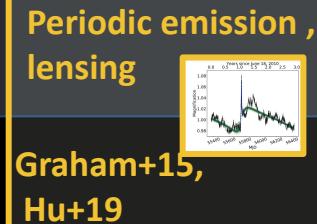
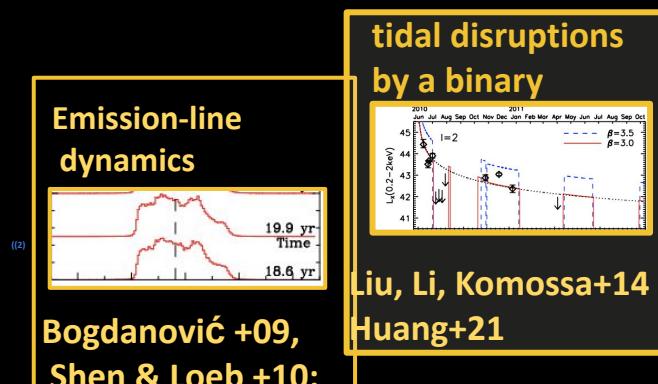


On the complementarity of time domain techniques for detecting close binary supermassive black hole candidates

A. Kovačević (1), Jian-Min Wang (2)

(1) University of Belgrade-Faculty of Mathematics

(2) Key Laboratory for Particle Astrophysics,
Institute of High Energy Physics, CAS



Graham+15,
Hu+19

Time domain surveys

| M | R.A. | Dec. | z | V-band | Period | $\log \left(P_{\text{orb}} \right)$ | τ | Am | Area |
|----------------------------------|------------|-------------|-------|--------|--------|--------------------------------------|--------|-------------------|------|
| UM 101 | 00:12:38.0 | +00:01:06.0 | 1.066 | 17.0 | 1868 | 8.197 | 0.013 | 1.2×10^6 | 3.0 |
| UM 254 | 00:23:03.2 | +00:15:53.0 | 0.759 | 17.25 | 1518 | 8.197 | 0.040 | 2.8×10^6 | 2.4 |
| UM 101 (00:12:38.01 - 114100.00) | 00:12:38.0 | +00:01:06.0 | 1.054 | 17.0 | 1600 | 8.197 | 0.013 | 1.2×10^6 | 3.0 |

Graham
+15,Liu+19

~>200
Binary SMBH
candidates

timeline

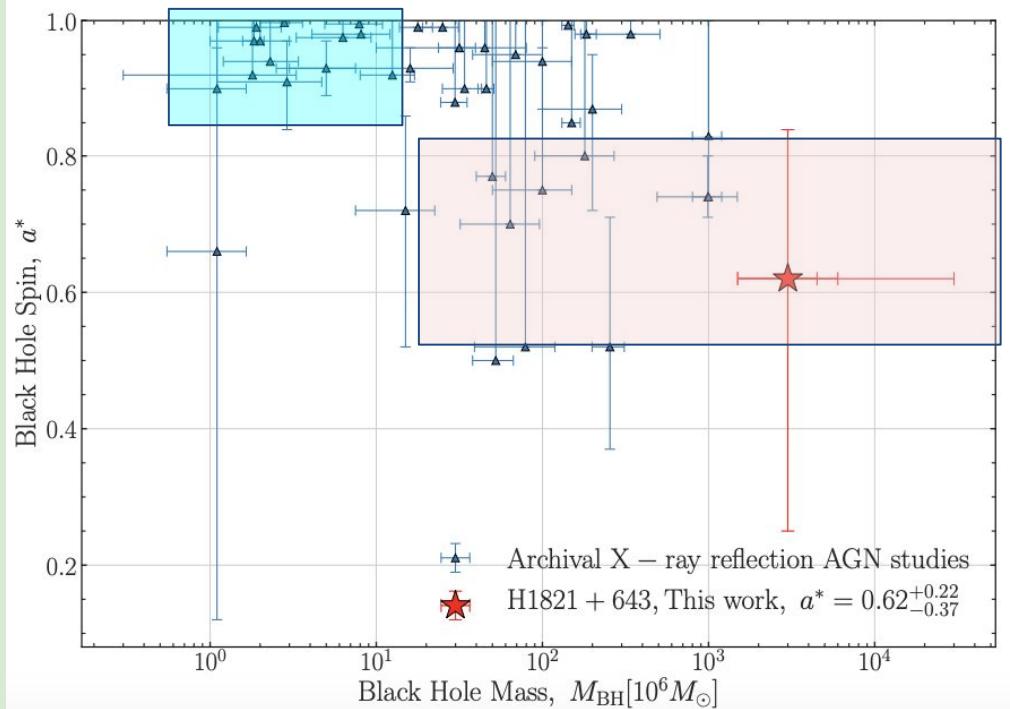
The spin conundrum

Not clear if SMBH should have a 'lot' of spin:

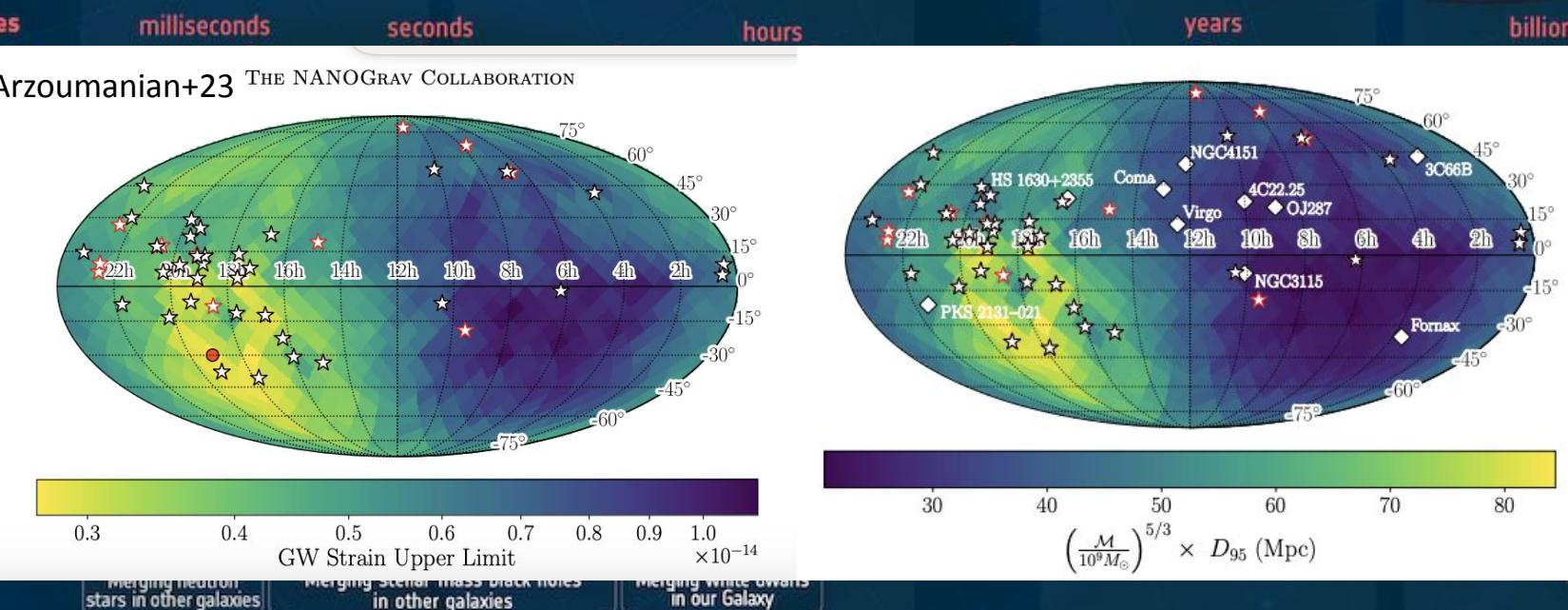
Angular speed of BH is
 $\sim [10^5/M_{\text{BH}}/\text{M}_{\text{sun}}] \{a/(1+\sqrt{1-a})\}$ radians/sec

If $a=0.9$, mass= $1\text{e}06\text{Msun}$
 ~ 0.01 revolutions/sec

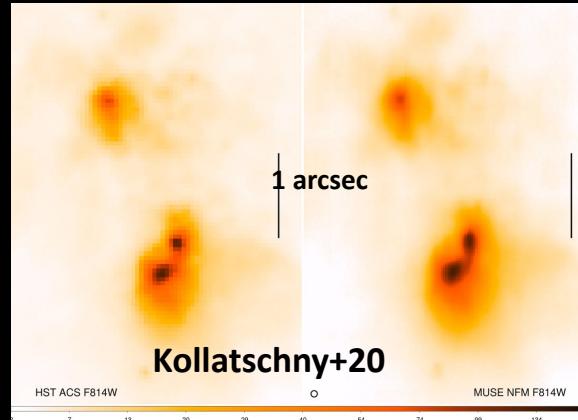
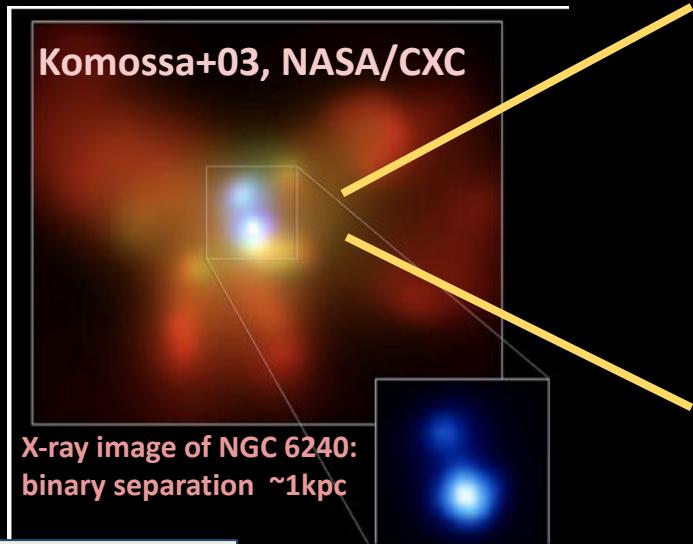
Raynolds+21,
[Sisk-Reynes+22](#)



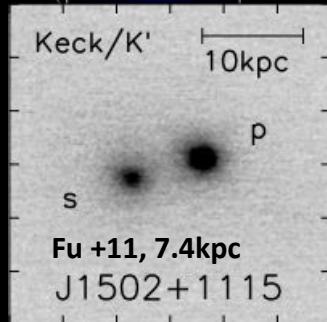
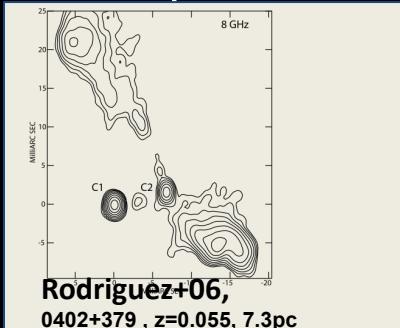
Gravitational waves from supermassive black hole binaries might be ‘right around the corner’



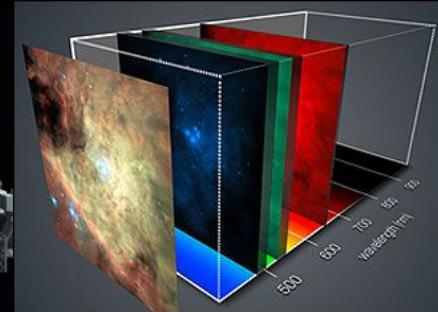
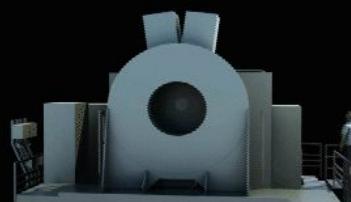
Astronomy images of the day year decade



MUSE image of NGC 6240: A triple nucleus system in the advanced or final state of merging



MUSE@VLT ESO





Binary SMBH parameters hyperspace and imaging

IMAGE RECONSTRUCTION MODEL

Fredholm integral
of the first kind

$$Y(r) = \int_{\Omega} h(r; r') X(r') dr',$$

observation Response function Image to reconstruct

Approximation

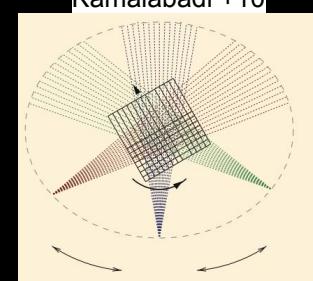
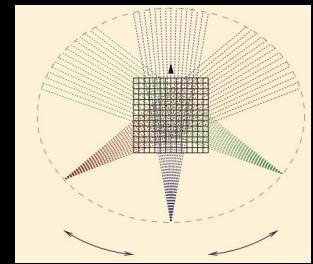
$$y = Hx + w.$$

$$(H)_{ij} = \int_{\Omega} h_i(r') \phi_j(r') dr', \quad 1 \leq i \leq M, \quad 1 \leq j \leq N,$$

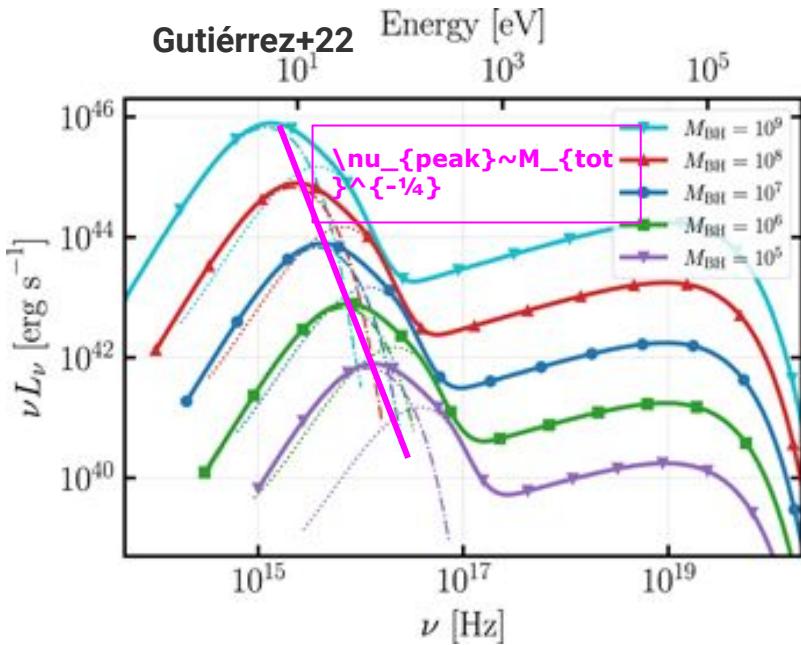
Discretization
over pixels

$$X(r) = \sum_{j=1}^N x_j \phi_j(r).$$

Inclusion of
motion of
object

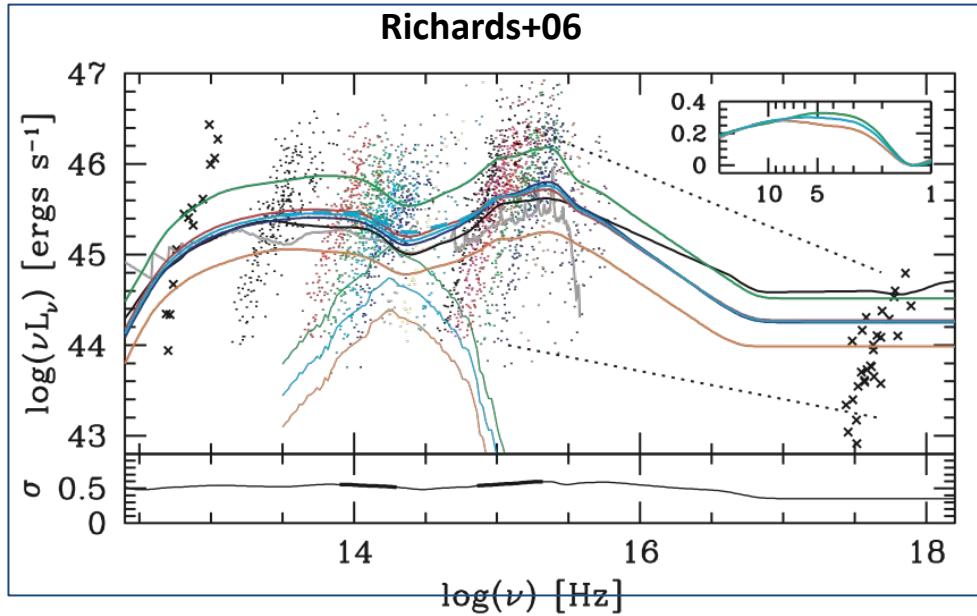


discernible spectral binary SMBH signatures



$$L_{\text{tot}} \sim M_{\text{tot}},$$

$$P \sim M_{\text{tot}} \Rightarrow [< 2 \text{ days, few years}]$$

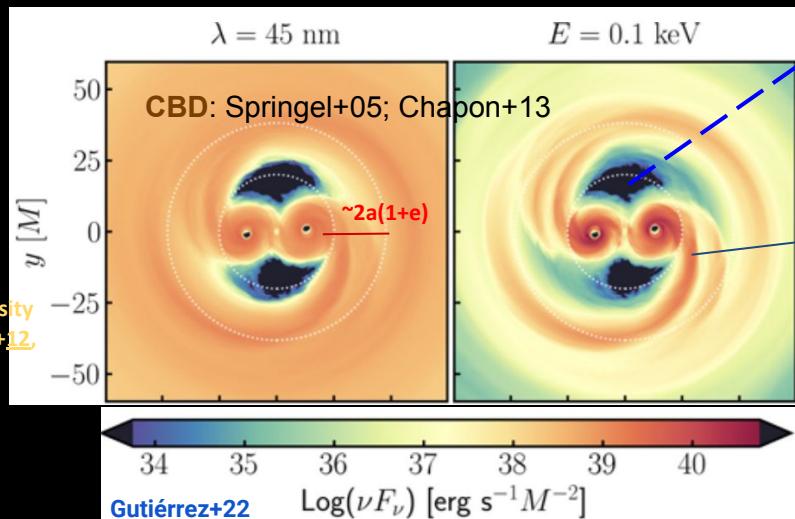


ELECTROMAGNETIC EMISSION AND INFORMATION LOSS

SCHEME OF BINARY SMBH EM

MINIDISC $\sim f(r_{\text{ISCO}}/r_{\text{trunc}})$
 $r_{\text{trunc}} \sim 0.35 - 0.4 r_{12}$
 (Bowen+17);

LUMP: $q > 0.1$, $m = 1$ density mode, the lump, (Noble +12, Shi +12, Farris +14, Noble+21)



Hydro variab < Doppler,
 $q < 0.05$ Farris+14,
 D'Orazio+15,+16

Doppler < hydro variab. In $q=1$, orbital Mach $v_{\text{kep}}/c_s < \sim 20$ Tang+18

ordered spikey/noisy

$$L_{\text{tot}}^{\text{obs}}(t) = \langle L_{\text{tot}} \rangle (1 + \boxed{\delta_{\text{Doppler}}(t)} + \boxed{\delta_{\text{hydro}}(t)}) ,$$

Non-face-on Face-on
 ↑with $\sin i$

CAVITY: MacFadyen & Milosavljević 08, D'Orazio+13, Farris+14, D'Orazio+16, Miranda+17, Muñoz+19,+20, Tiede+20, Derdzinski+21, Newtonian 3D-MHD Shi+12, 3D-GRMHD Noble+12, +21, Bowen+18, +19 Farris+11, Paschalidis+21, Cattorini+21

thin ballistic stream Shi & Krolik 15

$$\Omega_{\text{beat}} \approx \Omega_B - \langle \Omega_{\text{lump}} \rangle \sim 0.72 \Omega_B$$

$$\langle \Omega_{\text{lump}} \rangle = 0.28 \Omega_B \quad \text{Lopez Armengol+21; Noble+21}$$

minidisc masses modulation freq $\sim \Omega_{\text{beat}}$

minidisc masses + lump ang.vel. Ω_{lump} modulation freq $\sim (0.2 - 0.4) \Omega_{\text{binary}}$ and $2\Omega_{\text{beat}}$

binary torques do not completely halt mass accretion
 (MacFadyen & Milosavljević 08; Shi +12; Farris +14; Shi & Krolik 15).

Parity of Doppler and hydro when:

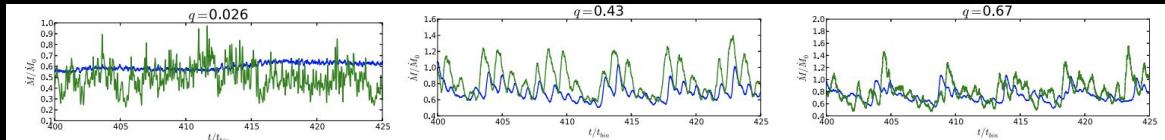
$$v/c \simeq \frac{1.5}{3.44 b} \left(\frac{1+f}{1-f} \right) \max\{b\bar{A}_{\text{MD}}, (1-b)\bar{A}_{\text{CBD}}\}$$

very high orbital velocities,
 $v/c \sim 0.12 - 0.16$

Gutiérrez+22

Red Noise: Mimicking ordered information

Burst model
(Farris+14)



Periodicity signal immersed in red noise

Red Noise mimics periodicity (Vaughan+16)

The power spectral density (PSD) for the DRW is (Kelly+09)

$$dX(t) = -\frac{1}{\tau} X(t) dt + \sigma \sqrt{dt} \epsilon(t) + b dt, \quad \tau, \sigma, t > 0. \quad (1)$$

$$\text{PSD}(f) = \frac{\tau^2 S F_\infty^2}{1 + (2\pi f \tau)^2}.$$

$\text{PSD} \propto f^{-2}$, for $f > 1/(2\pi\tau)$ red noise

$\text{PSD} \propto \text{const}(\text{i.e. const} \times SF_\infty^2)$, for $f < 1/(2\pi\tau)$ white noise

light crossing
time scale

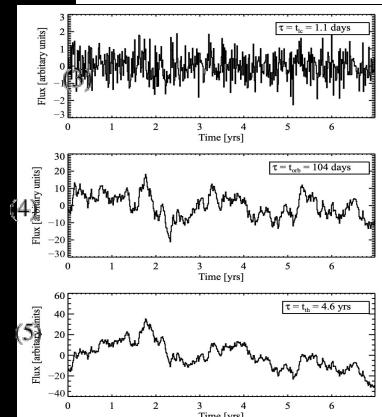
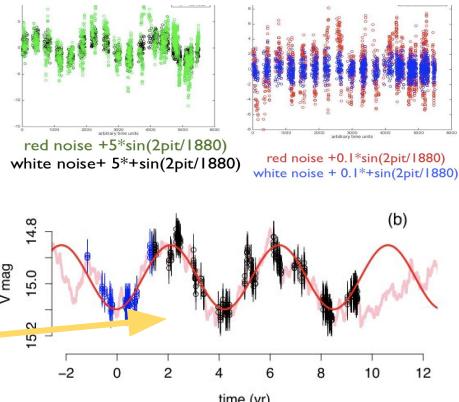
$$t_{lc} = 1.1 \times \left(\frac{M_{BH}}{10^8 M_\odot} \right) \left(\frac{R}{100 R_S} \right) \text{ days},$$

the gas orbital
timescale

$$t_{orb} = 104 \times \left(\frac{M_{BH}}{10^8 M_\odot} \right) \left(\frac{R}{100 R_S} \right)^{3/2} \text{ days},$$

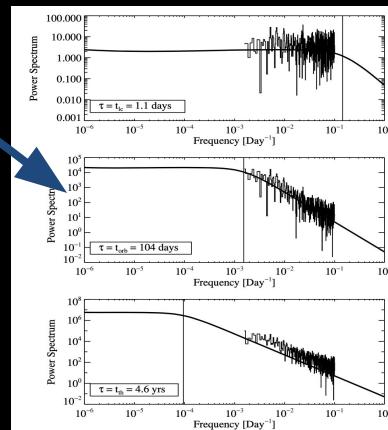
accretion disk
thermal timescale

$$t_{th} = 4.6 \times \left(\frac{\alpha}{0.01} \right)^{-1} \left(\frac{M_{BH}}{10^8 M_\odot} \right) \left(\frac{R}{100 R_S} \right)^{3/2} \text{ yr},$$

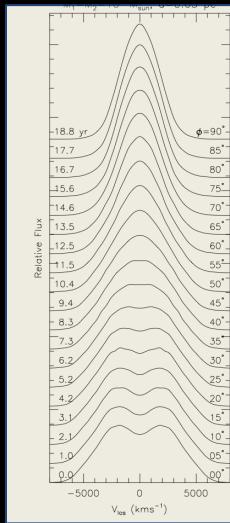


Kelly+09

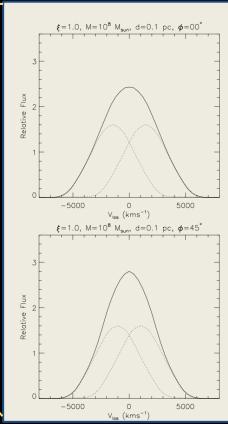
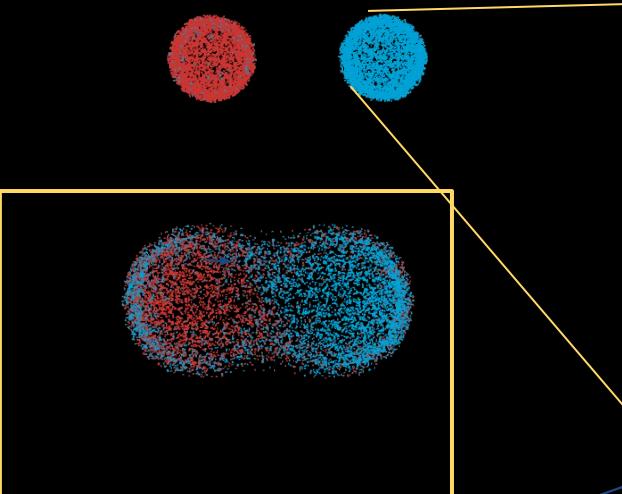
Fourier transform



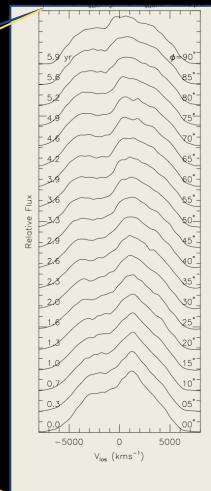
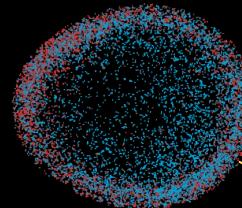
LOSS OF BINARY INFORMATION



optimal

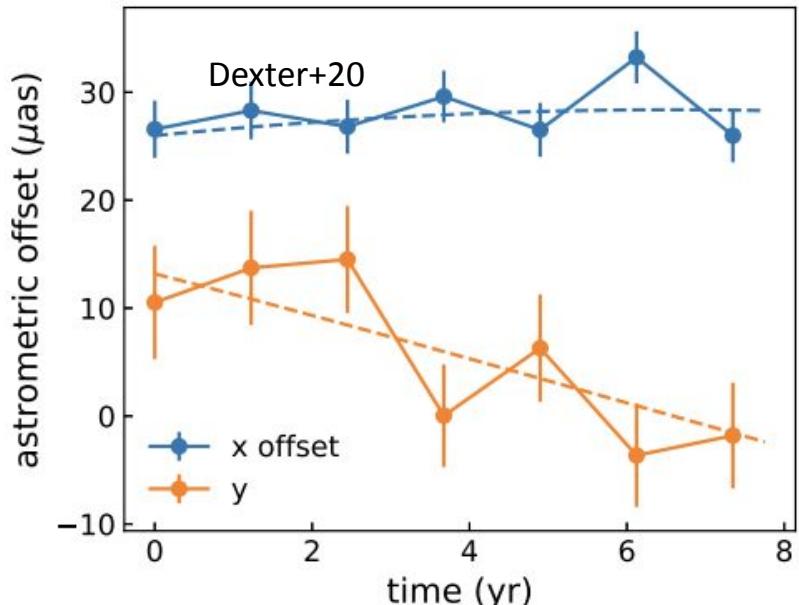


Shen & Loeb+10



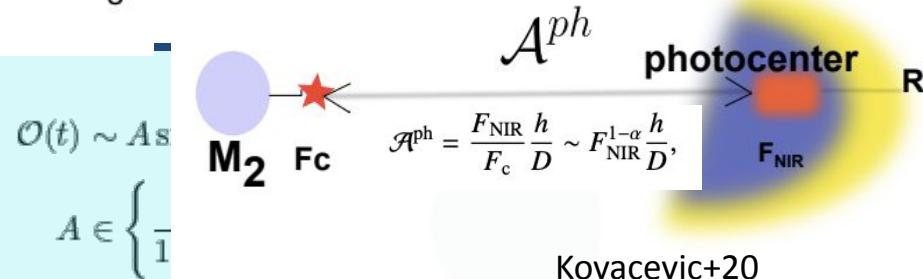
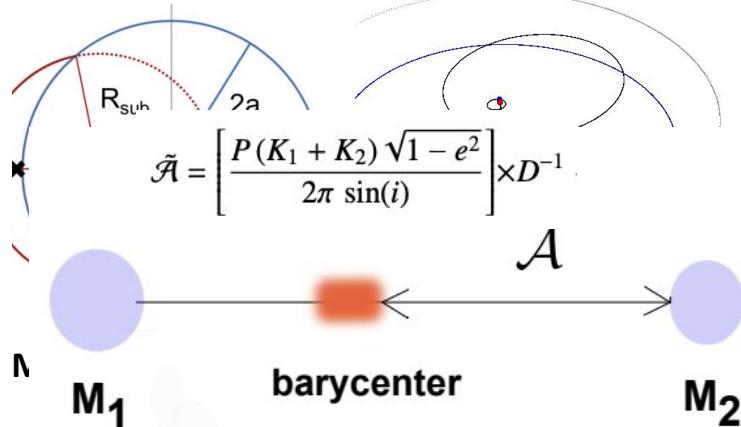
Early works: Popovic+00, Comerford +09;
Bogdanovic+09a,b; Boroson & Lauer+09;
Xu & Komossa+09; Wang+09; Smith+10;
Liu+10, Chornock+10; Gaskell+10 Koss+11;
Eracleous+11

NEW TECHNIQUES FOR FURTHER VETTING OF BINARY CANDIDATES



Circular SMBBH

$$\text{tech} \sim \Delta t_p = \frac{P}{T_{\text{obs,base,} \text{line}}}$$

DYNAMICAL+BRIGHTNESS ASTROMETRY
GRAVITY+

Astrometry with ngEHT, ng VLA

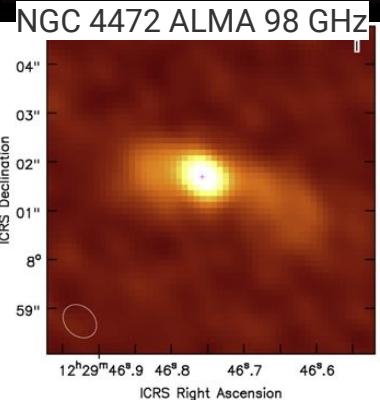
M87 EHT Collaboration

Brighter Jy levels
230 GHz (1.3 mm)

Safarzadeh+19

$$a = \frac{q}{1+q} \times a_0$$

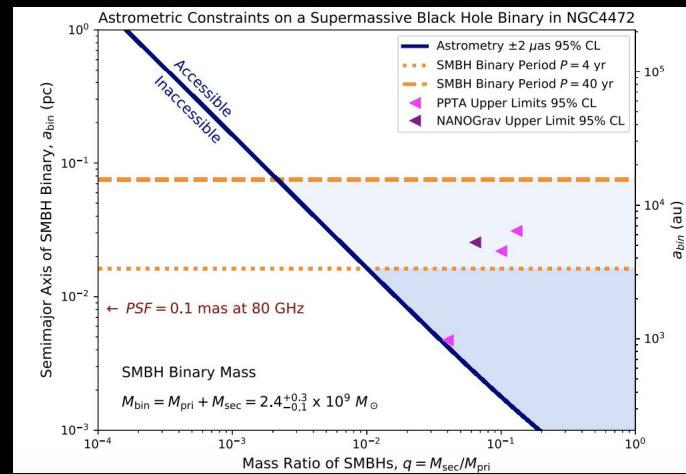
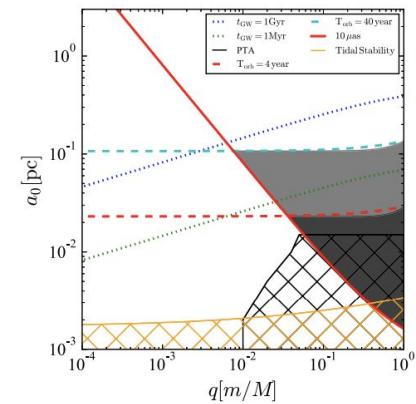
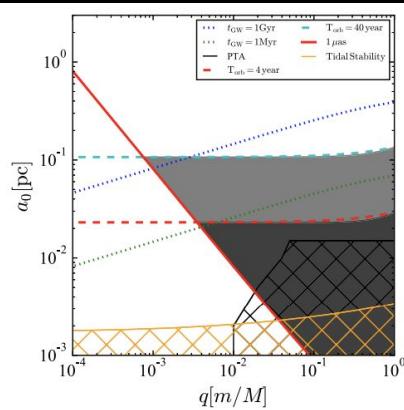
$$a_t = r(1 + q^{1/3})$$



Fainter mJy level
80 GHz (3.7 mm)

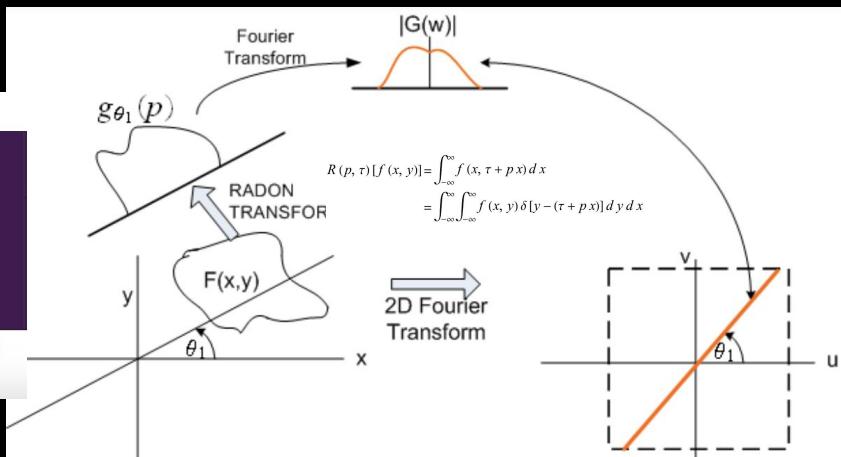
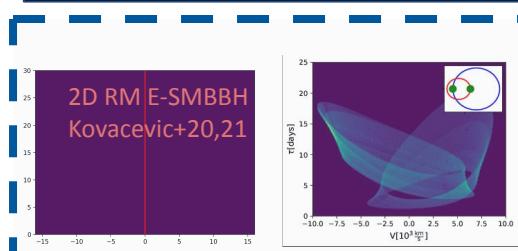
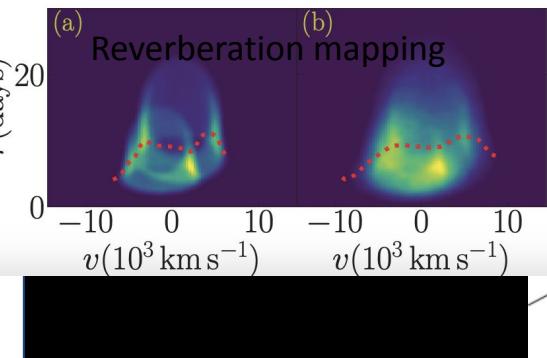
Wrobel & Lazio+22

ng VLA

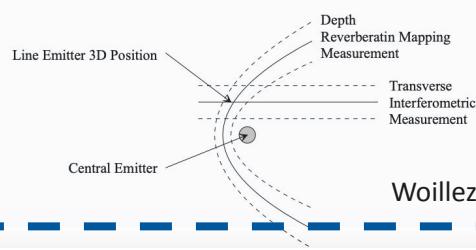


2D REVERBERATION MAPPING \perp INTERFEROMETRY OF BINARY SMBH

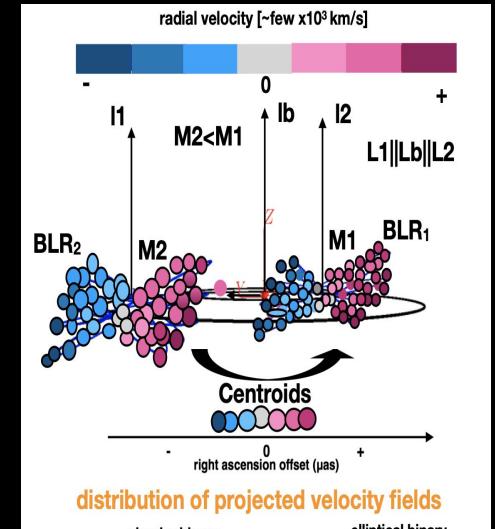
2D RM Circular SMBH
Wang+18



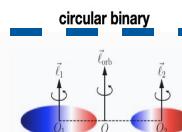
RM+OI



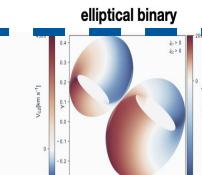
Woillez+03



distribution of projected velocity fields



Songsheng+19

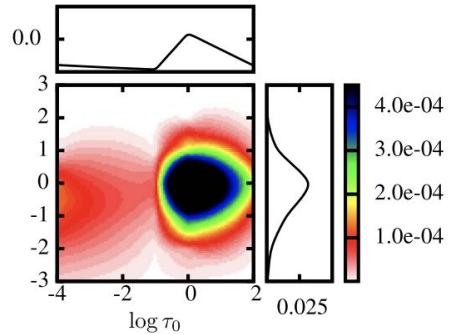


Kovačević+20

Reverberation mapping-taking into account motion of binary SMBH

First Atlases of kinematic signatures

PCA of 1D RM data
Nguyen+20

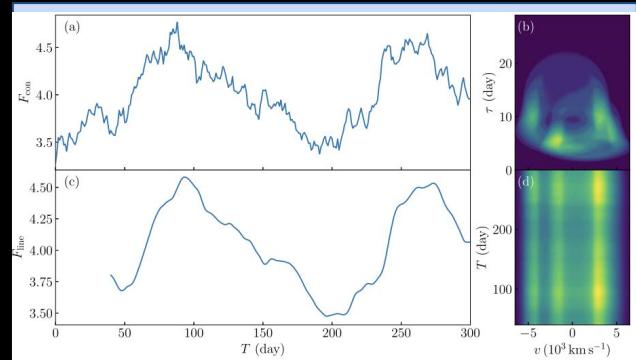


log(F_2/F_1)

$$w(\mathbf{F}^s, \mathbf{F}^o) = \begin{cases} e^{-5 d/d_c}, & \{a, q, e, i\} \text{ repeat} \\ 0, & \{a, q, e, i\} \text{ do not repeat} \end{cases}$$

$$\Pr(x = x') = \frac{\sum_{s=1}^N w(\mathbf{F}^s, \mathbf{F}^o) : x(\mathbf{F}^s) = x'}{\sum_{s=1}^N w(\mathbf{F}^s, \mathbf{F}^o)},$$

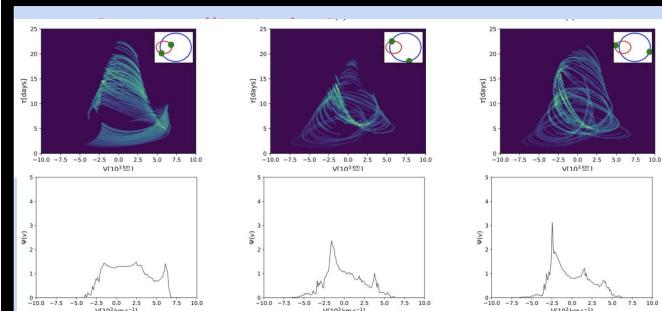
Circular SMBBH
Songsheng +20



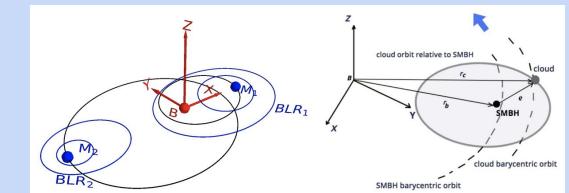
$$\Psi_{1,2}(v, t) = \int d\mathbf{R}_{1,2} \mathcal{H}_{1,2}(v, \mathbf{R}_{1,2}) \delta(t_{1,2}),$$

$$\Psi_{\text{tot}}(v, t) = \frac{\Psi_1(v, t)}{1 + \Gamma_0} + \frac{\Psi_2(v, t)}{1 + \Gamma_0^{-1}},$$

$$\tau = \frac{\int t \Psi_{\text{tot}}(v, t) dt}{\int \Psi_{\text{tot}} dt}.$$



$$\Psi(v, \tau) = \epsilon_0 \int_{R_{\text{in}}}^{R_{\text{out}}} \varrho^{-q} d\varrho \int_0^{2\pi} d\Omega \int_{-i_{\min}}^{i_{\max}} \sin idi \int_0^{2\pi} \delta(X_1) \delta(X_2) dE,$$



$$Q(\mathbf{u}, \lambda) = \iint I(\sigma, \lambda) e^{-2\pi i \sigma \cdot \mathbf{u}} d\alpha d\beta,$$

moments of intensity distribution

$$\mu_{lm} = \iint I \delta \lambda(\sigma, \lambda) \alpha^l \beta^m d\alpha d\beta.$$

centroids

$$p_\alpha(\lambda) = \frac{\mu_{10}}{\mu_{00}} = \frac{\iint \alpha I(\sigma, \lambda) d\alpha d\beta}{\iint I(\sigma, \lambda) d\alpha d\beta}$$

$$p_\beta(\lambda) = \frac{\mu_{01}}{\mu_{00}} = \frac{\iint \beta I(\sigma, \lambda) d\alpha d\beta}{\iint I(\sigma, \lambda) d\alpha d\beta}.$$

$$-\text{Arg}\left(\frac{Q(\mathbf{u}, \lambda)}{\mu_{00}}\right) \sim \frac{\int \sin(2\pi\sigma \cdot \mathbf{u}) I(\sigma, \lambda) d\alpha d\beta}{\int \cos(2\pi\sigma \cdot \mathbf{u}) I(\sigma, \lambda) d\alpha d\beta}$$

Fringe phase

$$\sim 2\pi \frac{\int I(\sigma, \lambda) \sigma d\alpha d\beta}{\int I(\sigma, \lambda) d\alpha d\beta} \mathbf{u}$$

$$\sim 2\pi \mathbf{u} \cdot \boldsymbol{\xi}(\lambda)$$

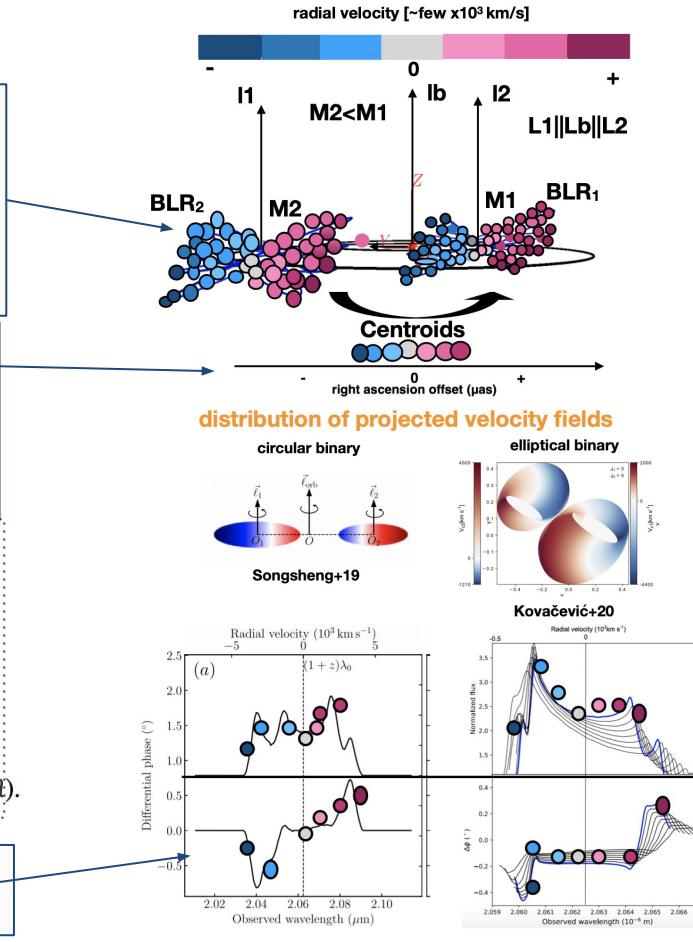
$$= 2\pi u \xi_\alpha(\lambda) + 2\pi v \xi_\beta(\lambda).$$

centroids vs fringe phase

$$\xi_\alpha(\lambda) = \frac{\mu_{10}}{\mu_{00}} = p_\alpha(\lambda) \quad \xi_\beta(\lambda) = \frac{\mu_{01}}{\mu_{00}} = p_\beta(\lambda).$$

Differential phase

$$\Delta\phi = -2\pi \mathbf{u} \cdot (\boldsymbol{\xi}(\lambda) - \boldsymbol{\xi}(\lambda_r)).$$



Generalized binary signal

$$I(\sigma, \lambda) = I_1(\sigma_1, \lambda) + I_2(\sigma_2, \lambda).$$

$$Q(\mathbf{u}, \lambda) = Q_1(\mathbf{u}, \lambda) + Q_2(\mathbf{u}, \lambda) = F_1 e^{-2\pi i \sigma_1 \cdot \mathbf{u}} + F_2 e^{-2\pi i \sigma_2 \cdot \mathbf{u}},$$

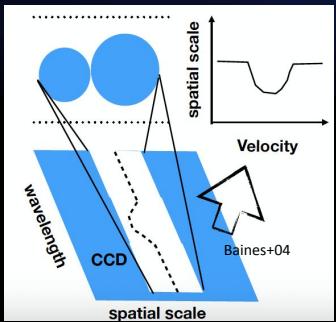
$$Q_n(\mathbf{u}, \lambda) = \frac{F_1 e^{-2\pi i \sigma_1 \cdot \mathbf{u}} + F_2 e^{-2\pi i \sigma_2 \cdot \mathbf{u}}}{F_1 + F_2}$$

$$\text{Arg}(Q_n(\mathbf{u}, \lambda)) \sim \arctan\left(\frac{\text{Im}(Q_n(\mathbf{u}, \lambda))}{\text{Re}(Q_n(\mathbf{u}, \lambda))}\right)$$

$$\text{Kovacevic+20} \sim 2\pi \mathbf{u} \cdot \frac{F_1 \sigma_1 - F_2 \sigma_2}{F_1 + F_2}.$$

SA+RM

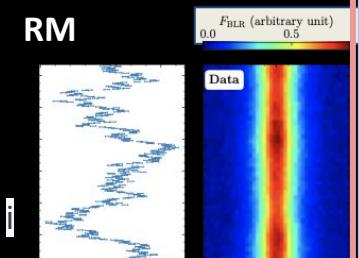
BINARY



$$\mathbf{F} = (F_1, F_2) \text{ and } \mathbf{E} = \left(\exp\left(i \cdot \frac{2\pi S}{\lambda}\right), \exp\left(i \cdot \frac{2\pi(S-a \sin(i))}{\lambda}\right) \right)$$

$$T \propto \langle \mathbf{F}, \mathbf{E} \rangle.$$

RM



$P(\text{Model} | (\text{SA, RM})) \propto P(\text{SA} | \text{Model}) * P(\text{RM} | \text{Model}) * P(\text{Model})$
Li&Wang+22

Wang+20

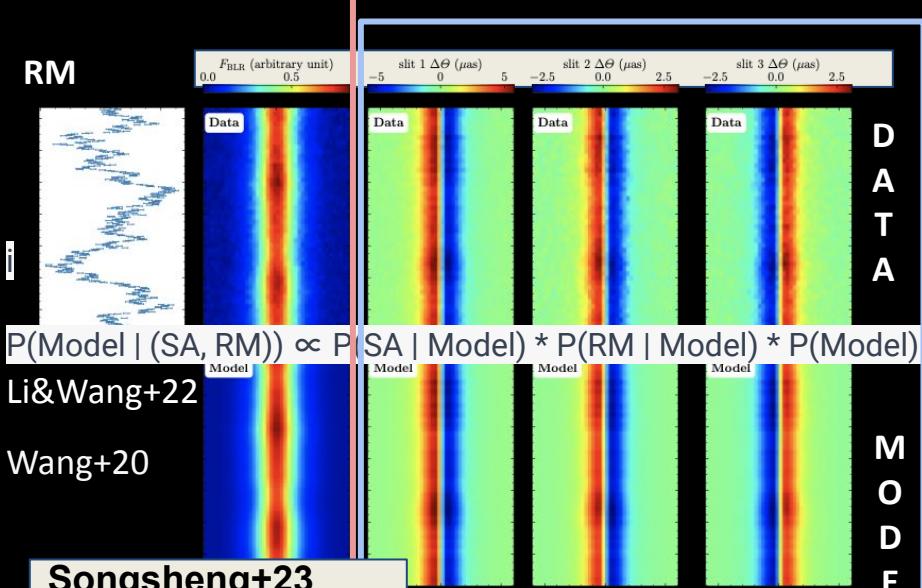
Songsheng+23

D
A
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M
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L

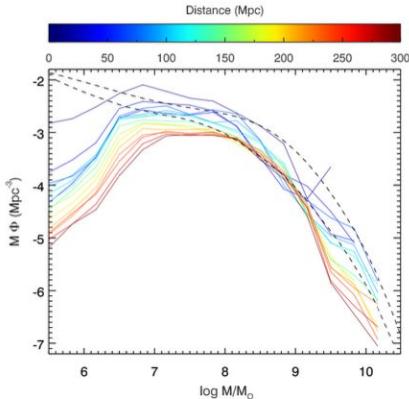
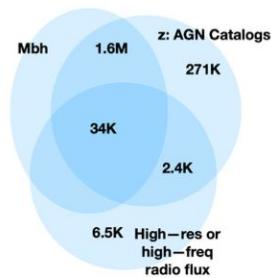
SA

$$\Theta(v, t) = \frac{F'_c(t)\Theta_c(v, t) + F_{\text{BLR}}(v, t)\Theta_{\text{BLR}}(v, t)}{F'_c(t) + F_{\text{BLR}}(v, t)}$$



Event Horizon and Environs (ETHER): A Curated Database for EHT and ngEHT Targets and Science

Ramakrishnan +23



The Vera C. Rubin Observatory will enable extensive studies of periodic flux variability, and is thus expected to significantly enlarge the sample of binary black hole candidates

~160 binary candidates

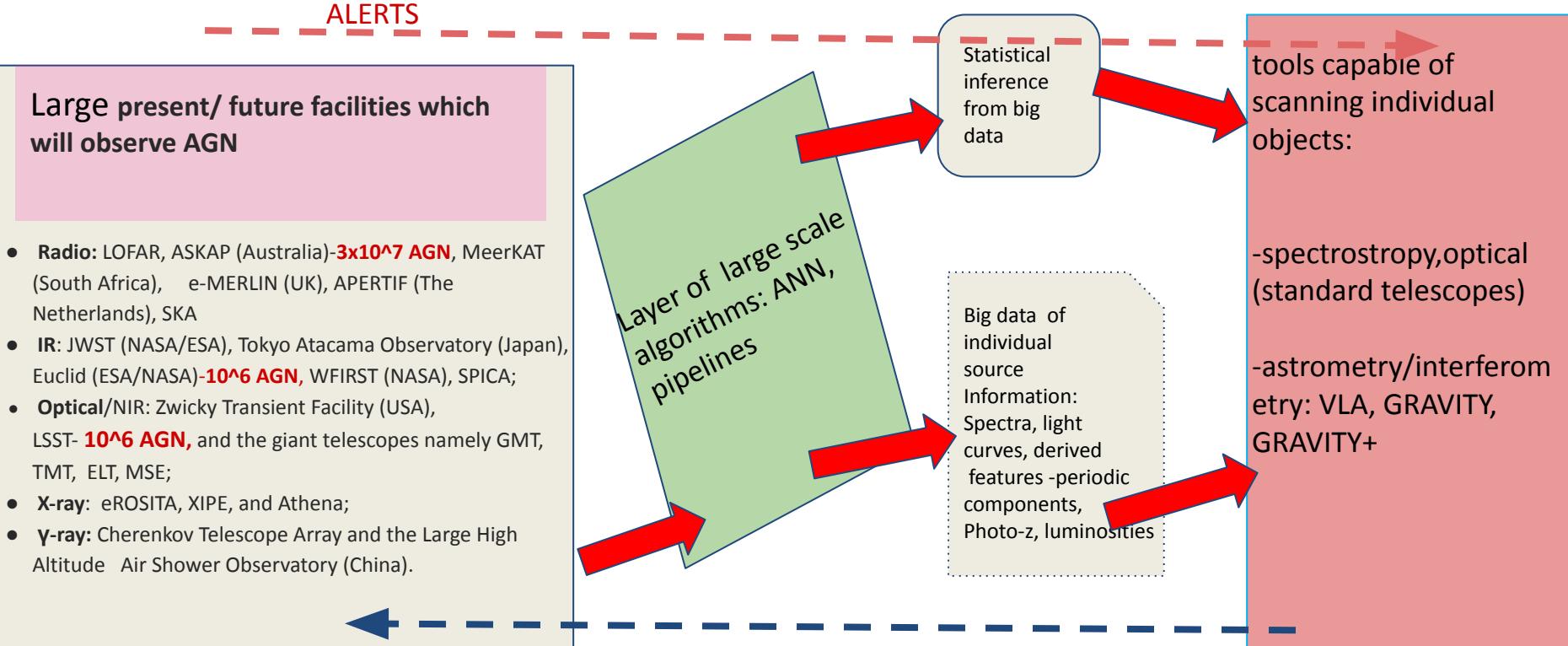
~10 from VLBI

~few candidates
double velocity components in NLR/BLR

Majority~
periodic flux variability

A few
X-shaped
radio
sources

Move forward **instead of** looking back.



PILLARS OF MULTIMESSINGER ASTRONOMY

eZ

ZWICKY TRANSIENT FACILITY

