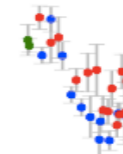
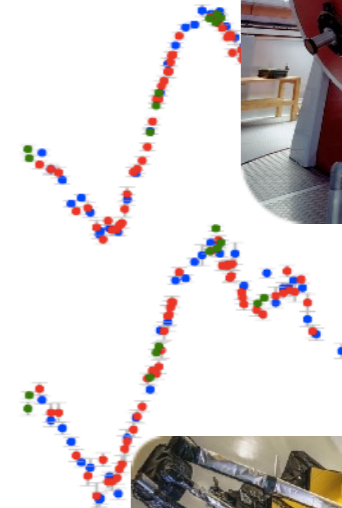
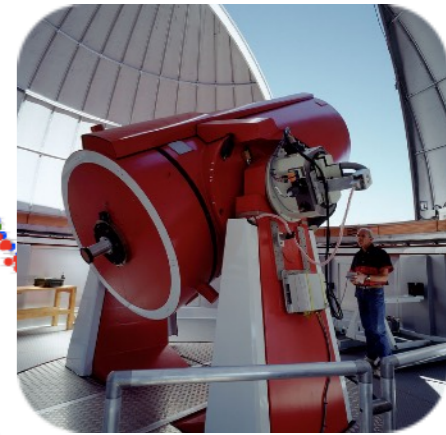
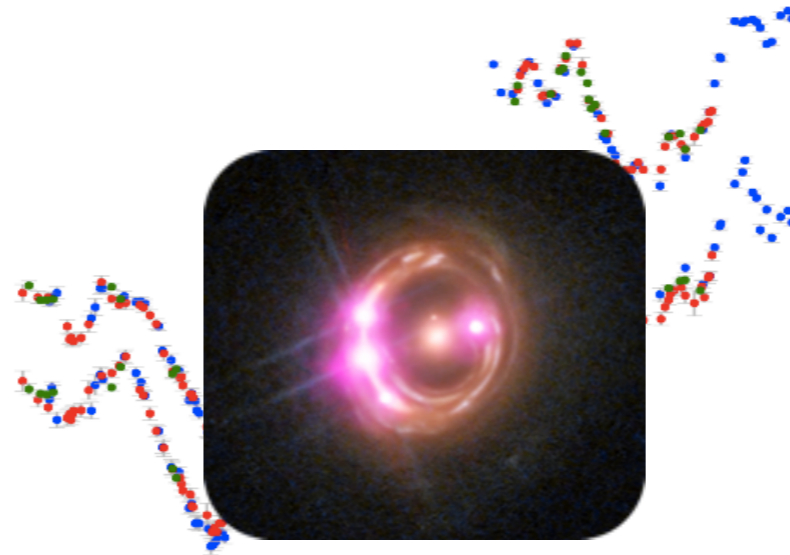
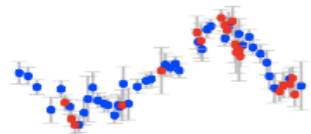
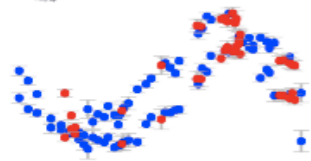
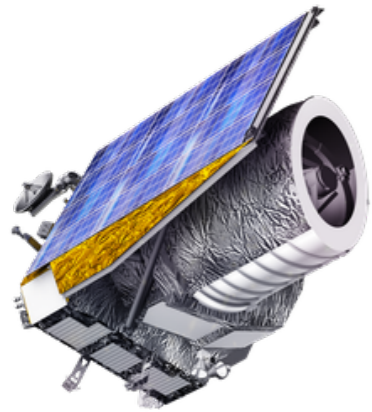


# Time Delay Cosmography with Strongly Lensed quasars

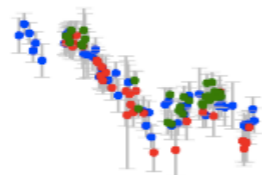
Frédéric Courbin (EPFL, Switzerland)  
For the TDCOSMO collaboration



COSMICLENS

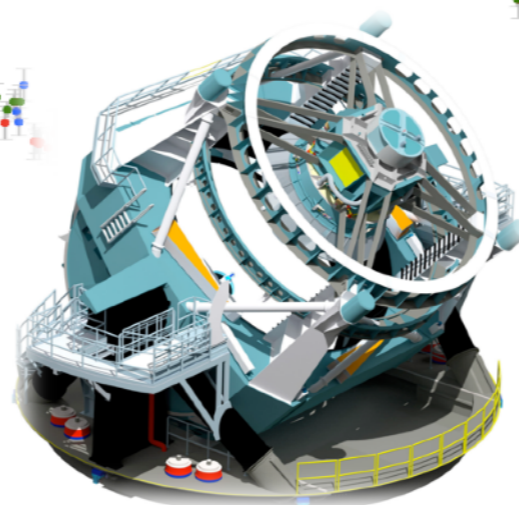


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FONDO NAZIONALE SVIZZERO  
SWISS NATIONAL SCIENCE FOUNDATION

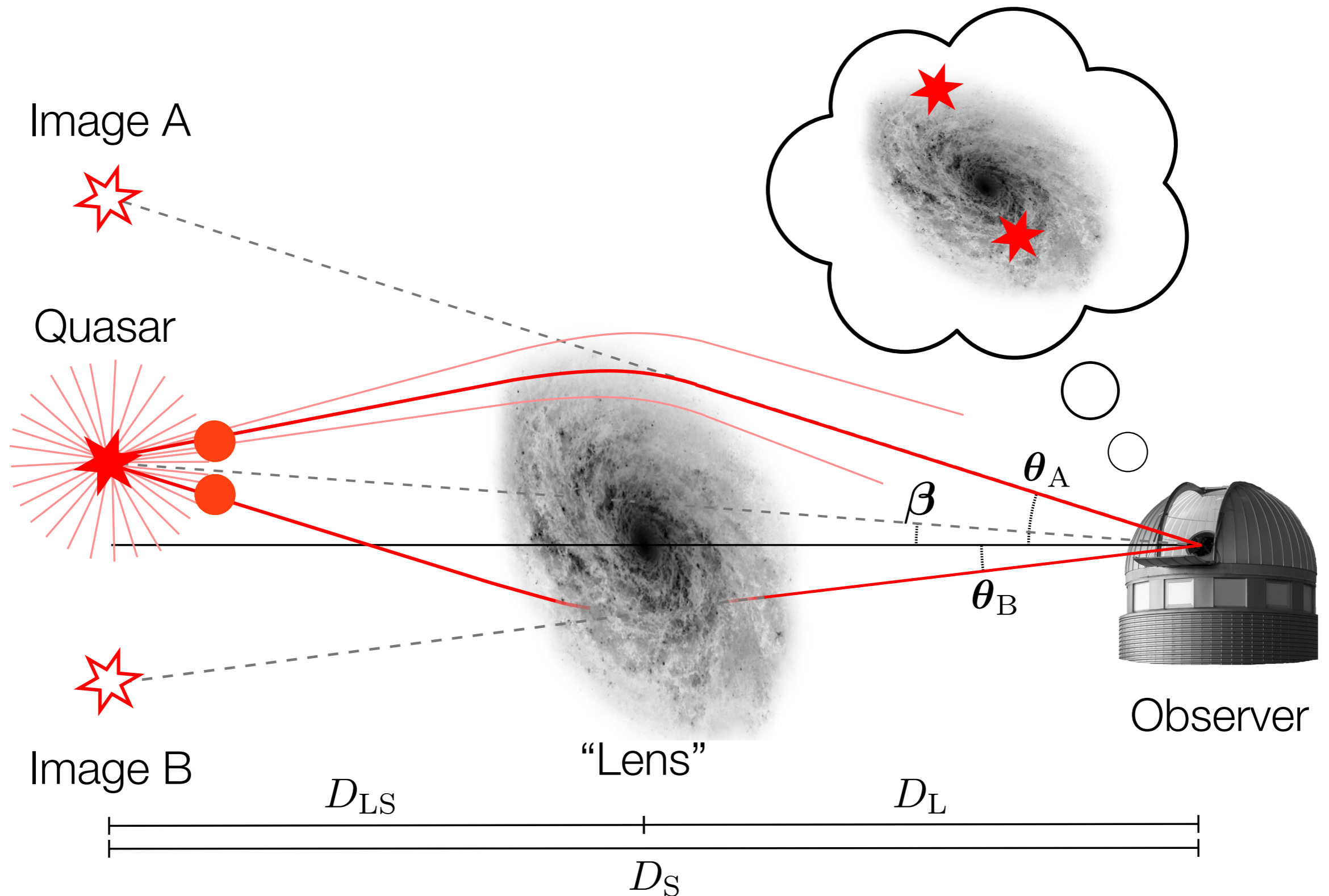


EPFL

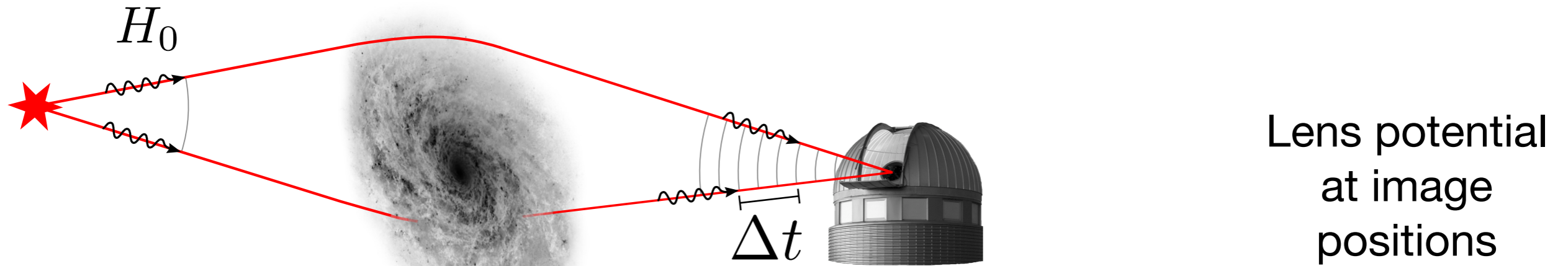
Laboratoire d'astrophysique <http://lastro.epfl.ch>  
Ecole Polytechnique Fédérale de Lausanne (EPFL)

CosmoVeese - Lisbon - May 2023

# Time Delays in Strongly Lensed Quasars



# Time Delays Measure the Hubble Constant $H_0$



Lens potential  
at image  
positions

Source position  
(unconstrained)

Astrometry  
of the images



Sjur Refsdal  
(1964)

$$\Delta t = \frac{1 + z_L}{c} \underbrace{\frac{D_L D_S}{D_{LS}}}_{D_{\Delta t}} \cdot \Delta \left( \frac{1}{2} |\vec{\theta} - \vec{\beta}|^2 - \psi(\vec{\theta}) \right)$$

$$D_{\Delta t} \propto 1/H_0$$

Time delays provide a *single-step* and *independent* constraint on  $H_0$ .

# Time Delay Cosmography Collaborations

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H0  
Lenses  
in  
COSMOGRAIL'S  
Wellspring

PI: Suyu

COSmological  
MONitoring  
GRAvitational  
Lenses

PI: Courbin

Now grouped as TDCOSMO : Time Delay COSMOgraphy ([tdcosmo.org](http://tdcosmo.org))  
See also ERC project COSMICLENs ([cosmiclens.epfl.ch](http://cosmiclens.epfl.ch))

# Example of RX J1131-123

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Time delays between lensed images

# Example of RX J1131-123

---

**Time delays** between lensed images

Mass in the Einstein ring

**Mass slope** at image position



# Example of RX J1131-123

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Time delays between lensed images

Mass in the Einstein ring  
Mass slope at image position

Mass contribution of intervening galaxies  
along the line-of-sight (external mass sheet)

**ALL ANALYSIS BLIND !**



# 1- Time Delay Measurements

# Photometry with image deconvolution



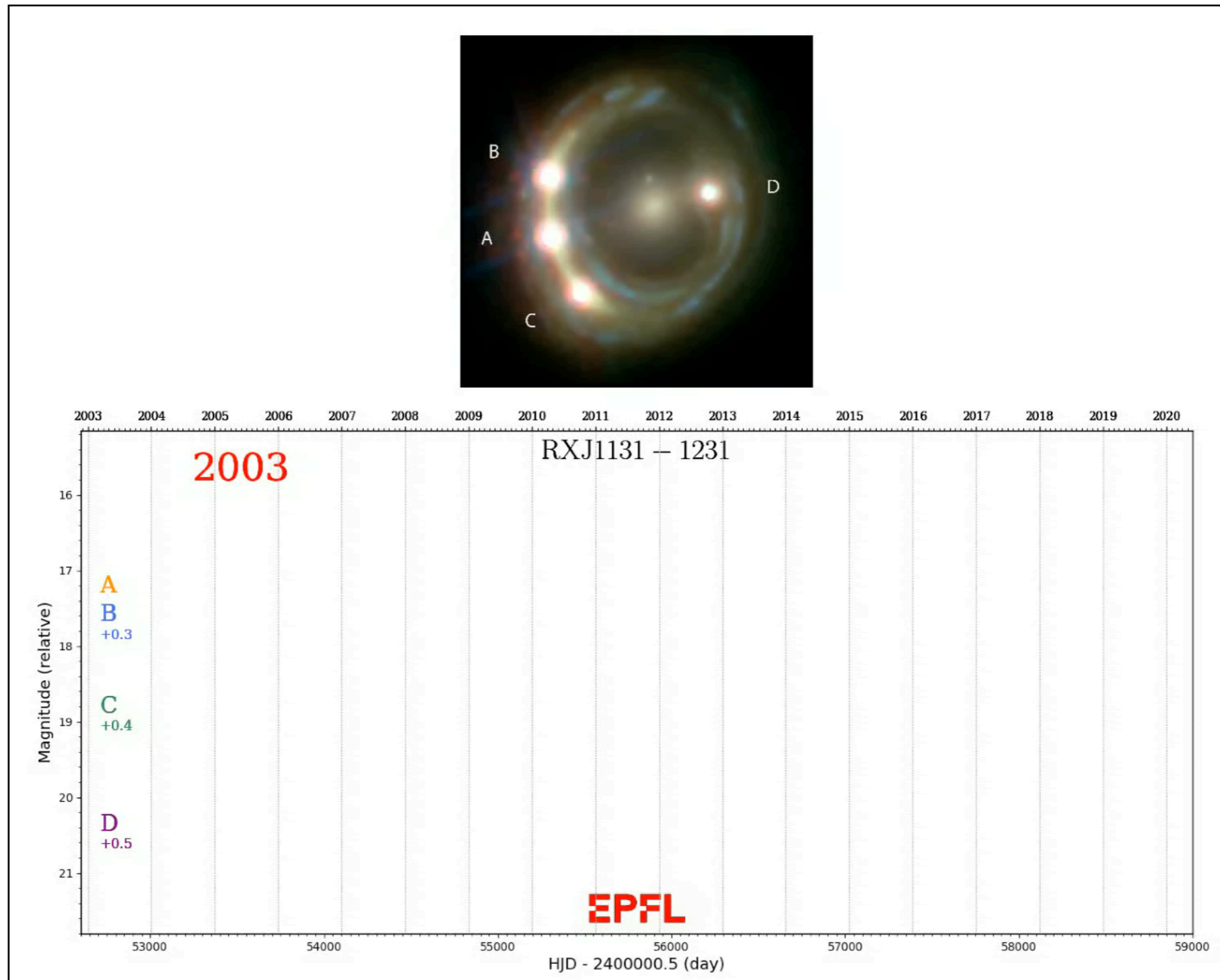
Deconvolution methods **with finite resolution** described in

Magain, Courbin, Sohy, 1998, ApJ 494, 472

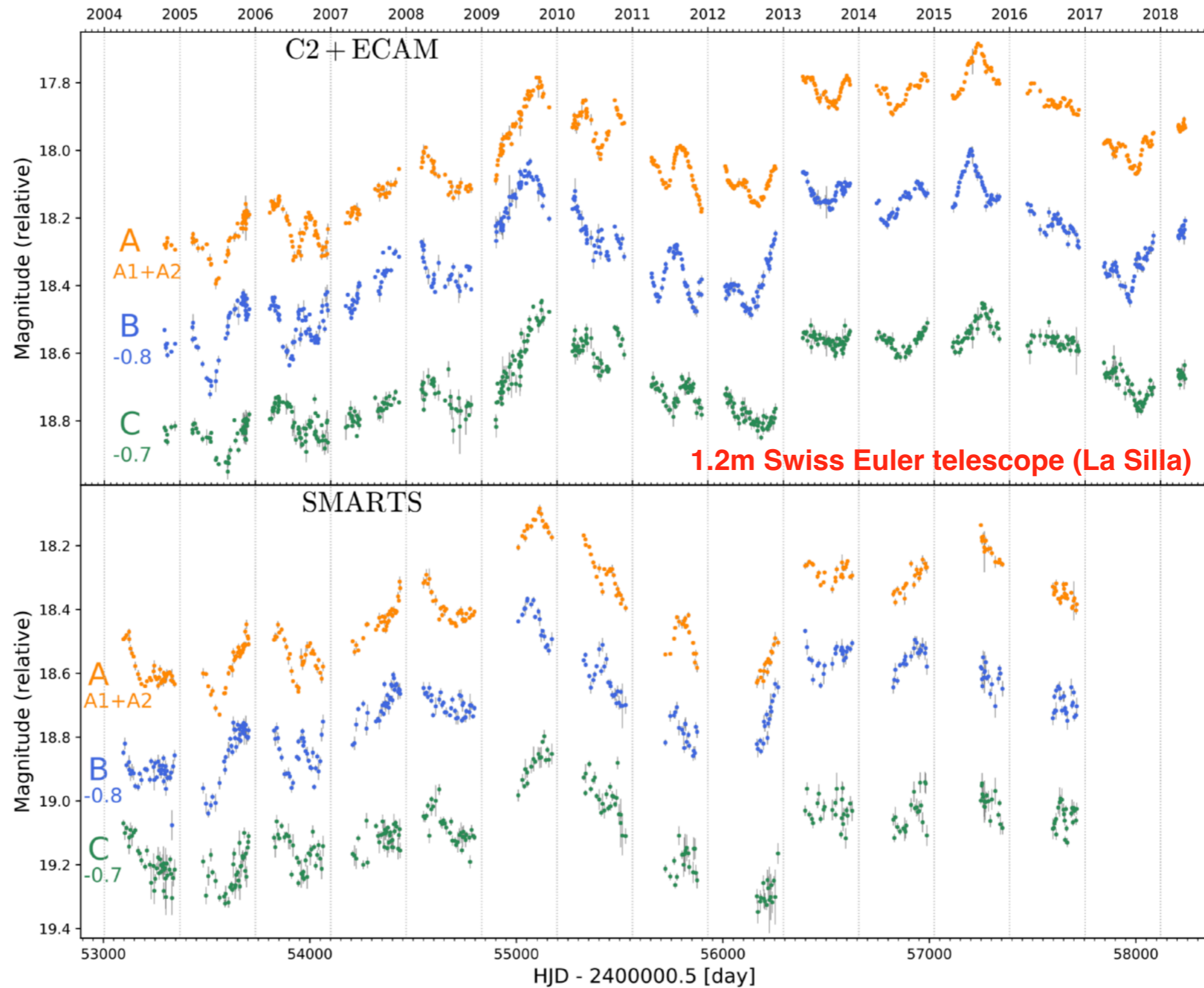
Cantale, Courbin, et al. 2016, A&A 589, 81

Millon et al. 2023 in press : JAX version including wavelet regularization -> in Rubin-LSST pipeline

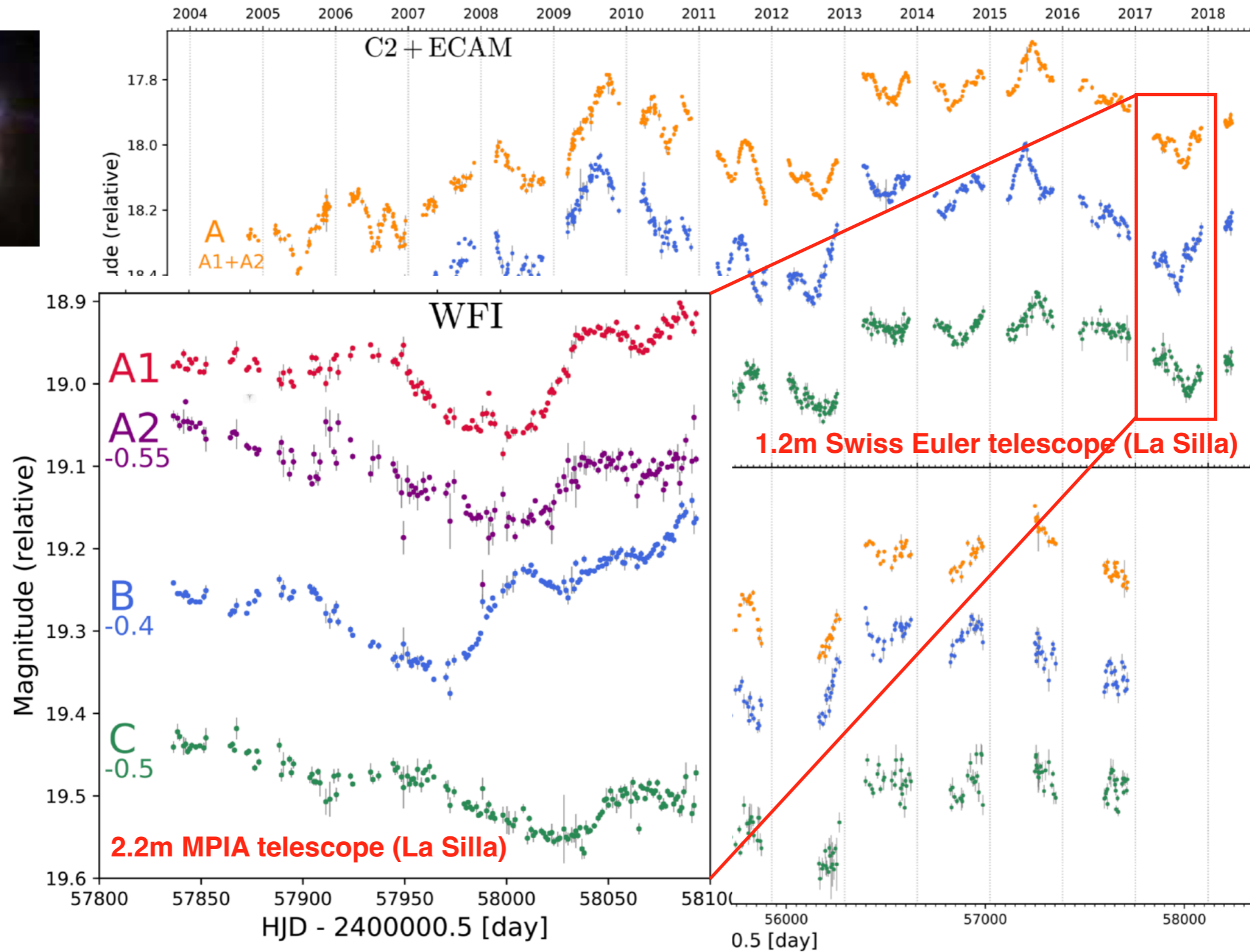
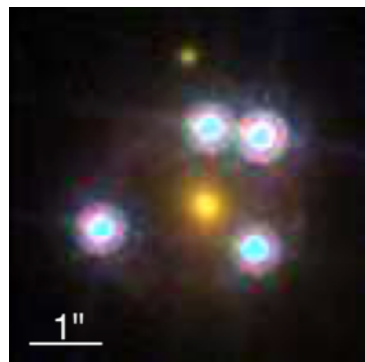
# COSMOGRAIL Light Curves of RXJ1131-123



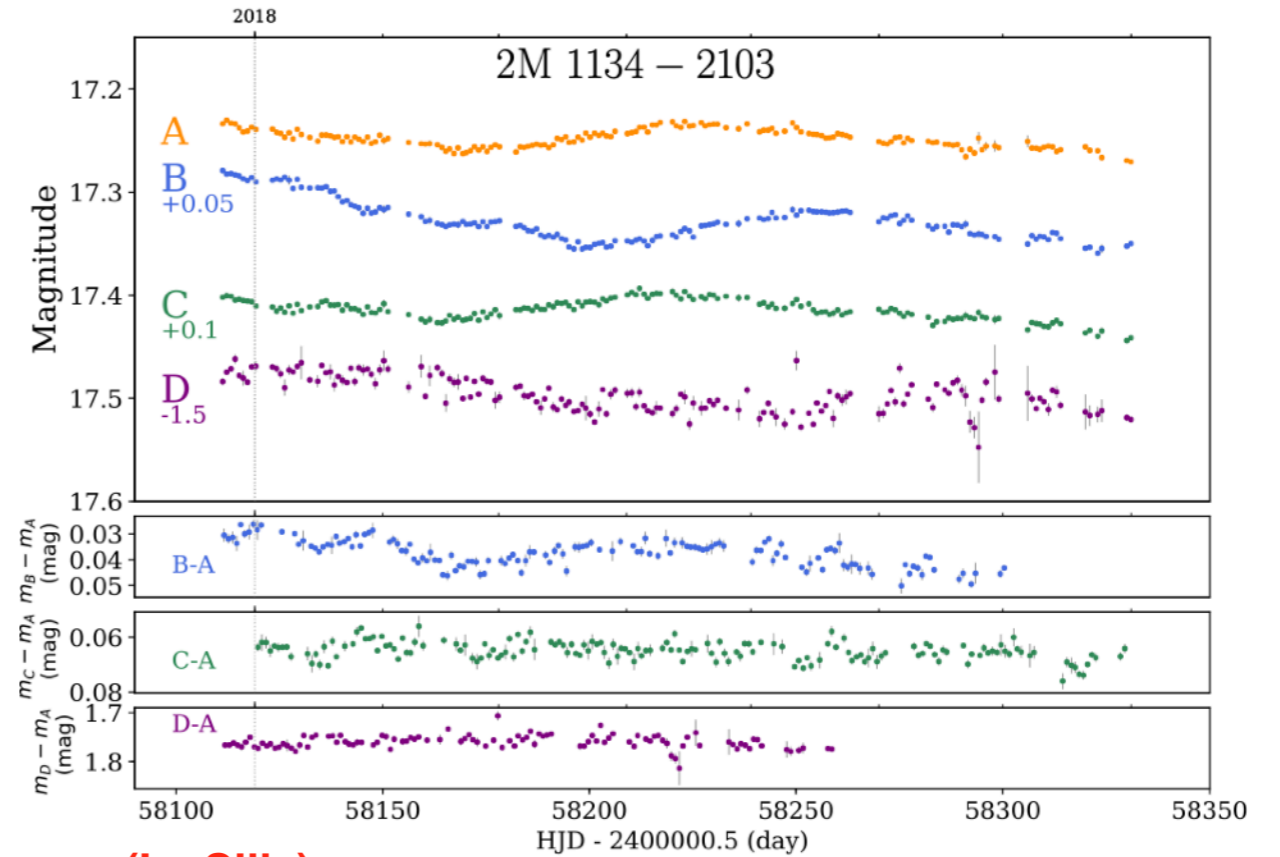
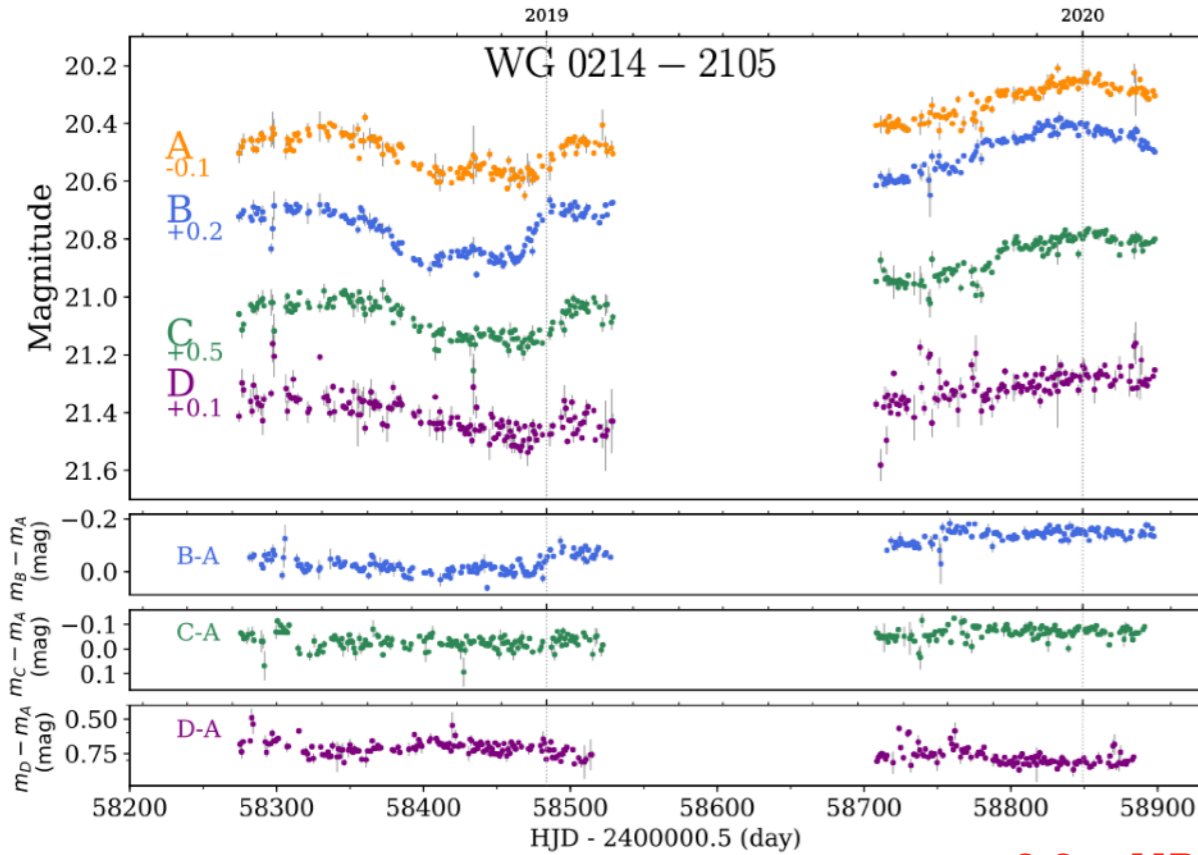
# COSMOGRAIL Light Curves of WFI2033-4723



# MPIA 2.2m Light Curves of WFI2033-4723

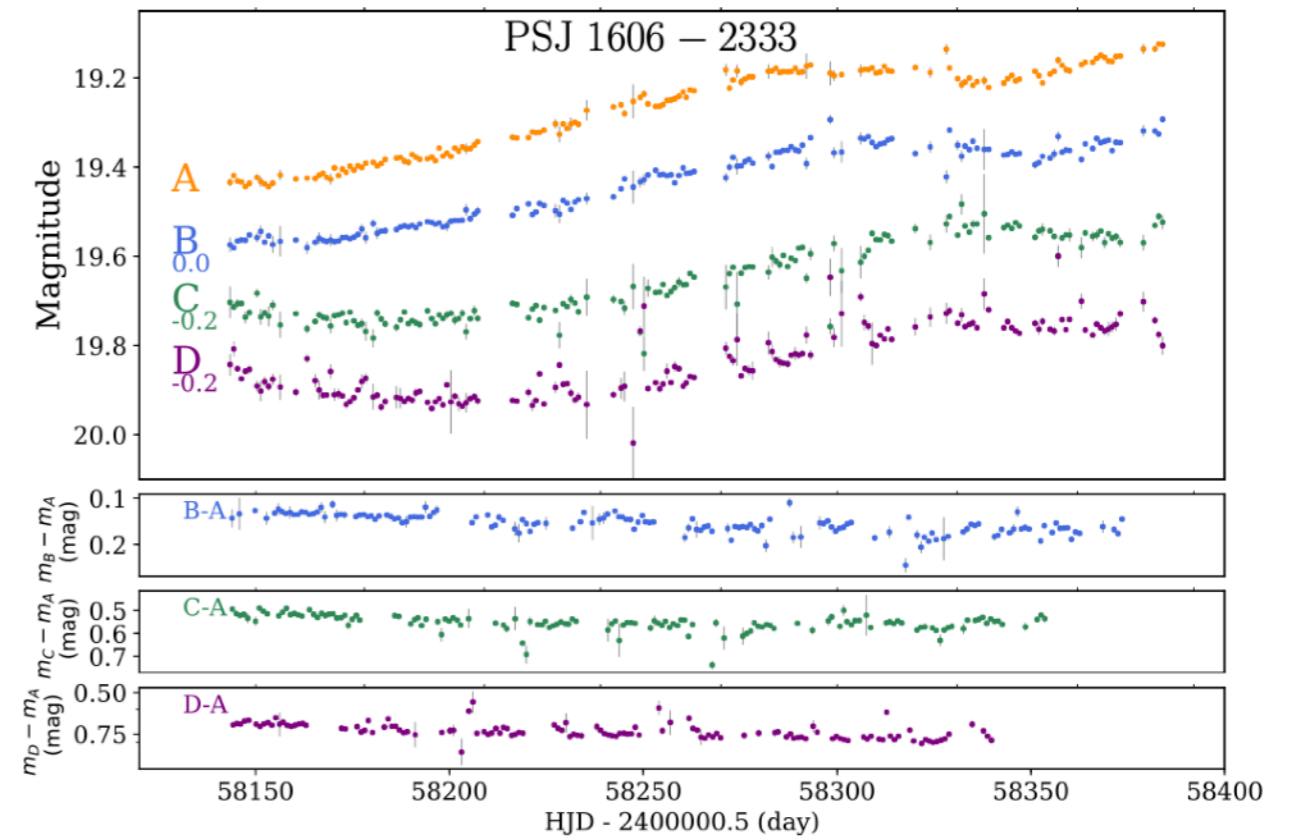


# Mass Production of Time Delays

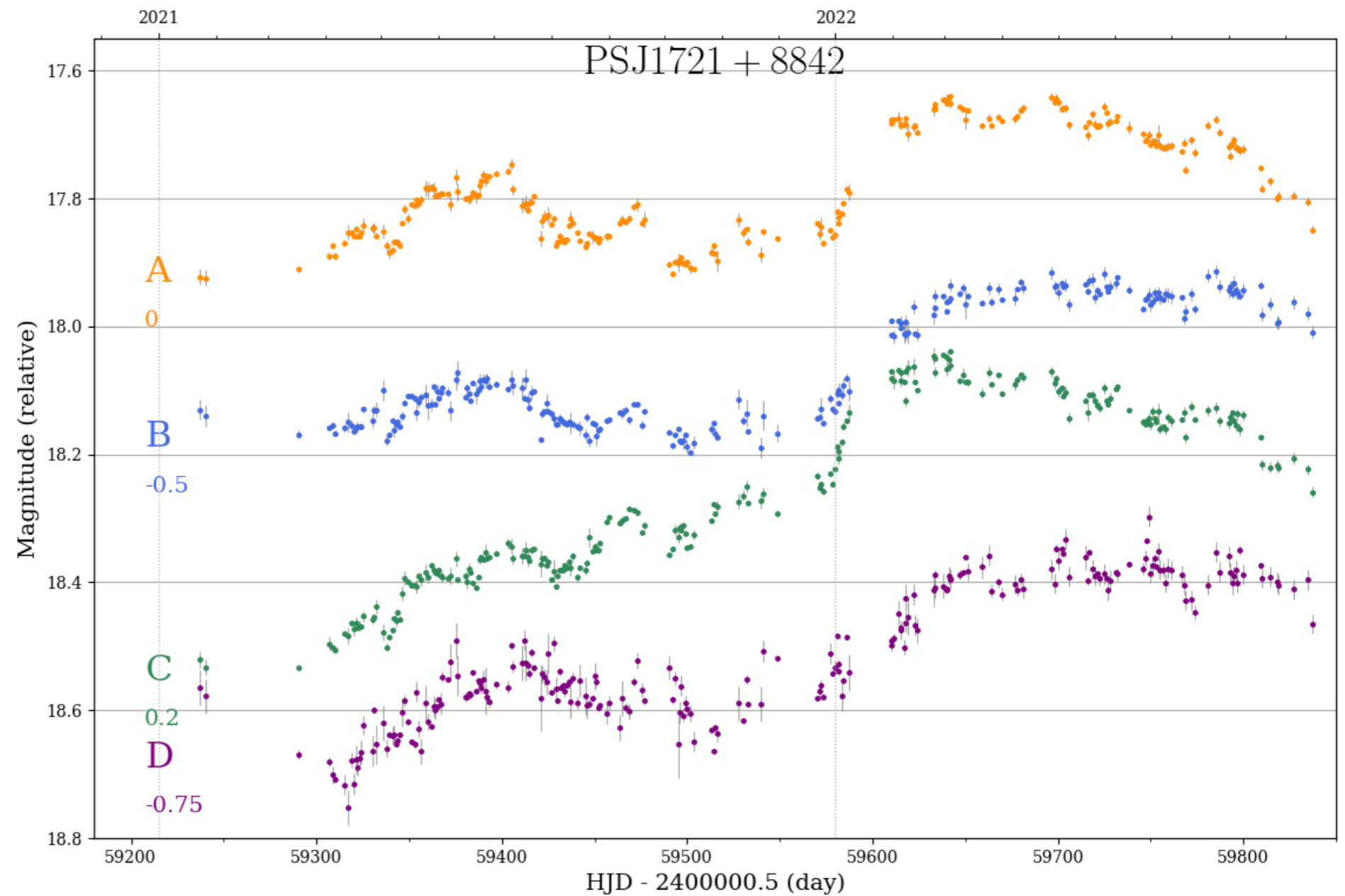
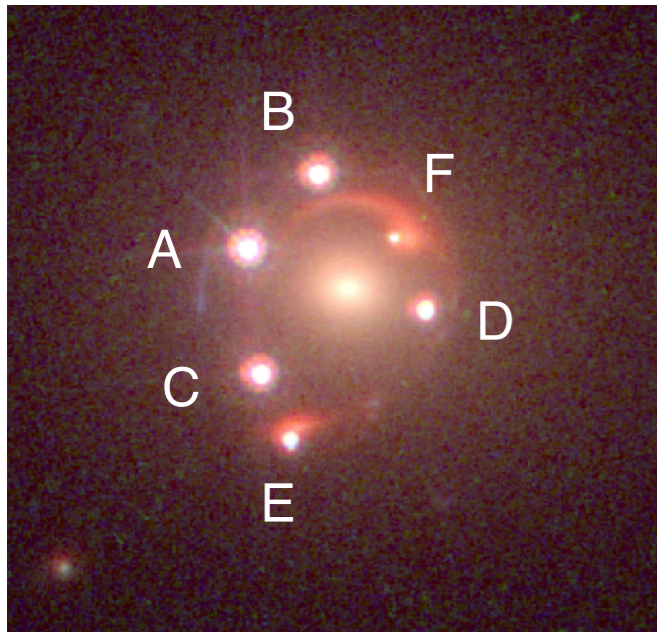


2.2m MPIA telescope (La Silla)

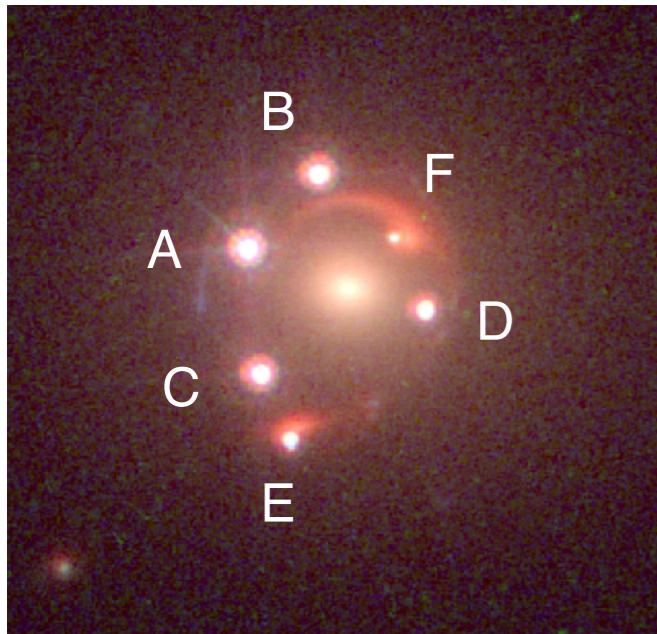
- 2m to 3m telescopes
- Daily cadence
- 30 min exposure per epoch
- 3 mmag precision per epoch
- Single-season measurement
- Better than LSST !
- More to come with 2000h of 2.6m VST



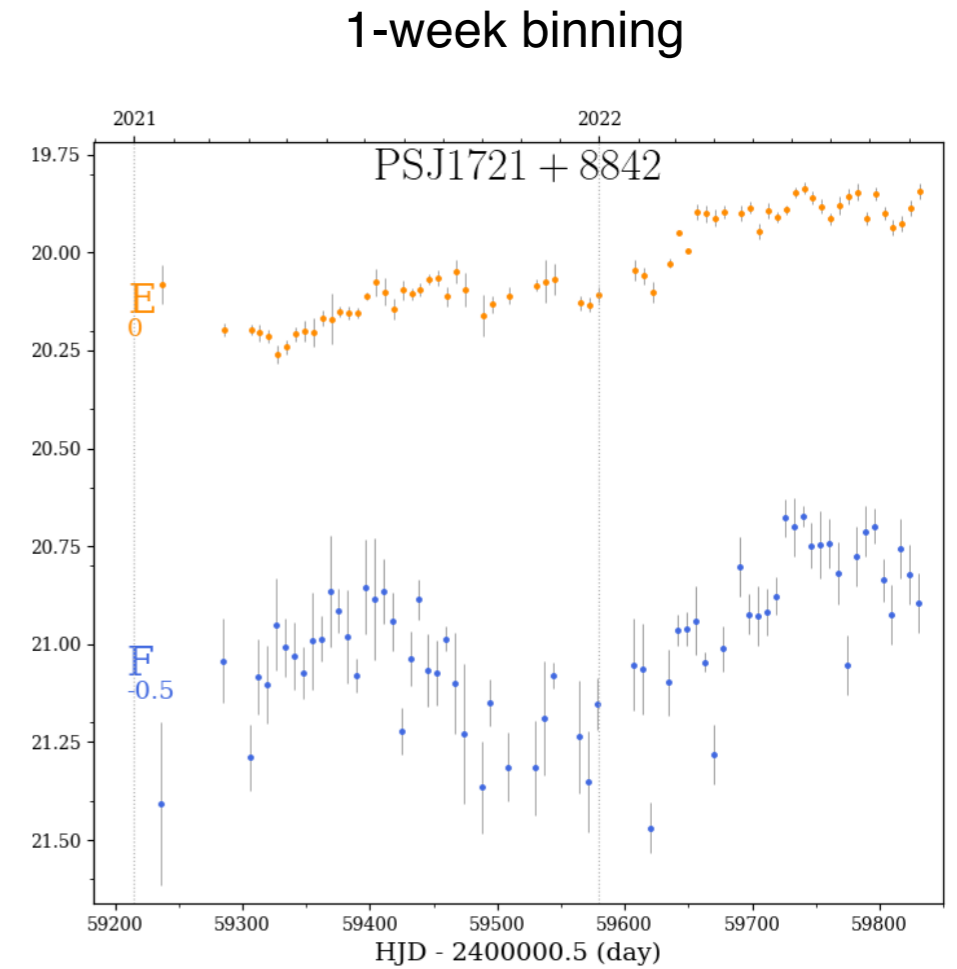
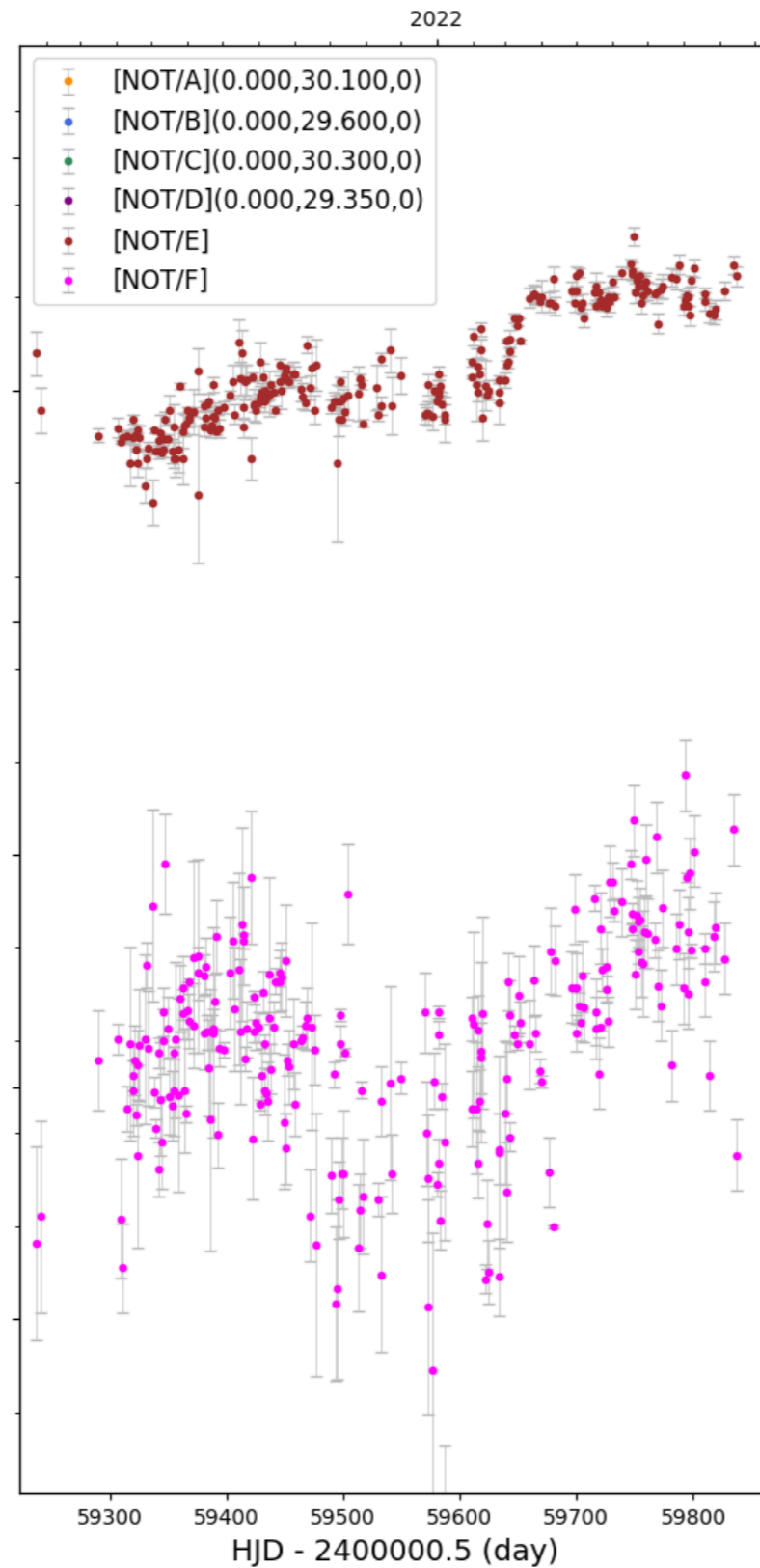
# The 6-image quasar J1721+88 : NOT light curves



# The 6-image quasar J1721+88 : NOT light curves



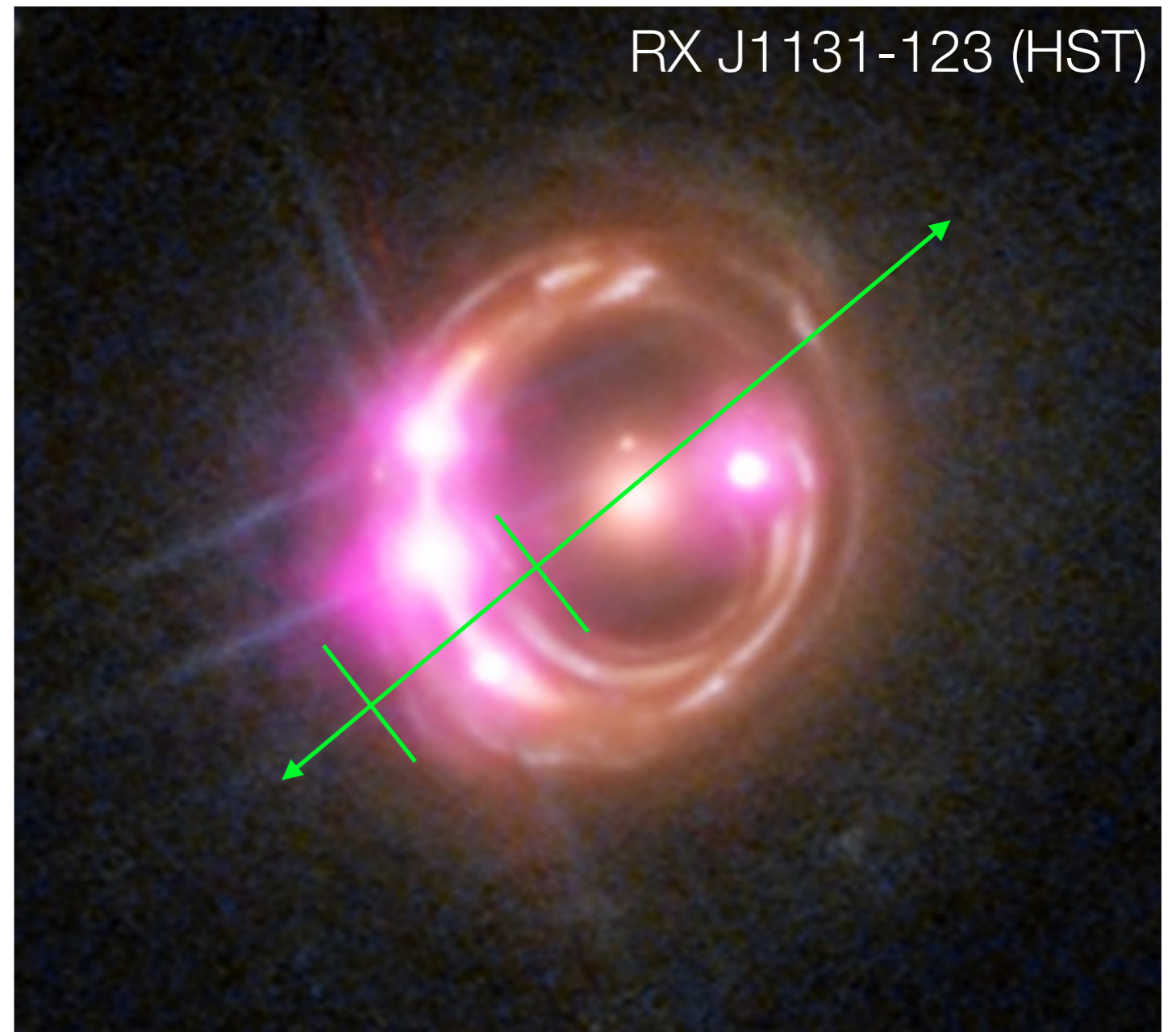
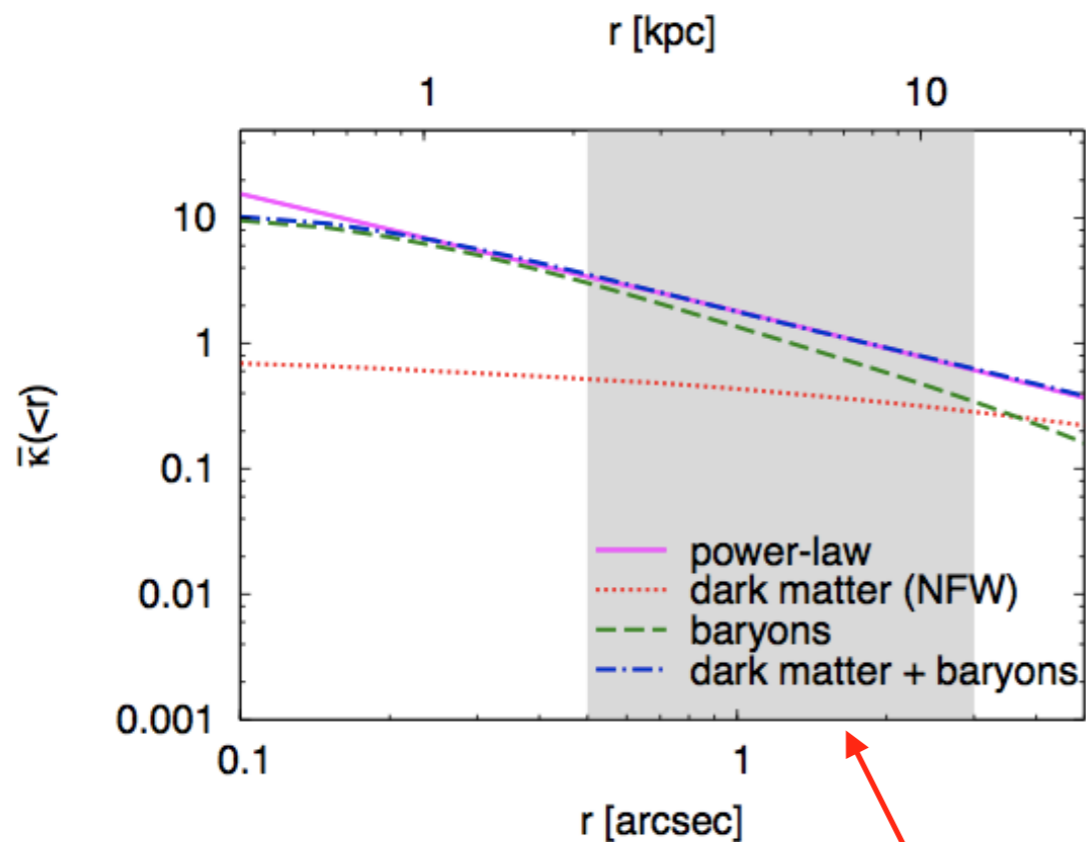
Daily cadence





## 2- Constraining the Mass Slope

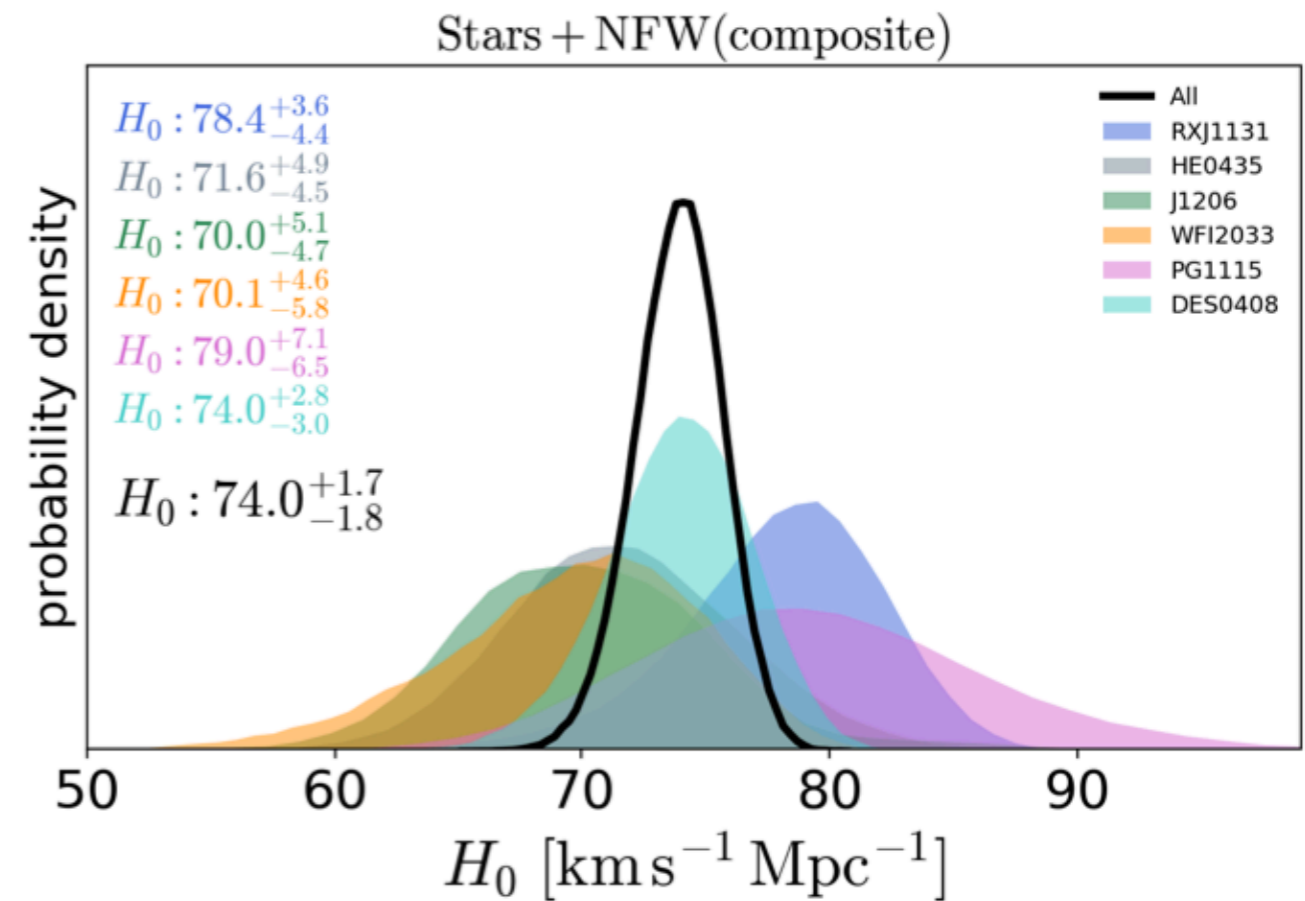
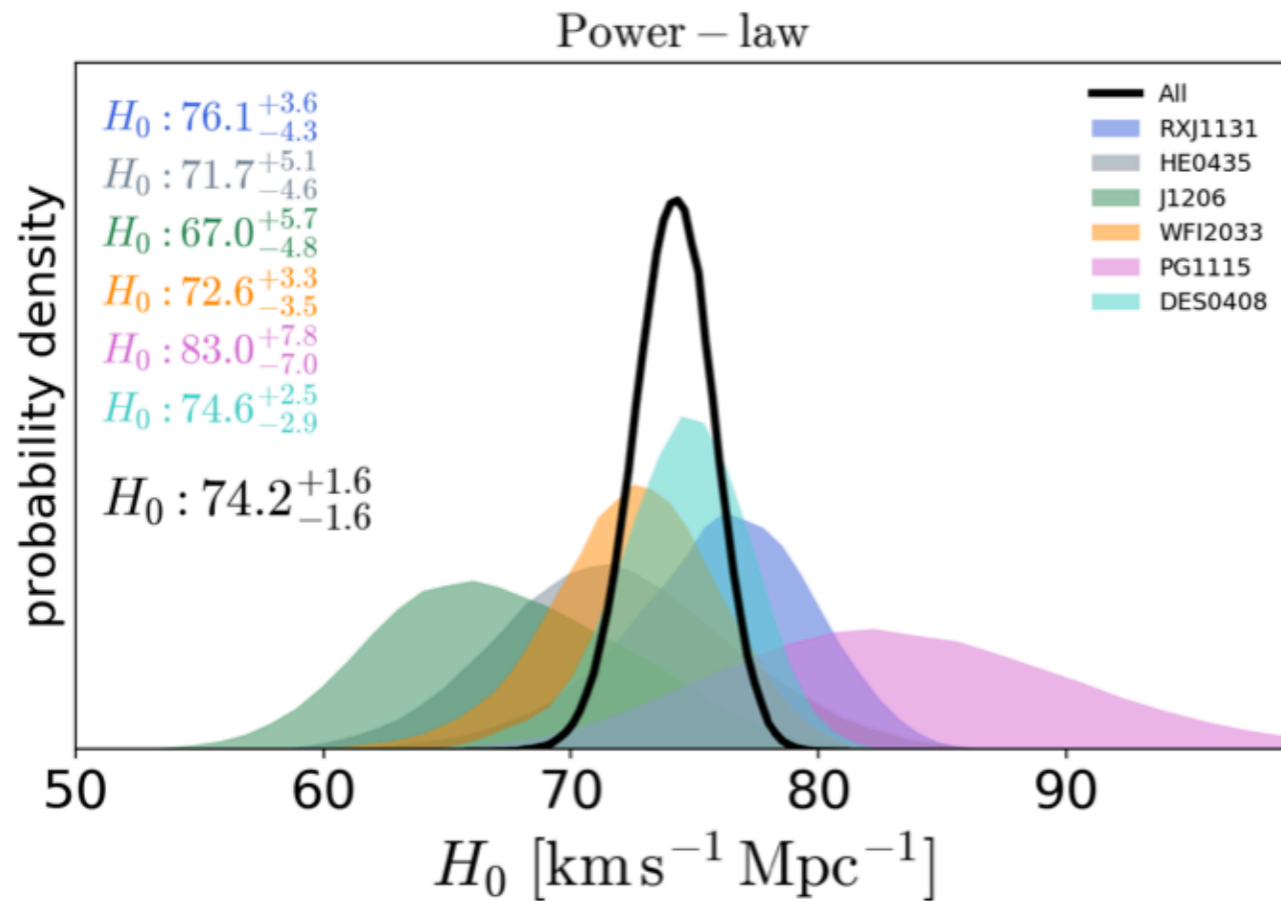
# Constraining Models with Thick Rings



Lensing constraints come from all pixels covered by the Einstein ring formed by the quasar host

More complex models and simple power-law converge to the same mass slope

# No Significant Dependence on Lens Model



### 3- The Mass-sheet Transform (MST)

# Model Degeneracies: Mass Sheet Transform (MST)

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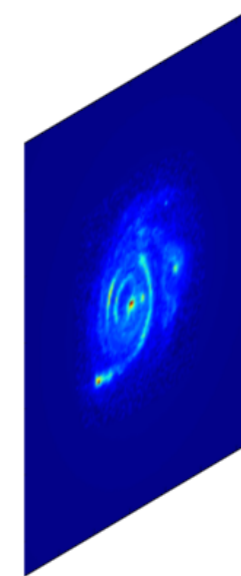
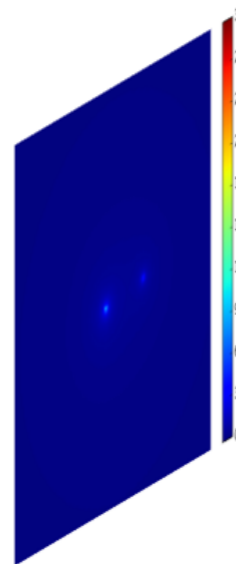
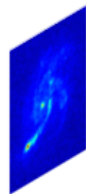
Source plane

Mass

Lensed images

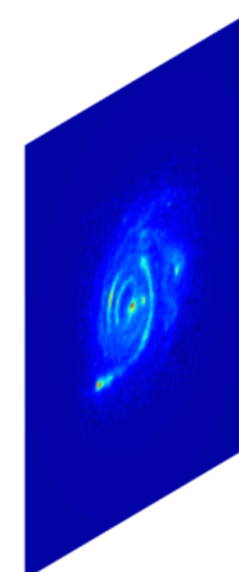
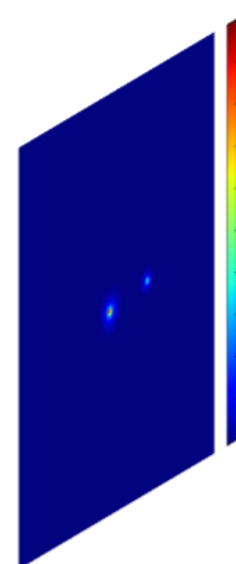
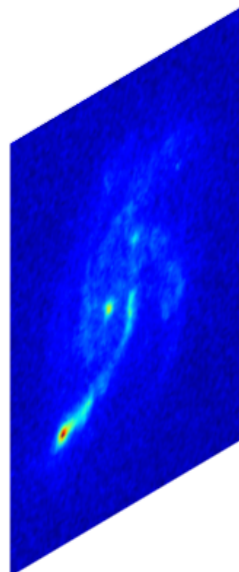
$\beta$

$\kappa$



$\lambda\beta$

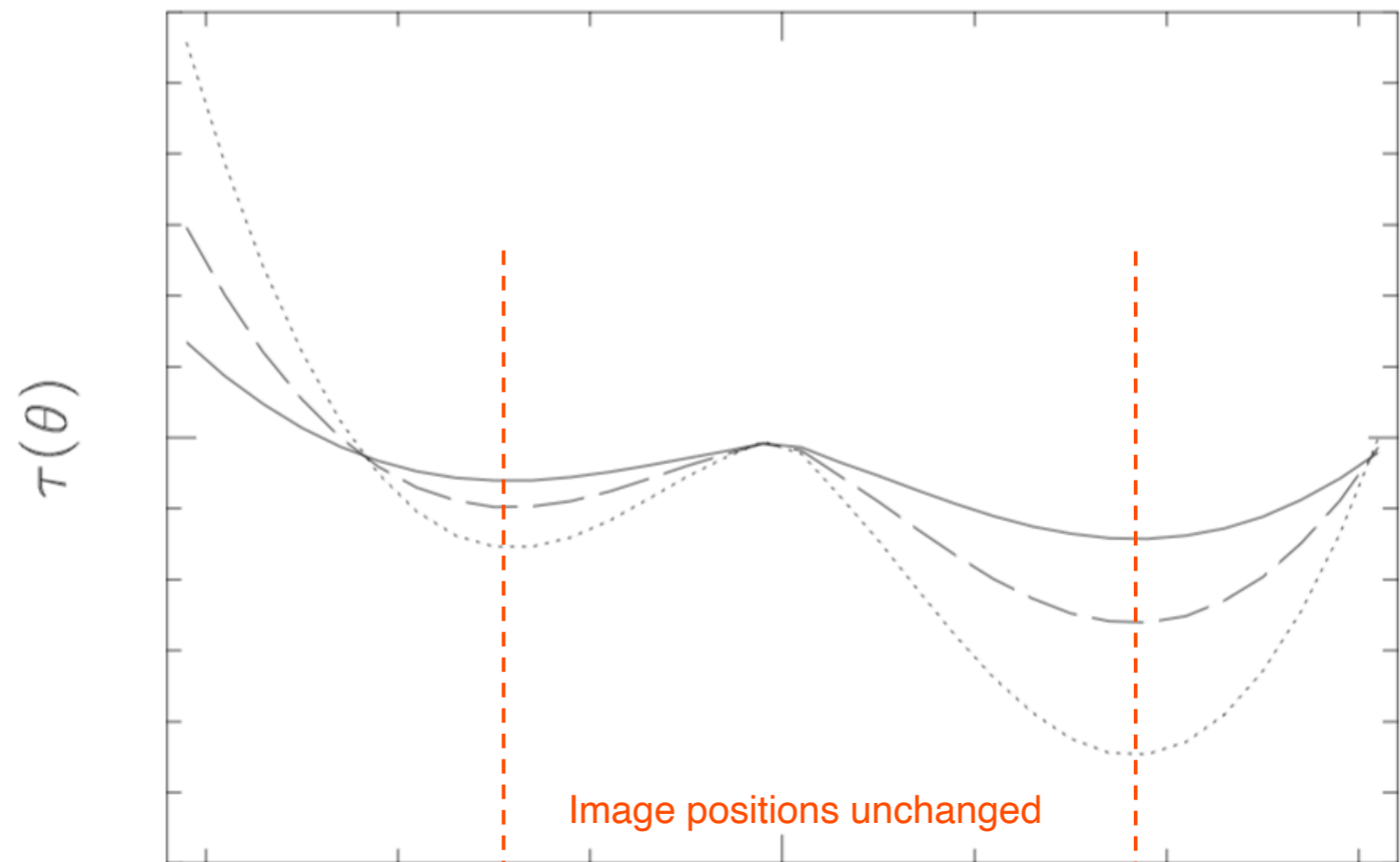
$\lambda\kappa + (1 - \lambda)$



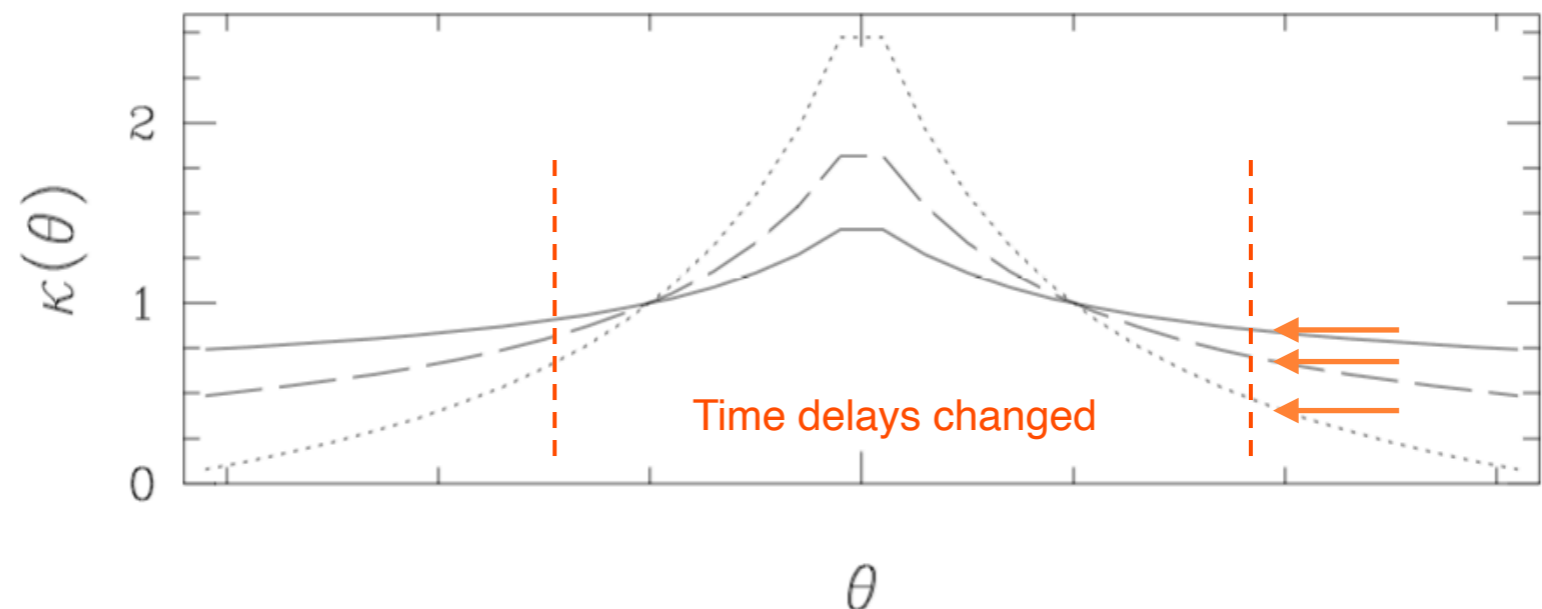
# Mass Sheet Transform (MST)

$$\kappa_\lambda(\vec{\theta}) = \lambda\kappa(\vec{\theta}) + 1 - \lambda$$
$$\vec{\beta}_\lambda = \lambda\vec{\beta},$$

Arrival time surfaces  
in the image plane

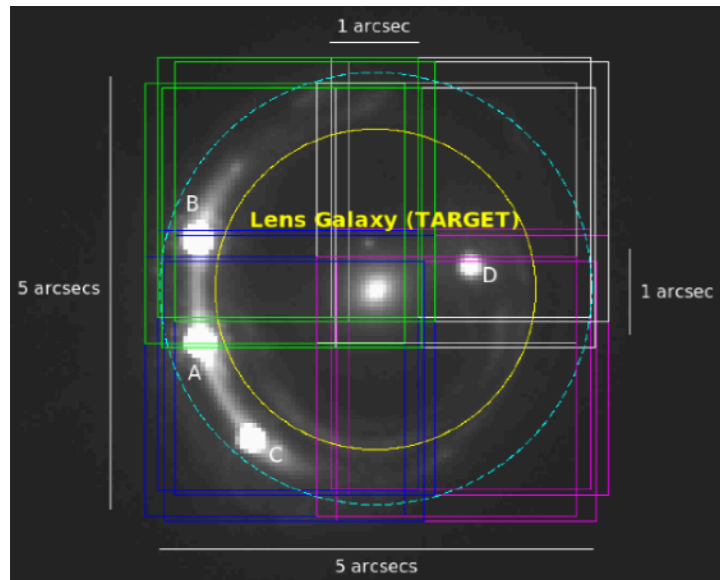


Normalized mass profile  
 $\kappa$  = projected mass density  
in units of the critical mass

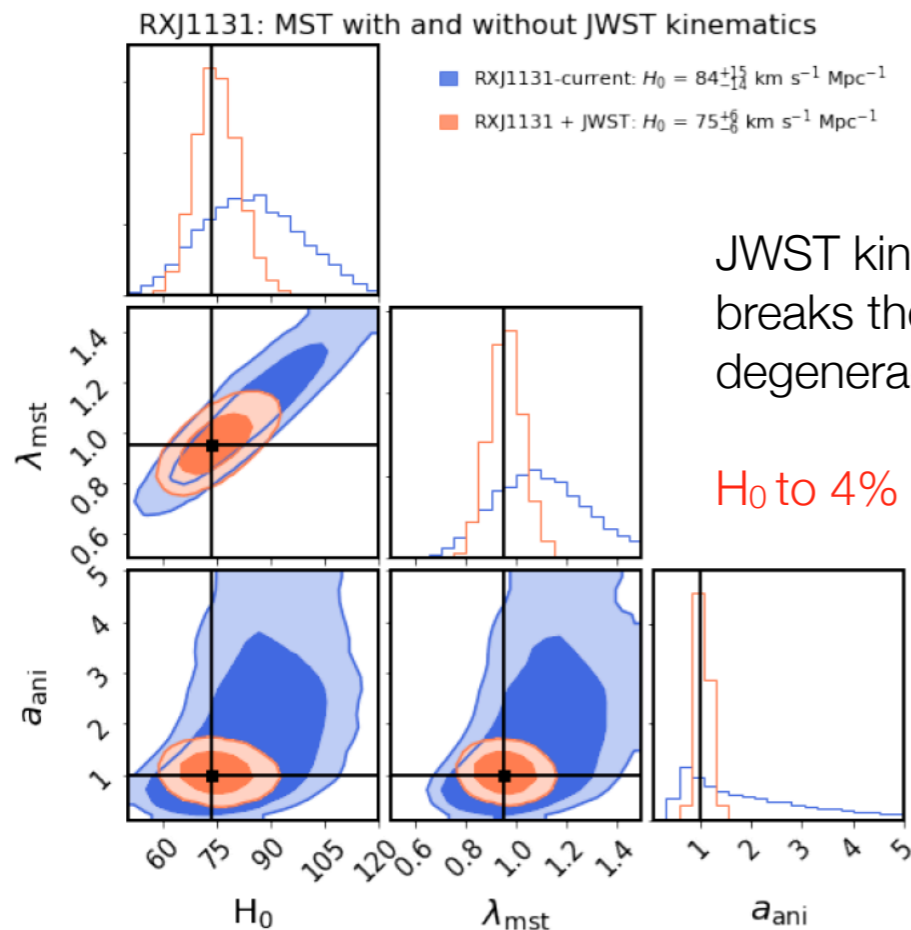


# Future Avenues

Spatially resolved kinematics  
(ongoing with VLT/MUSE, Keck KCWI, JWST pending)

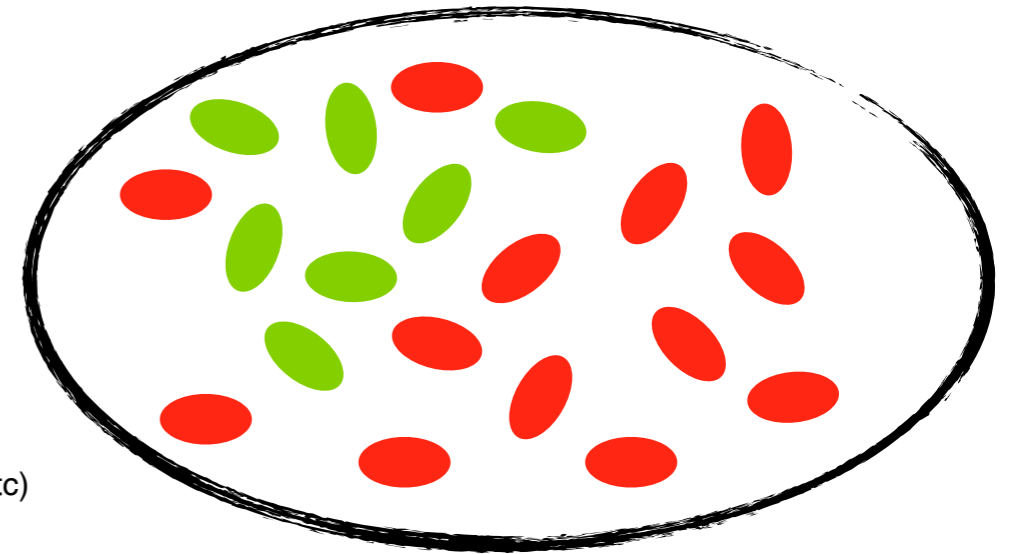


Accepted JWST dithers with NIRSspec (exp. time: 6.5h)



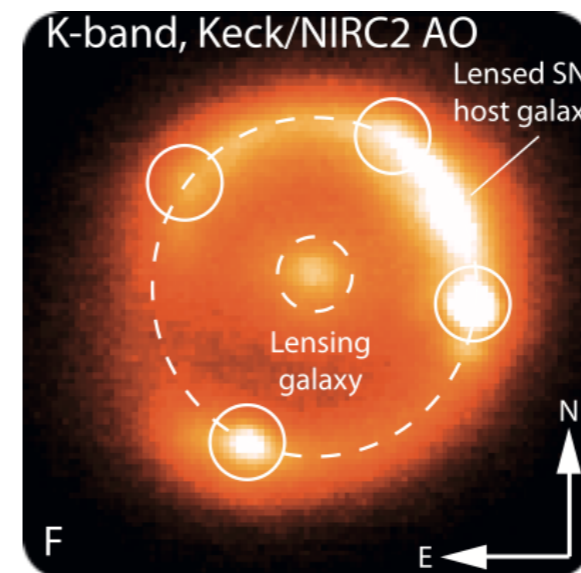
Hierarchical Bayesian Analysis for both cosmology and galaxy evolution

● Time-delay lenses (TDCOMOS)  
● Non-time-delay lenses (Euclid, LSST, etc)



$H_0$  to 1.2% with 40 delays + 200 lenses with no time delay but resolved kinematics (Euclid is a key-player here !)

Lensed supernovae



Ongoing search

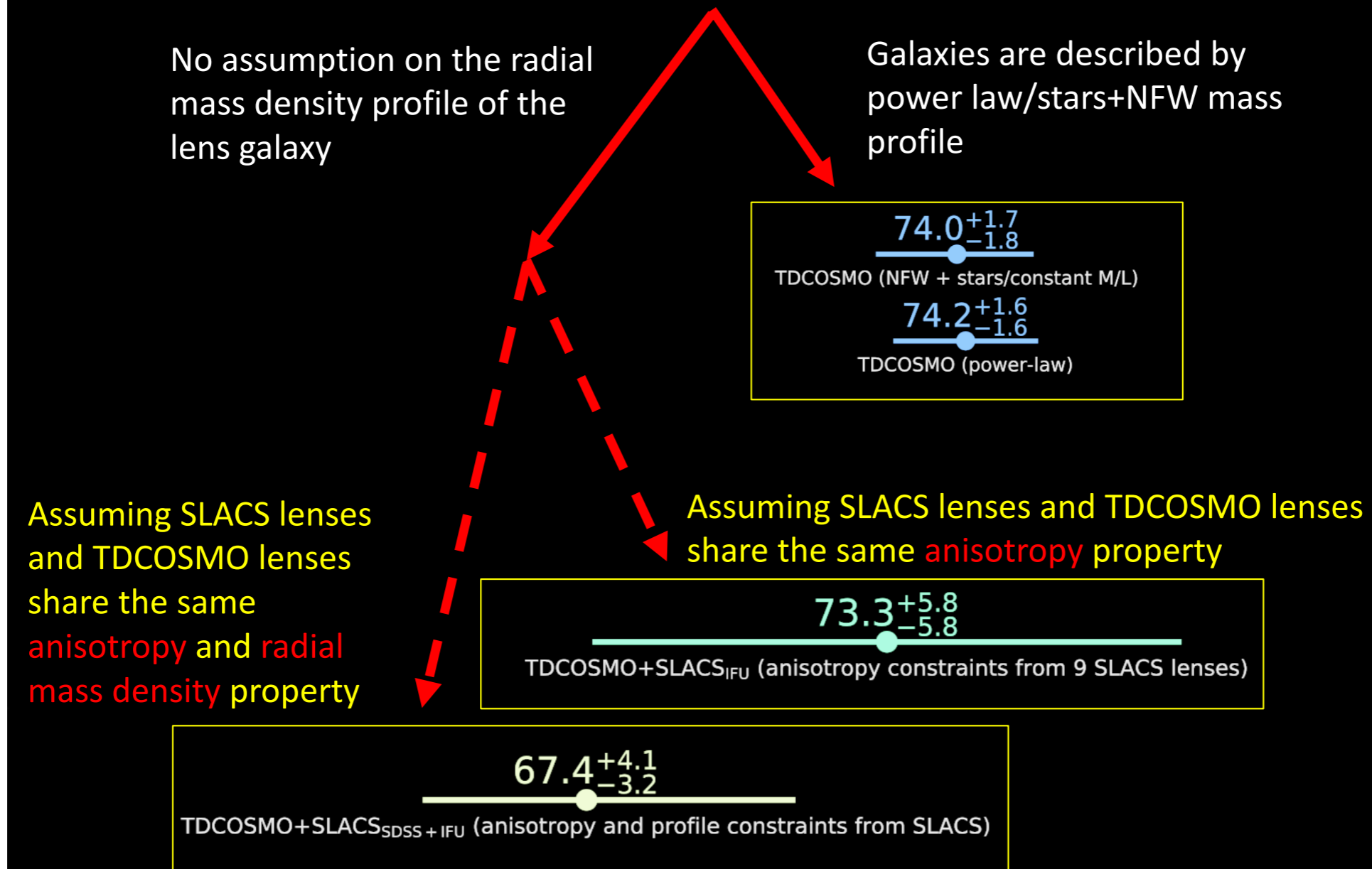
- in ZTF alerts
- by monitoring monthly known lenses
- in ongoing VST large program

Approved ToO follow-up at VLT (MUSE + XShooter)

Goobar et al. (2017, Science 356, 291)

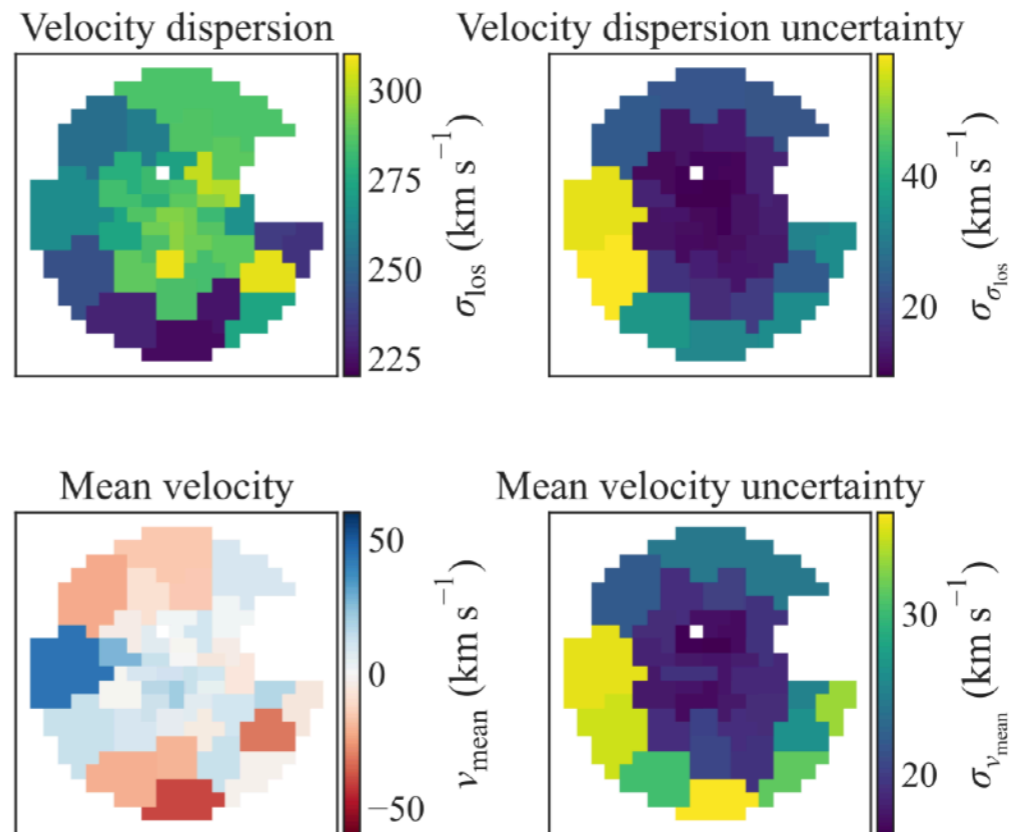
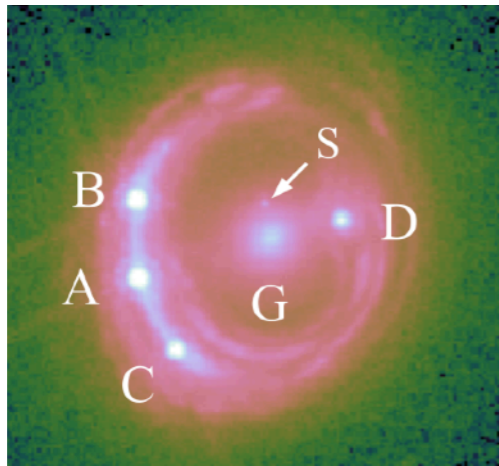
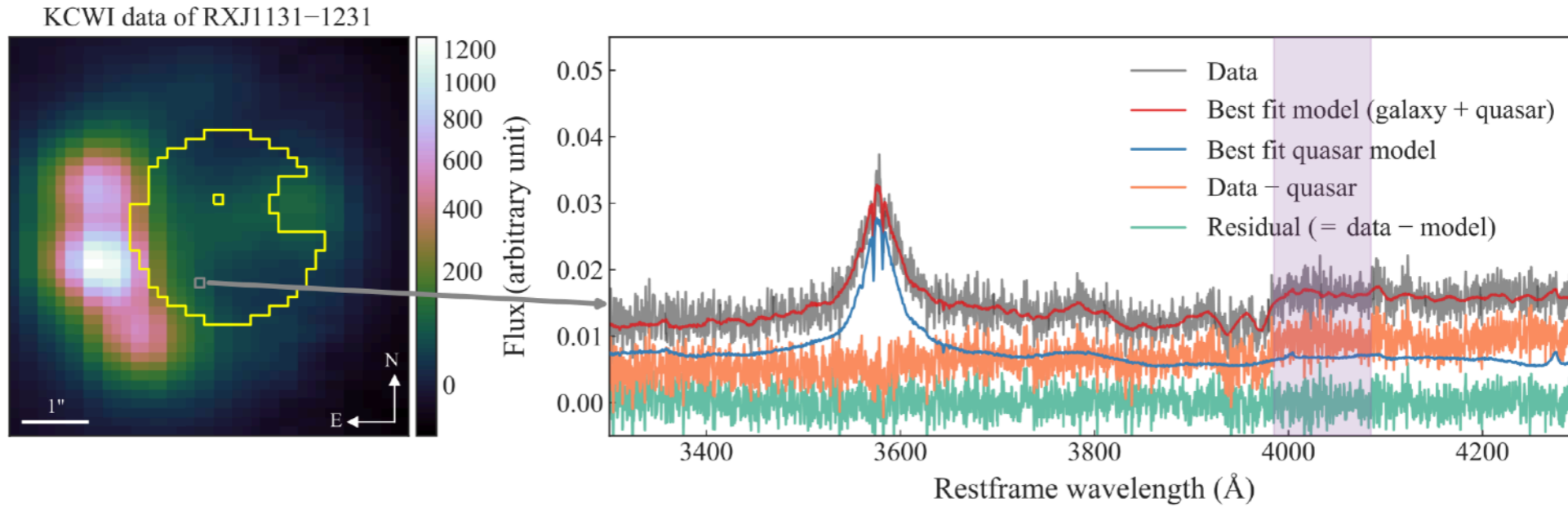
# Avenue #1 - Hierarchical Bayesian Analysis

## TDCOSMO - decision Tree





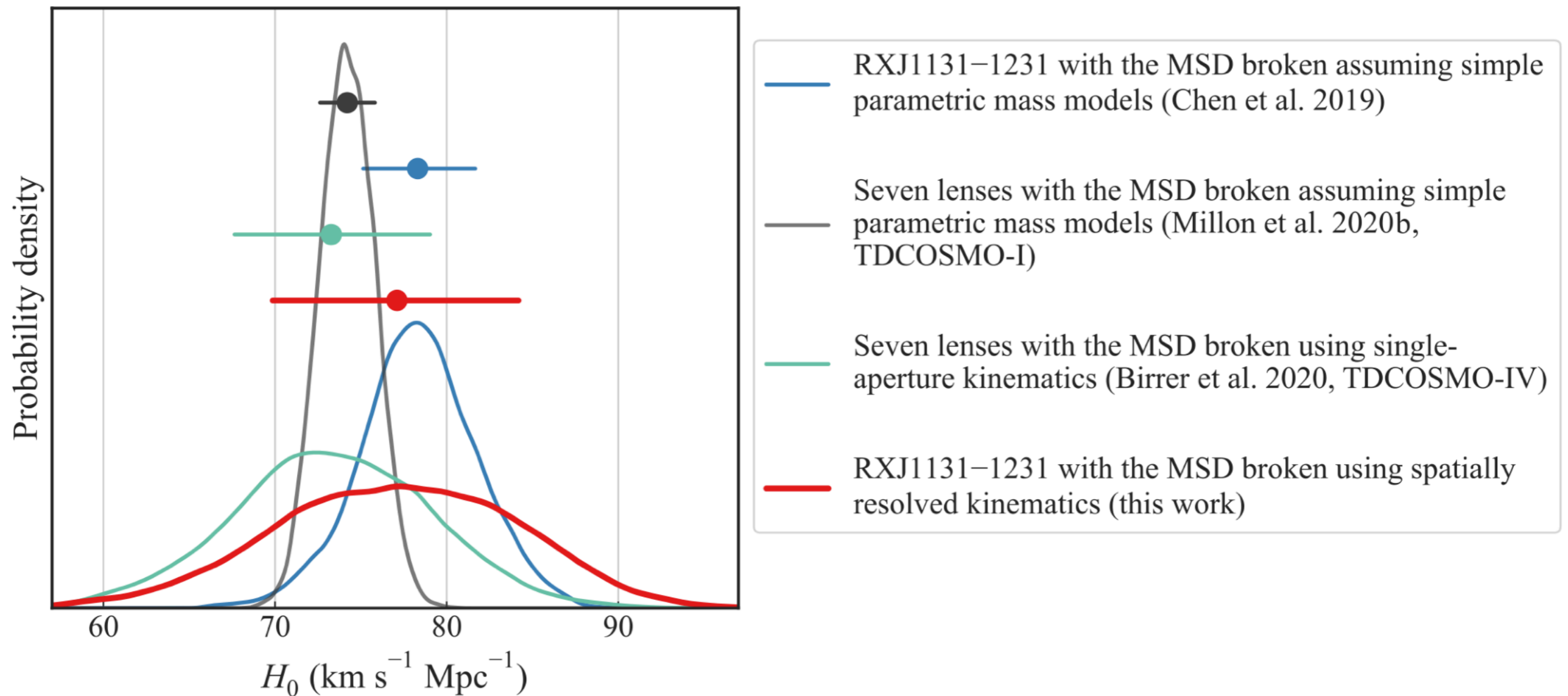
# Avenue #2 - Dynamics of Time-Delay Lens Galaxies



4h of Keck KCWI IFU spectroscopy (no-AO)

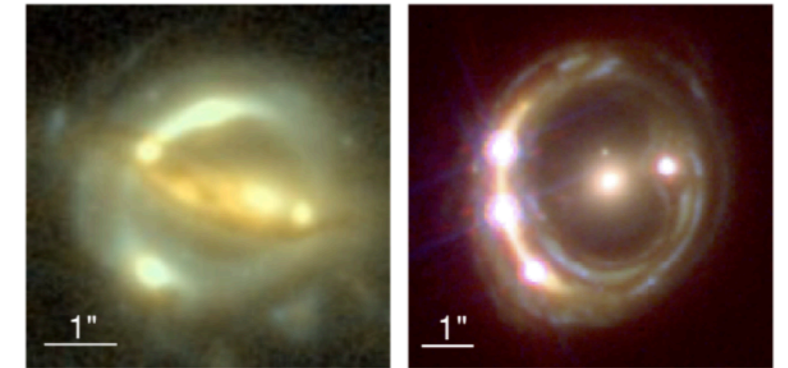
More to come with VLT-MUSE, Keck, JWST

# Avenue #2 - Dynamics of Time-Delay Lens Galaxies



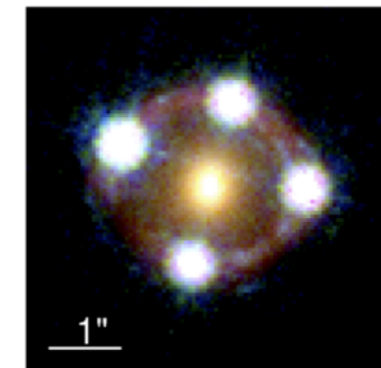
# Summary

- Strong lensing time delays consist in an **absolute distance indicator**
- Time delays are measured to a few percents within **1-2 seasons**
- **7 lenses** give  $H_0$  with accuracy and precision comparable to supernovae and are **independent**
- **In flat lambda-CDM  $H_0 = 74.0 \pm 1.8 \text{ km.s}^{-1}.\text{Mpc}^{-1}$**
- The **Mass-Sheet-Degeneracy** needs to be addressed
- Avenue #1: **Hierarchical analysis: more work needed**
- Avenue #2: **Resolved kinematics: supports previous analysis**

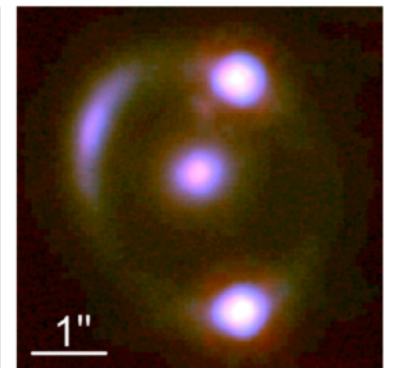


(a) B1608+656

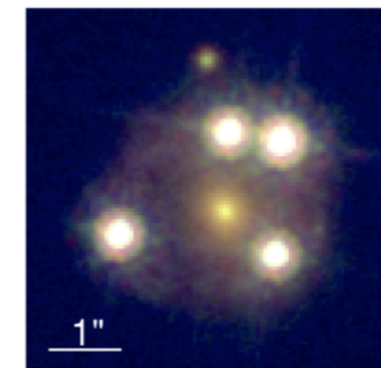
(b) RXJ1131-1231



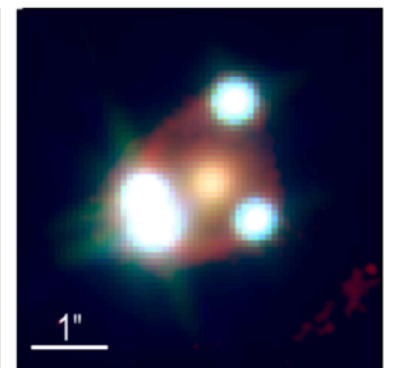
(c) HE 0435-1223



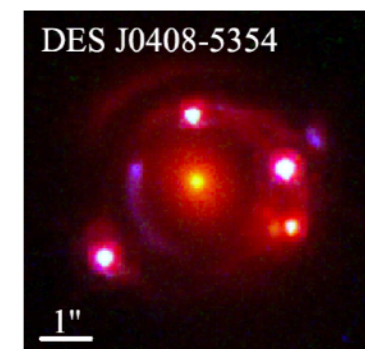
(d) SDSS 1206+4332



(e) WFI2033-4723



(f) PG 1115+080



DES J0408-5354