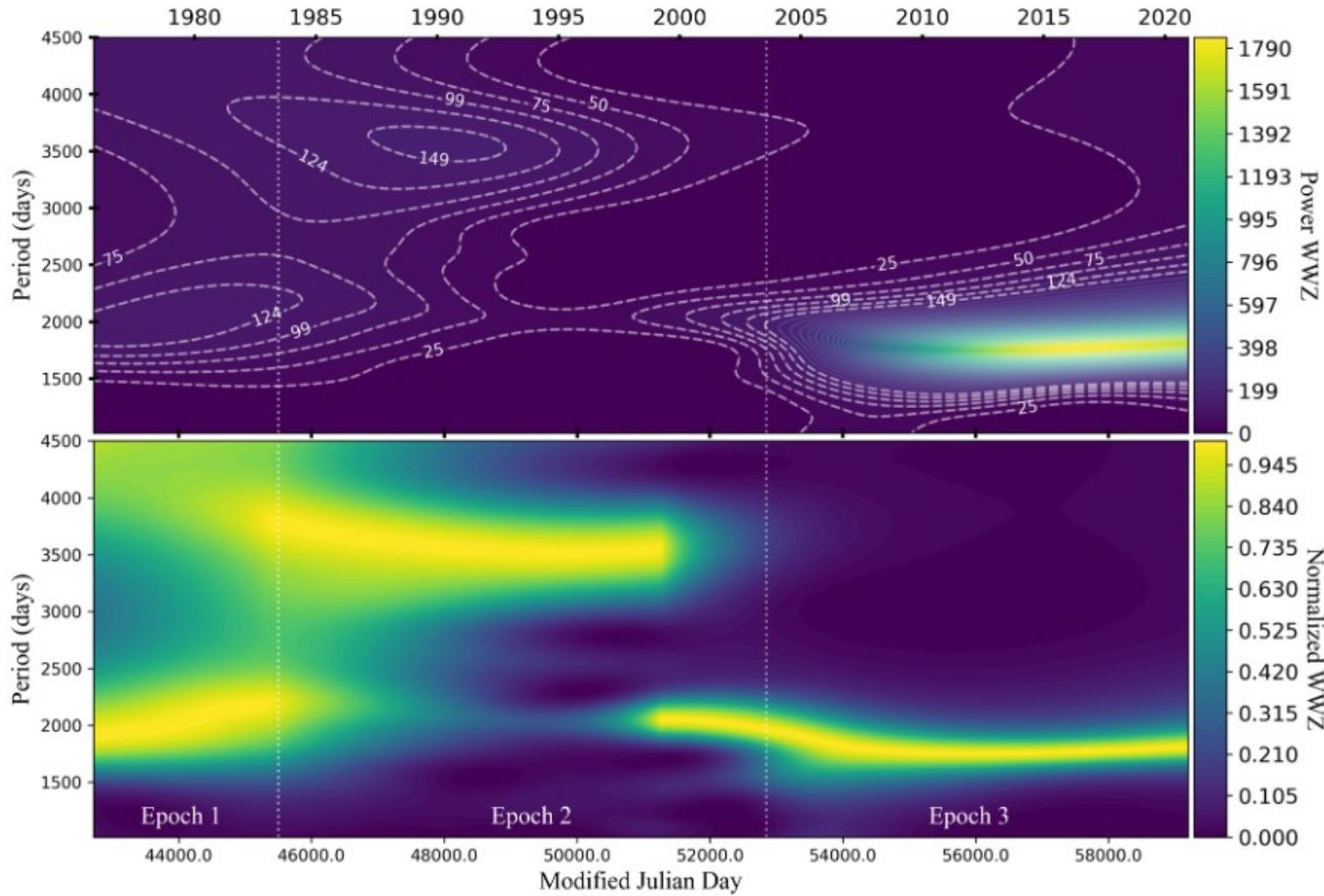


S. O'Neill

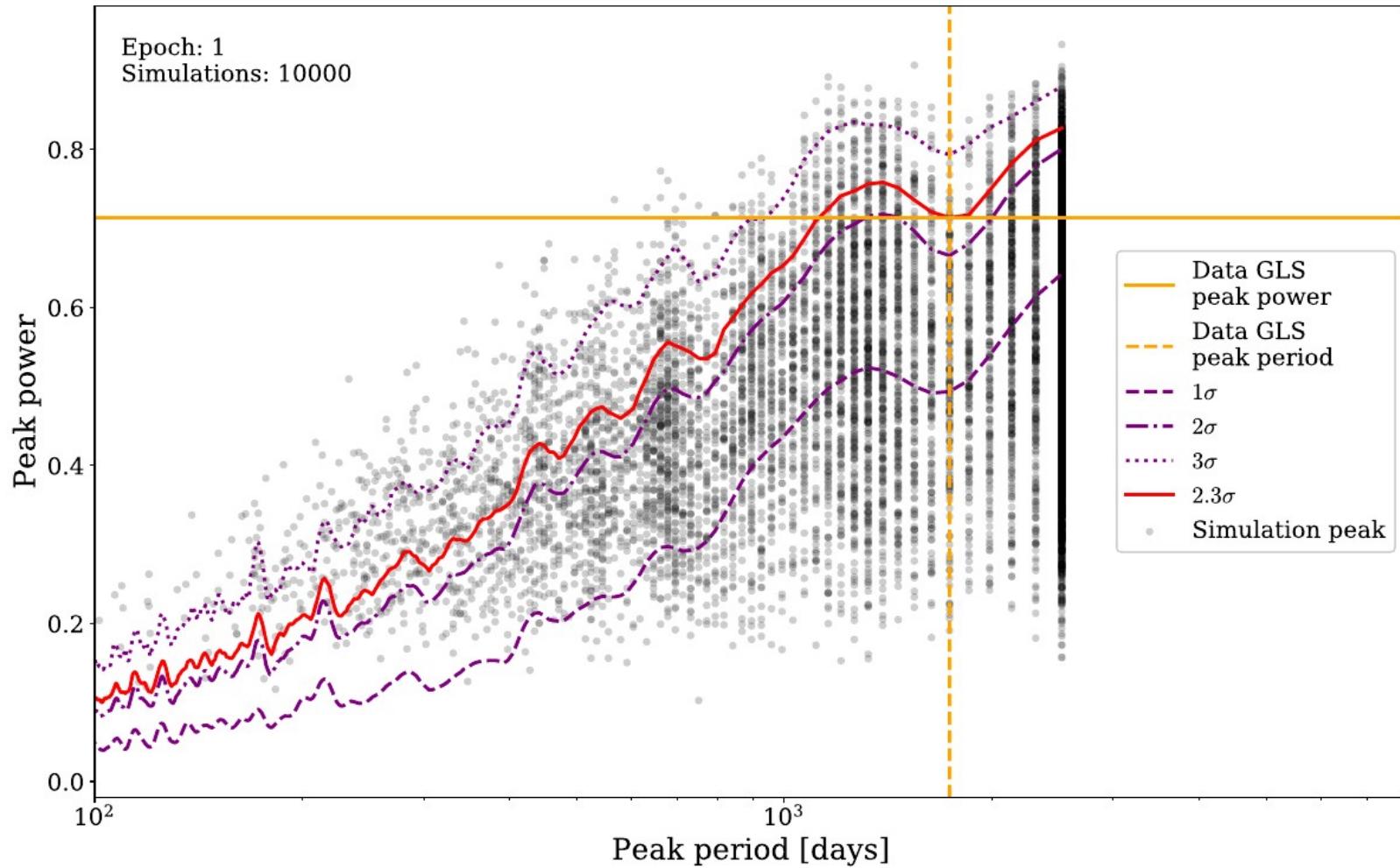
S. Kiehlmann A.C.S. Readhead

Additional slides

WWZ transform: two epochs with matching period



# Generalized Lomb-Scargle Periodogram: look-elsewhere



# Super Massive Black Hole Binary candidates

Source	Separation	Mass	Orbital period	References
B3 0402+379	7.3 pc (projected)	$1.5 \times 10^{10} M_{\odot}$	$3 \times 10^4$ yr	Rodriguez+ 2006, Bansal+ 2017
OJ 287	$\sim 0.1$ pc	$1.8 \times 10^{10} M_{\odot}$ $1.5 \times 10^8 M_{\odot}$	9 yr	Sillanpaa+ 1988, Valtonen+ 2016, Dey+ 2021